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# Nuclear structure functions at $x > 1$ : Searching for Super-fast quarks

- Inclusive scattering at  $x > 1$ 
  - Quasielastic  $\rightarrow$  SRCs
  - DIS  $\rightarrow$  pdfs at  $x > 1$ : mapping out superfast quarks
  - JLab6, 12, EIC?

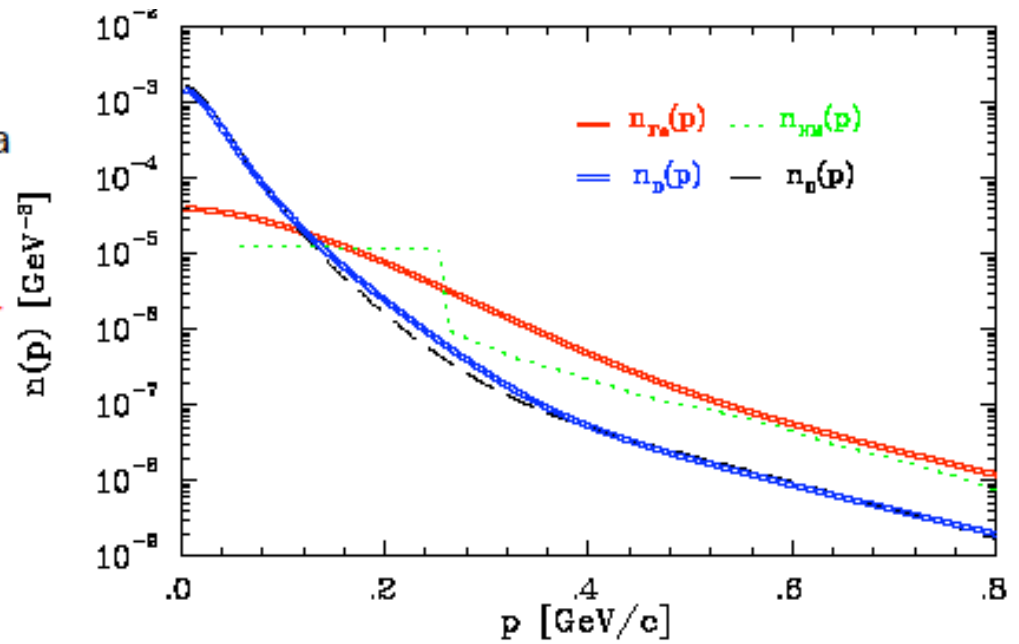
John Arrington, Argonne National Lab,  
EIC-NUC2010, April 9<sup>th</sup>, 2010



QE scattering,  $x > 1$ :  
 high-momentum nucleons,  
 Short-range correlations

Deuteron and  
 Iron fits to data  
 ( $y^*$ -scaling)

Deuteron and  
 nuclear matter  
 calculations.

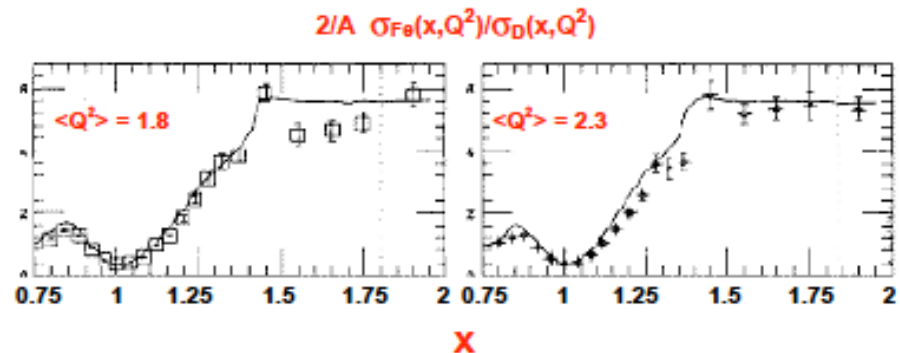


Same high momentum behavior seen is for C, Au (lower quality data)

Distribution at high momentum has same shape for deuteron  
 and heavy nuclei - 2N SRCs appear to dominate.

Same as seen in cross section ratios,  $\sigma_A/\sigma_D$  at large  $x$ .

Fe data from SLAC NE3  
 $^2\text{H}$  data interpolated to  
 NE3 kinematics from  
 older SLAC experiments.

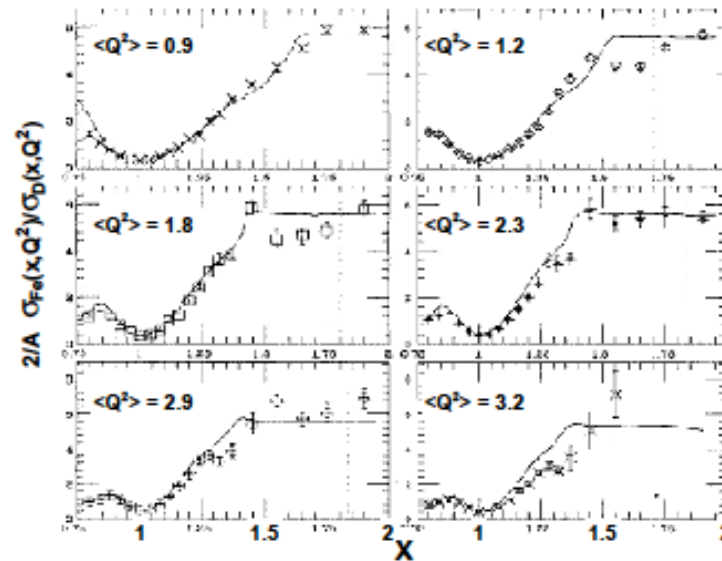


## SRCs in $\sigma_A/\sigma_D$ Ratios

$\sigma_A/\sigma_D$  ratios show that heavy nuclei and deuterium have similar high momentum tails in regions where mean field motion is negligible ( $x > 1.5$ ).

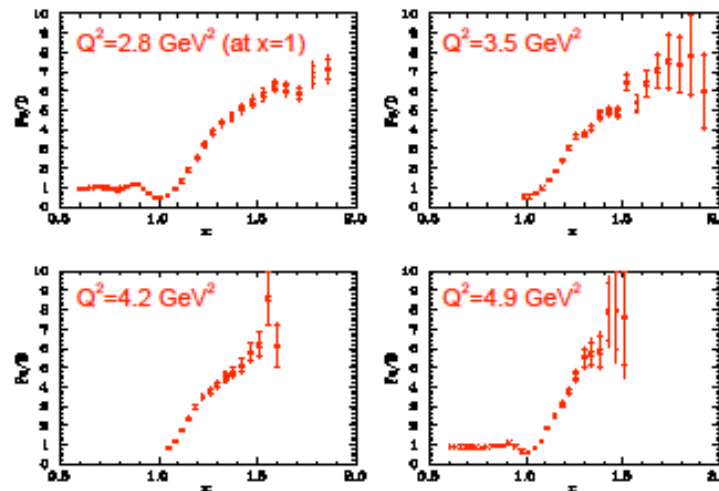
### SLAC

Fe data from NE3.  
Deuterium data is interpolated to NE3 kinematics from previous SLAC measurements.



### JLab - Hall C

Ratios limited by lack of high-x deuterium data. (89-008 was a short run focussed on heavy nuclei).



SLAC - combined deuterium and heavy target data from different experiments

Hall B - Measured ratios of heavy targets to  $^3\text{He}$ , rely on measured or calculated  $^3\text{He}/^2\text{H}$

Hall C (4 GeV) - Experiment did not focus on deuteron, so  $x$  coverage is poor at large  $Q^2$

E02-019 (6 GeV) -  $^2\text{H}$ ,  $^3\text{He}$ ,  $^4\text{He}$ , and heavy nuclei; paper in preparation

CLAS data,  $\text{Fe}/^3\text{He}$

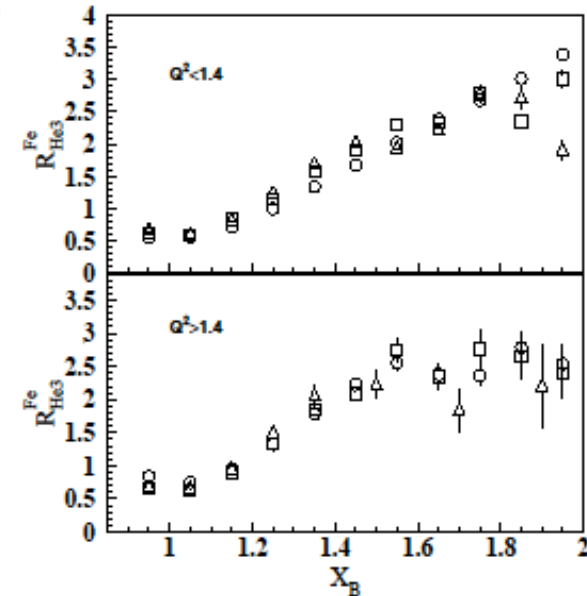
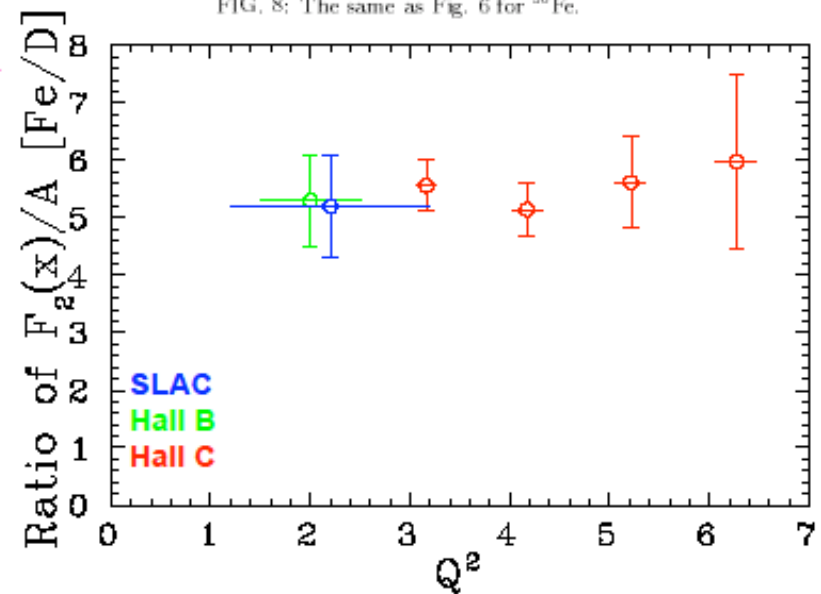


FIG. 8: The same as Fig. 6 for  $^{56}\text{Fe}$ .

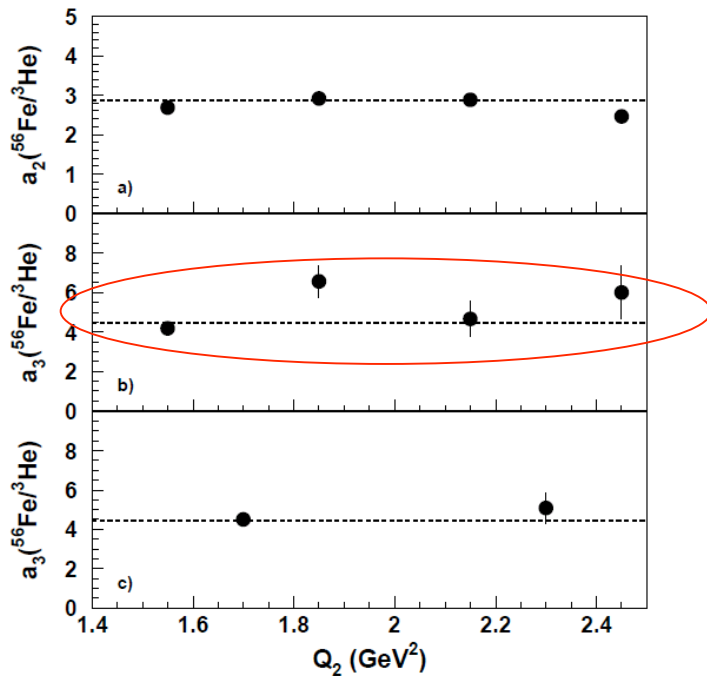
$F_2^{\text{Fe}}/F_2^{\text{D}}$  at large  $x$



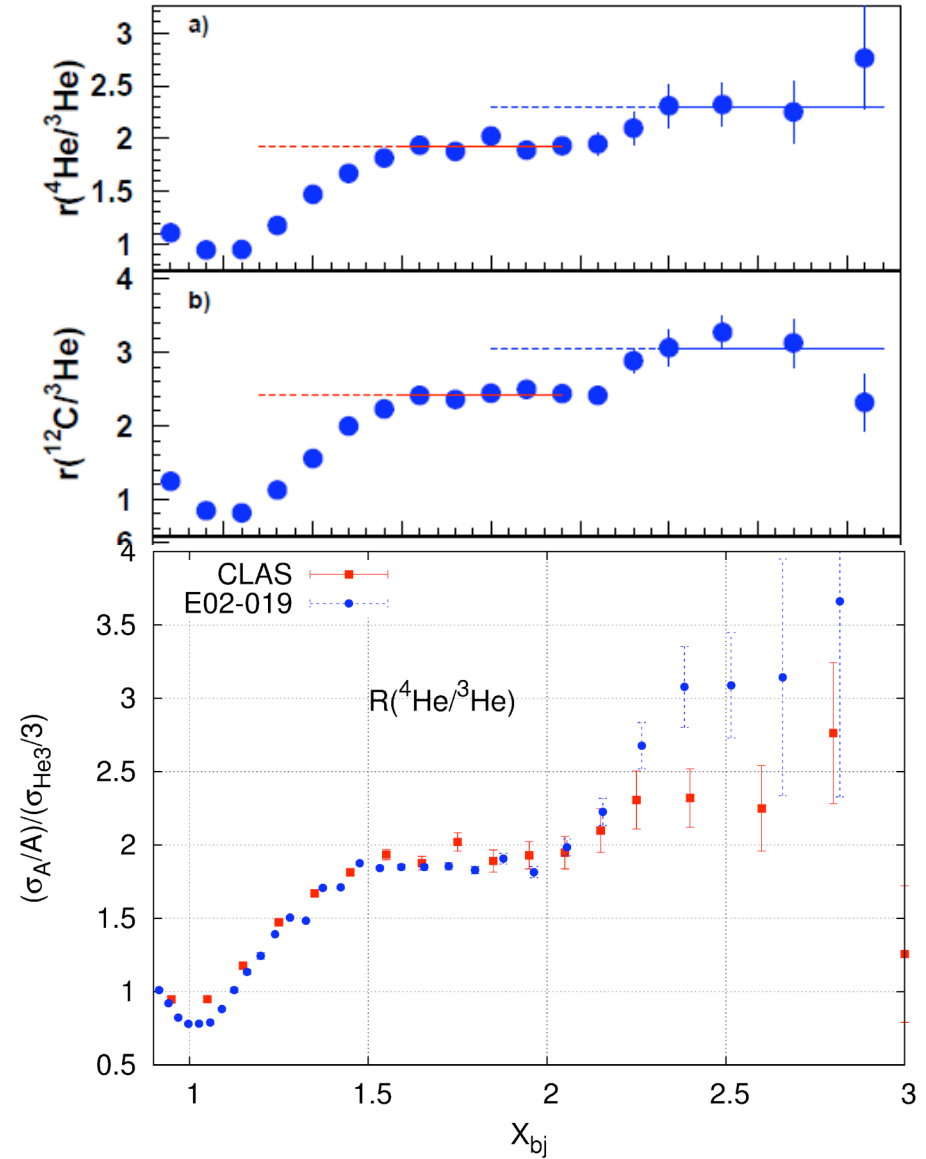
# CLAS: 3N-SRCs

- $A/{}^3\text{He}$  ratios for  $x > 2$  should show similar plateau if 3N-SRCs dominate and have A-independent structure
- CLAS ratios: first such suggestion of 3N-SRCs

$Q^2$  low (dominated by  $Q^2 < 1.7 \text{ GeV}^2$ )

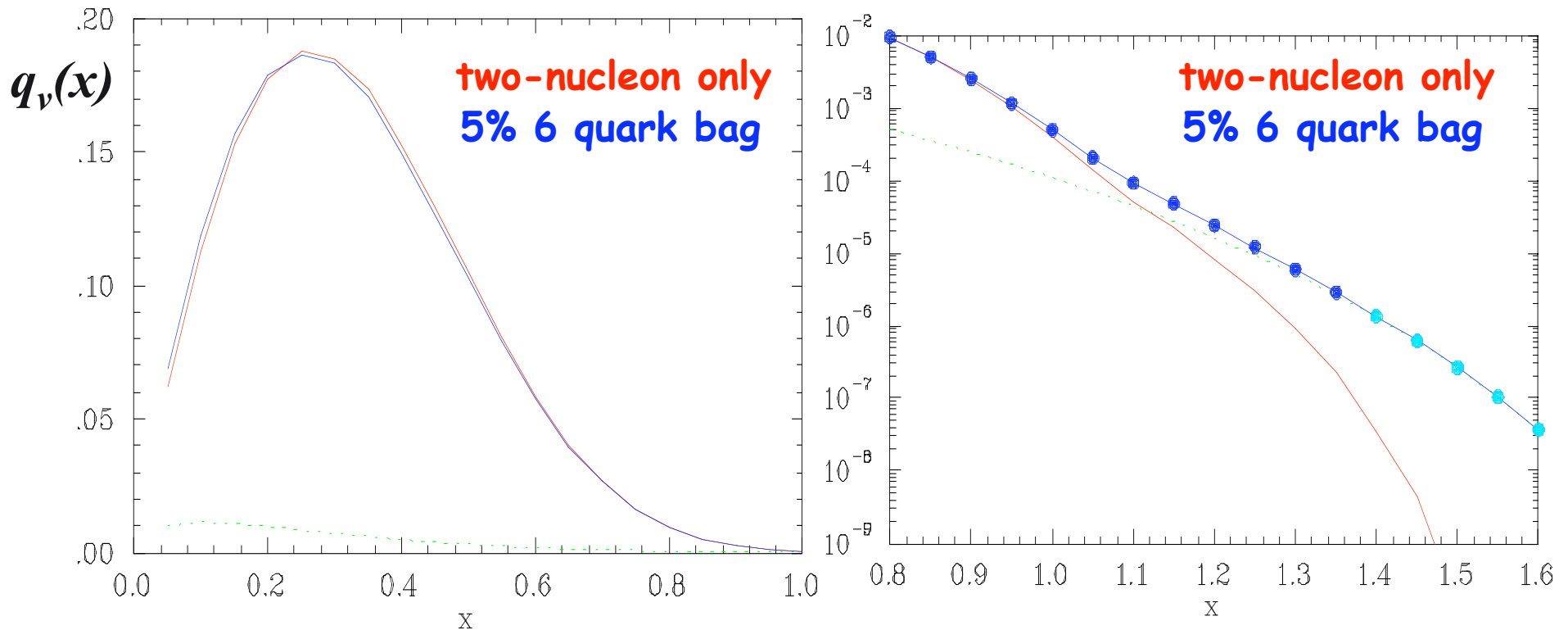


*K. Egiyan et al, PRL96, 082501 (2006)*



# DIS at $x > 1$ : Superfast quarks, short range structure

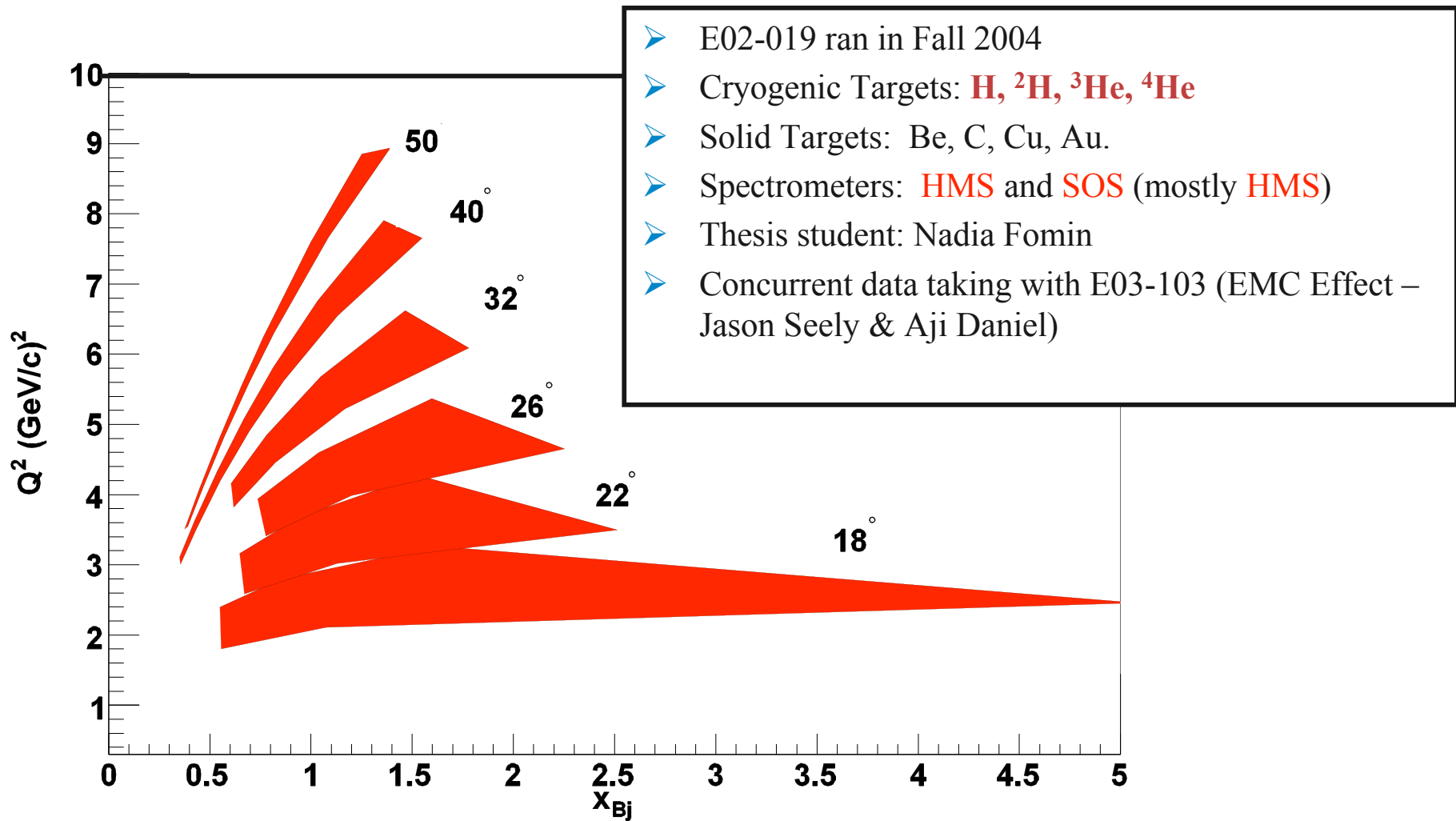
- 12 GeV  $x > 1$  proposal  $\rightarrow$  DIS-dominated scattering in SRC-dominated kinematics
- Exotic states, where nucleons share momentum (e.g. 6q bag), yield much larger “EMC” effect at  $x > 1$



## What do we know about superfast quarks?

- 2 results for high  $x$  SFQ distributions (**CCFR** & **BCDMS**)
  - both fit  $F_2$  to  $\exp(-sx)$ , where  $s$  is the “slope” related to the SFQ distribution fall off.
  - **CCFR**:  $s=8.3\pm 0.7$  ( $Q^2=125$  GeV/c<sup>2</sup>) “*very large short range structure*”
    - *Poor resolution in  $x$*
  - **BCDMS**:  $s=16.5\pm 0.5$  ( $Q^2: 52-200$  GeV/c<sup>2</sup>) “*little short range structure*”
    - *Low statistics (only upper limits above  $x=1.05$ )*
  
- Plenty of lower  $Q^2$  data (SLAC, JLab E89-008 (4 GeV))
  - Not in DIS region (but not clear how to define for  $x>1$ )
  - Expect large higher twist contributions at large  $x$
  - However, even at very low  $Q^2$  (to about 3 GeV<sup>2</sup>), the data showed qualitatively scaling vs Nachtmann  $\xi$

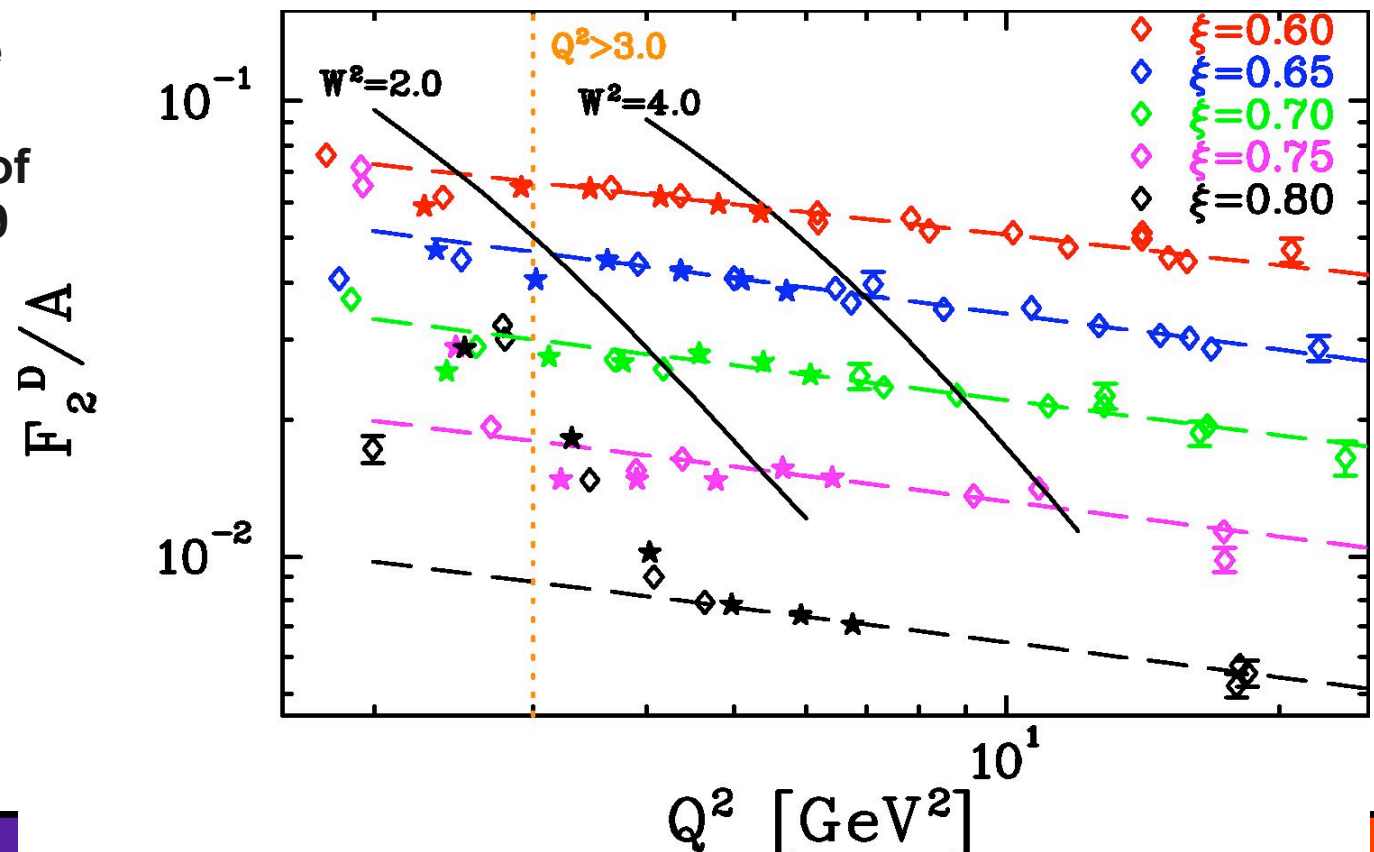
# E02-019: Hall C at JLab





# Scaling of the nuclear structure functions

- Low  $Q^2$  JLab data (from E89-008, 4 GeV) are consistent with extrapolated structure function from high  $Q^2$  SLAC data [ fixed  $d\ln(F_2)/d\ln(Q^2)$  ]
- Above  $\xi=0.65$ , there is a large gap between JLab, SLAC data, but there are indications of scaling up to  $\xi=0.75$
- New data fill in the gap up to  $\xi\sim 0.75$ , show indications of scaling up to  $\xi\sim 0.9$



# Step 1: Apply target mass corrections

$$F_2^{TMC}(x, Q^2) = \frac{x^2}{\xi^2 r^3} F_2^{(0)}(\xi) + \frac{6M^2 x^3}{Q^2 r^4} h_2(\xi) + \frac{12M^4 x^4}{Q^4 r^5} g_2(\xi)$$

Structure function including target mass corrections (i.e. as measured)

“Massless-limit” structure function: corresponds to large  $Q^2$  limit (i.e. to pdfs)

$$h_2(\xi, Q^2) = \int_{\xi}^1 du \frac{F_2^{(0)}(u, Q^2)}{u^2}$$

$$g_2(\xi, Q^2) = \int_{\xi}^1 dv (v - \xi) \frac{F_2^{(0)}(v, Q^2)}{v^2}$$

- We want  $F_2^{(0)}$ , the massless limit structure function as well as its  $Q^2$  dependence
- Need model for  $F_2^{(0)}$  to calculate  $h_2, g_2$

$$r = \sqrt{1 + \frac{4x^2 M^2}{Q^2}} \equiv \sqrt{1 + \frac{Q^2}{\nu^2}}$$

$$\xi = \frac{2x}{1 + \sqrt{1 + 4x^2 M^2 / Q^2}} = 2x / (1+r)$$

I. Schienbein et al, J.Phys G, 2008

# $F_2^{(0)}$ Model for TMCs

- Factorized  $\xi$ ,  $Q^2$  dependence
- $\sim$ logarithmic  $Q^2$  dependence (fit to world's data at several  $\xi$  values)
- For each target, interpolate nearby data to  $Q^2=7$ , fit  $F_2^{(0)}(\xi, Q^2=7)$

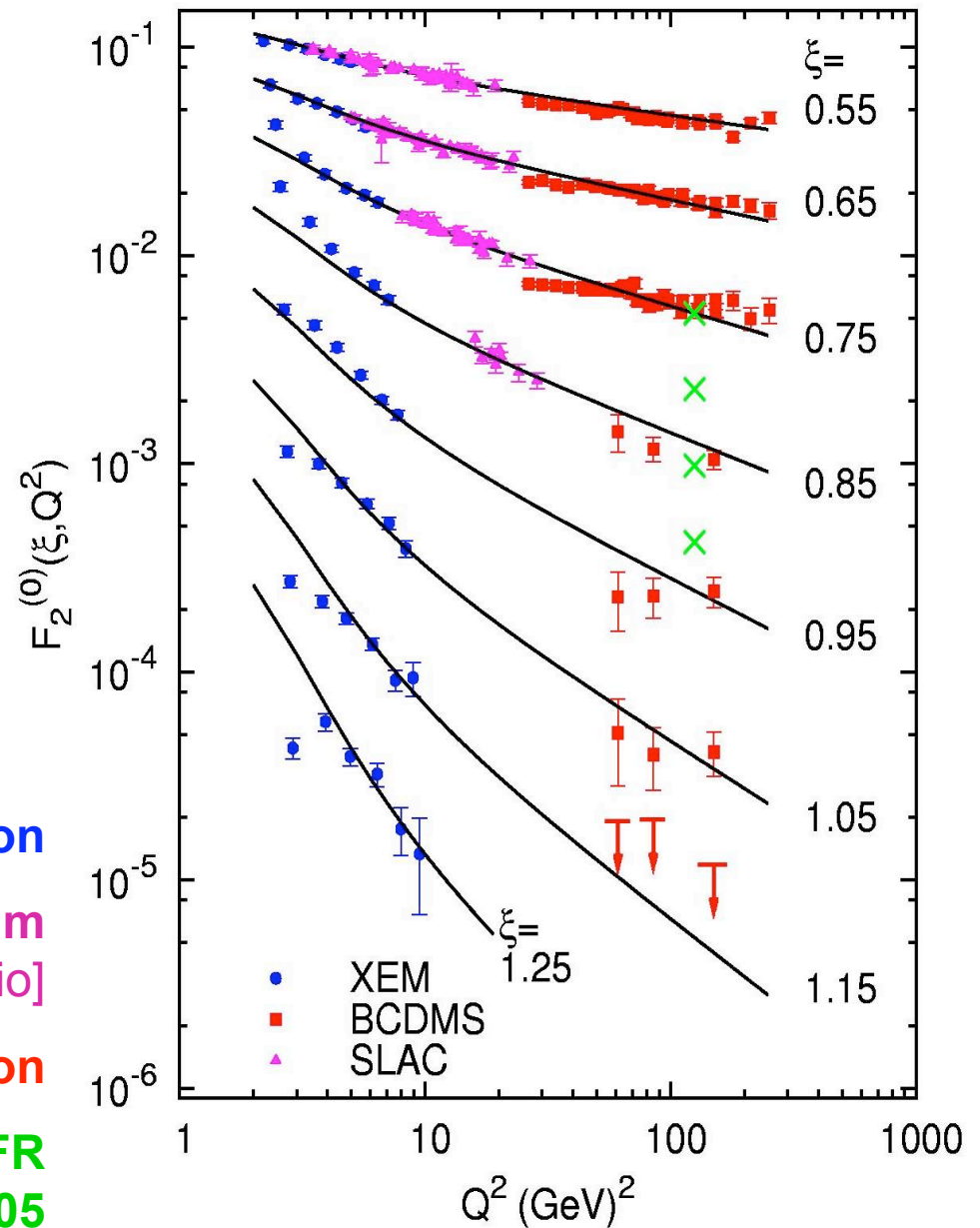
Model then used to apply TMC,  
estimate  **$\sim 2\%$  model-dependence**

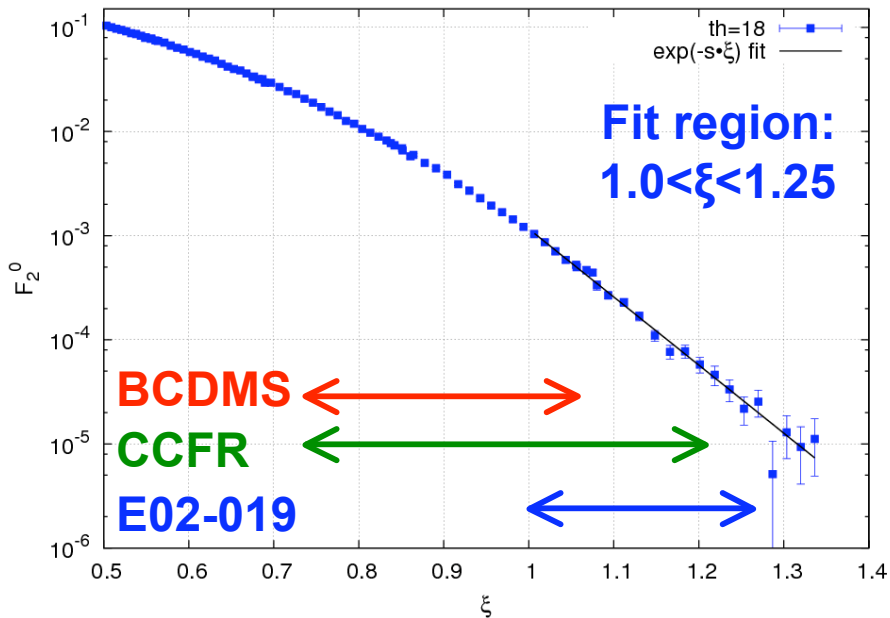
**E02-019 carbon**

**SLAC deuterium**  
[times SLAC C/D ratio]

**BCDMS carbon**

**x = projection of CCFR  
falloff, 0.75-1.05**

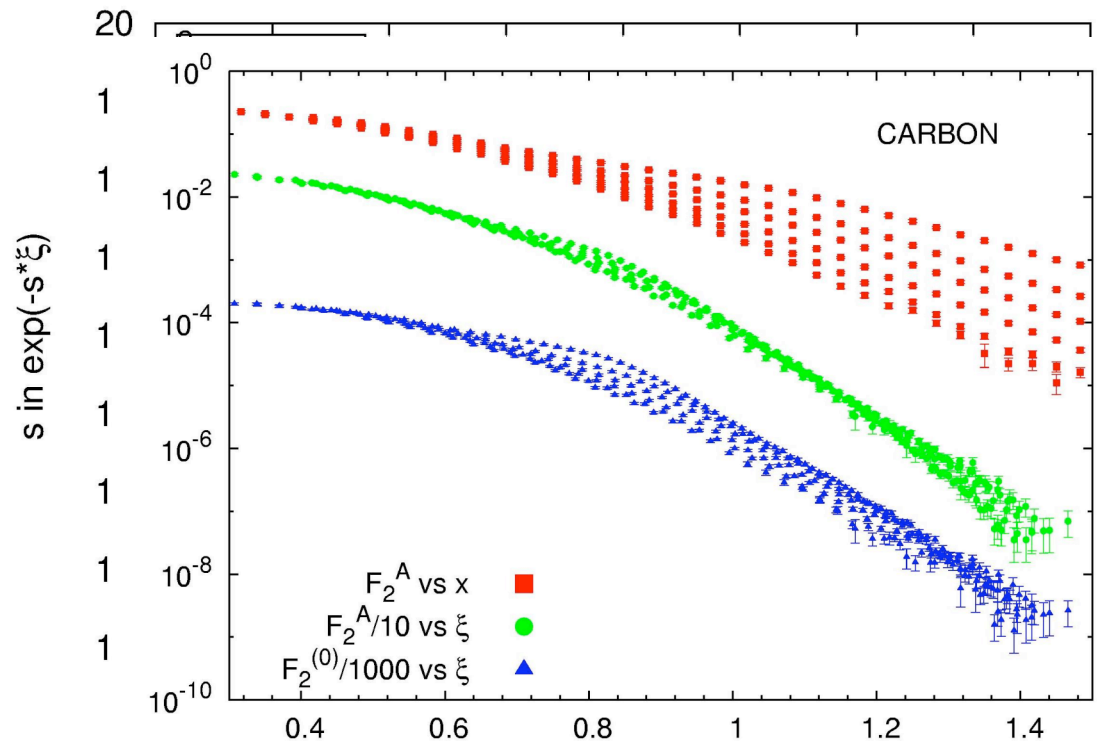




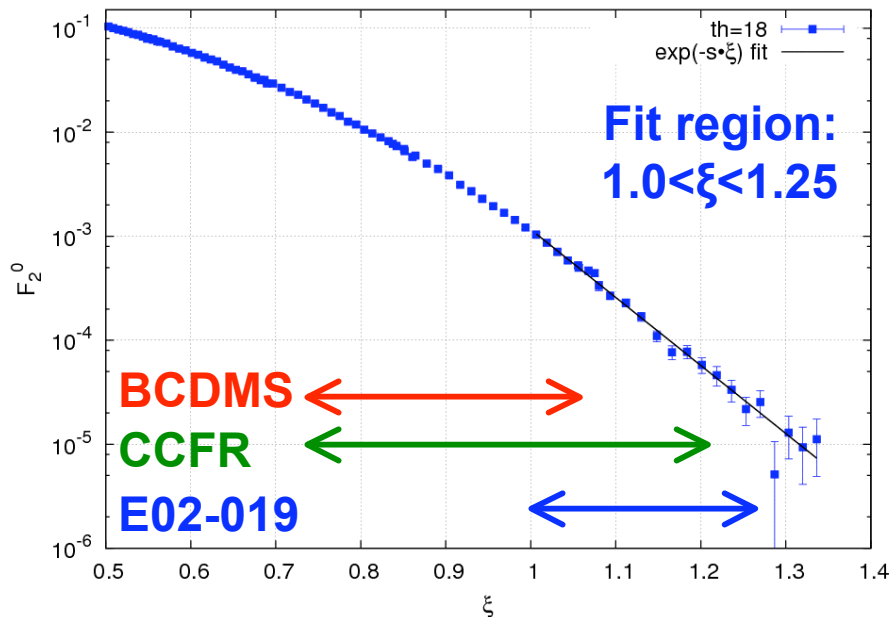
Final step: fit  $\exp(-s\xi)$  to  $F_2^0$  and compare to **CCFR** and **BCDMS**

**CCFR** ( $Q^2=125 \text{ GeV}^2$ )  
 $s=8.3 \pm 0.7$

**BCDMS** ( $Q^2: 52-200 \text{ GeV}^2$ )  
 $s=16.5 \pm 0.5$



# Some concerns about the comparisons

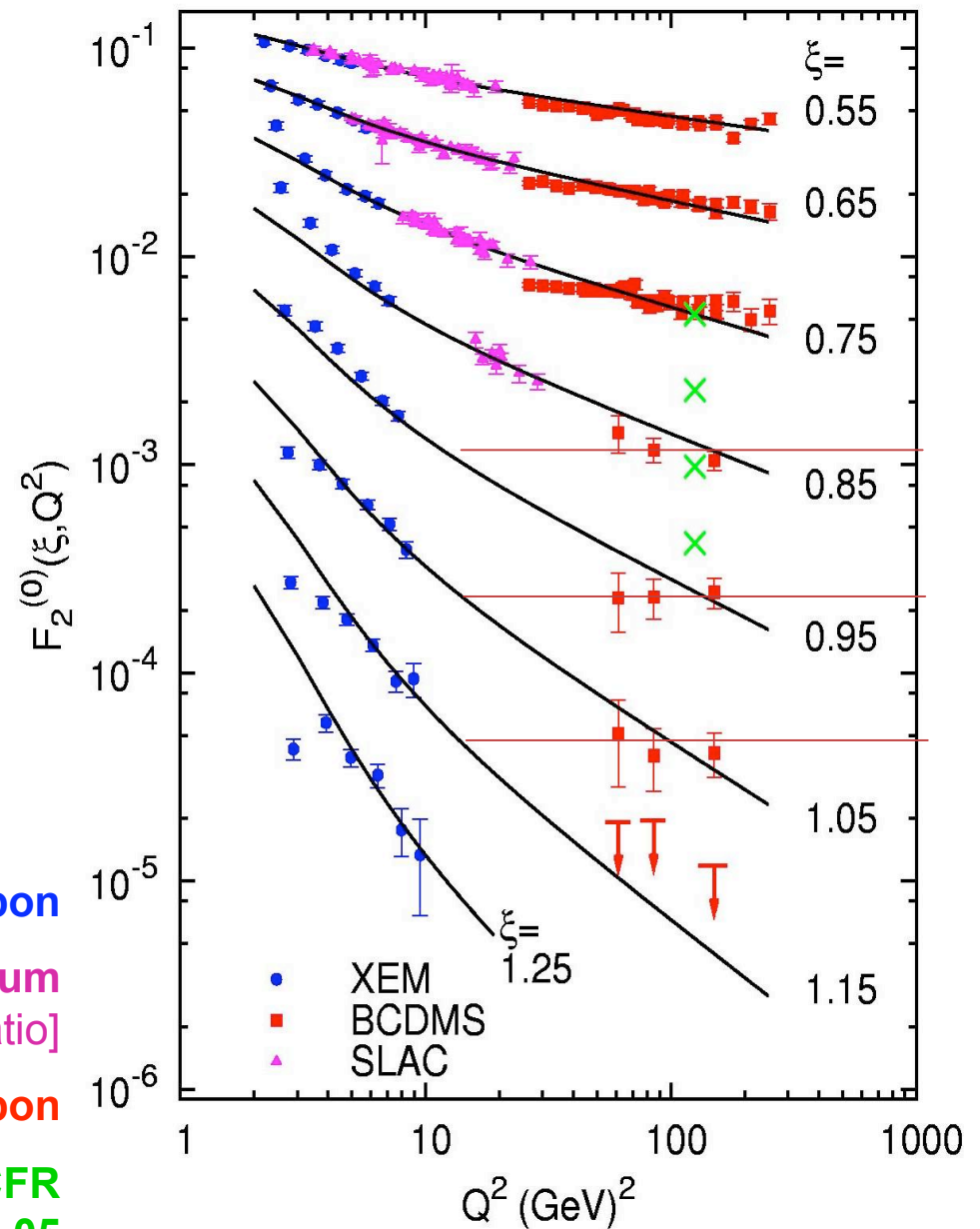


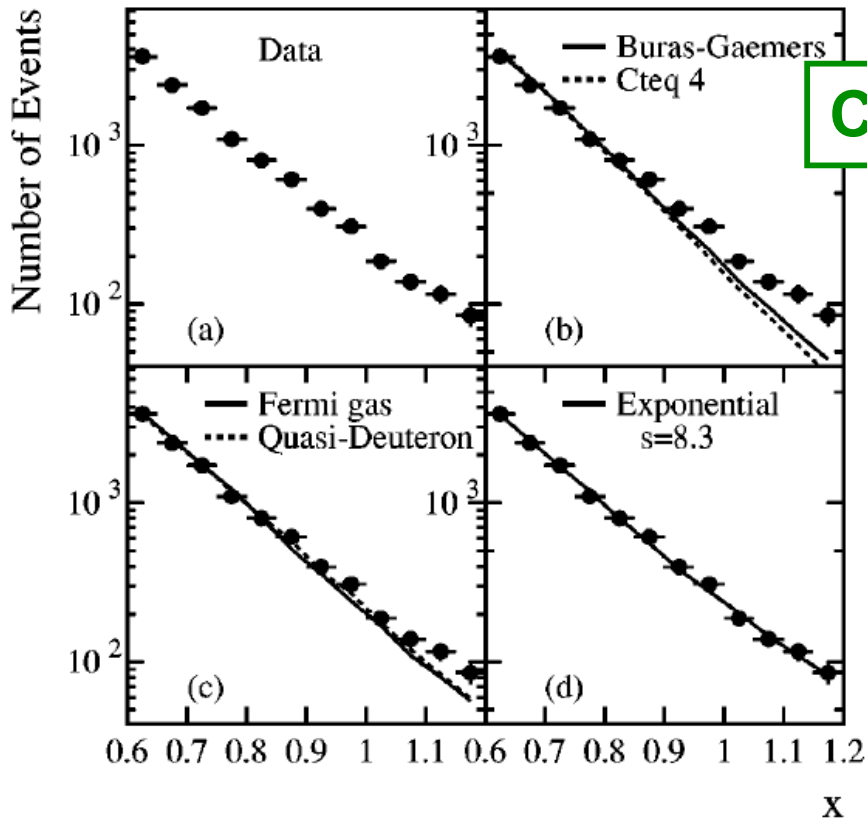
E02-019 carbon

SLAC deuterium  
[times SLAC C/D ratio]

BCDMS carbon

x = projection of CCFR  
falloff, 0.75-1.05





CCFR

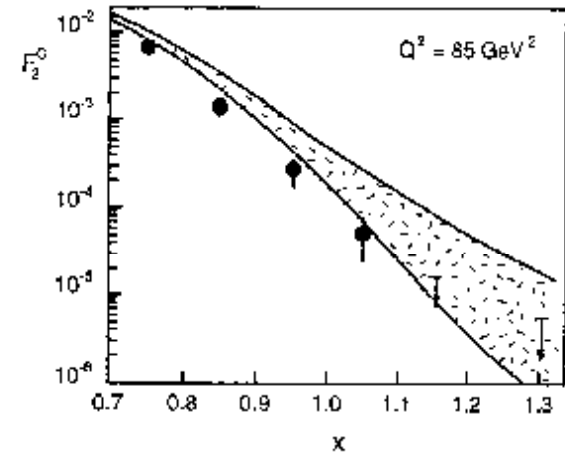
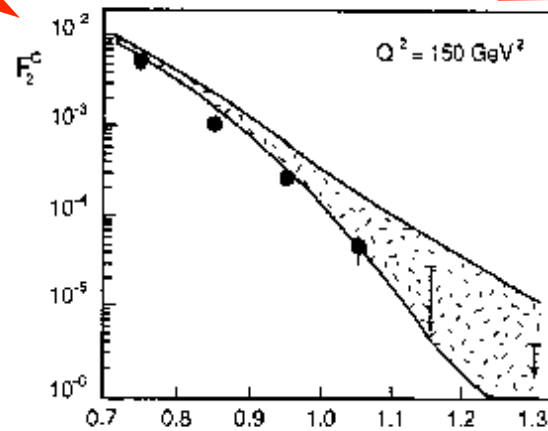
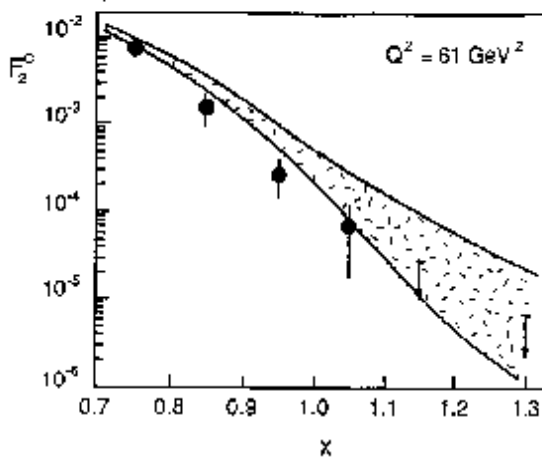
Bottom left fig is CTEQ style PDF convoluted with Fermi gas model: only 20-30% below the high-x data

Low  $Q^2$  data at large x suggest that PDFs underestimate  $F_2$  by similar amount

Idea that CCFR data imply very large SRC does not appear to be justified

CCFR, BCDMS may not go to large enough x to interpret slopes in terms of SRCs or more exotic short-range structure

BCDMS



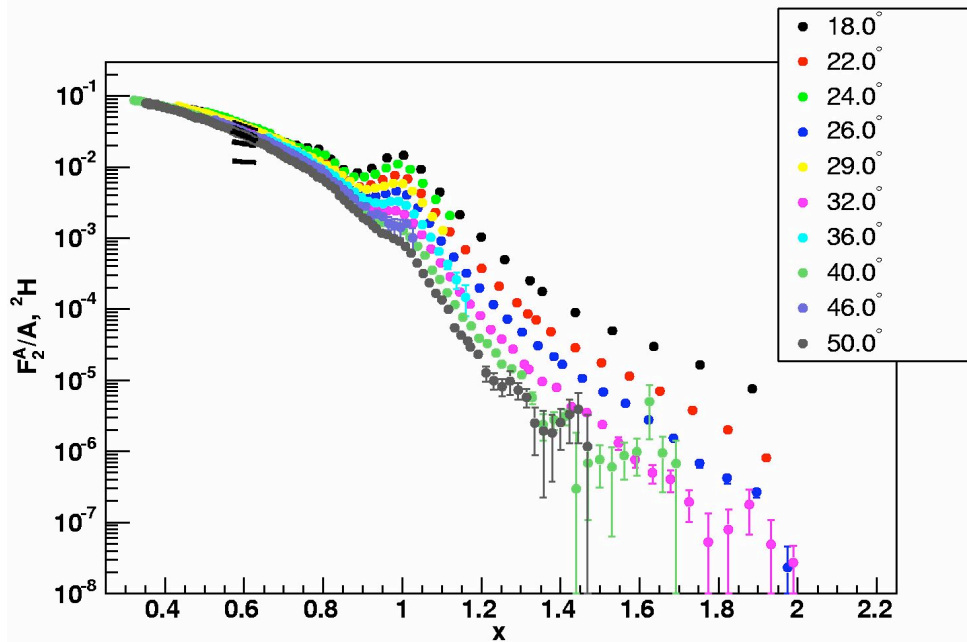
# Future

- Apparent consistency of 6 GeV measurements and BCDMS support idea that 12 GeV measurement can constrain superfast quarks
  - Comparison of QCD evolution to our fitted  $Q^2$  dependence will provide more quantitative measure of scaling violations
- $(m/M)E \otimes (h)IC$  limited by cross section
  - For  $s=1000$ ,  $L \approx 10^{34}$ , statistics running out for  $x \approx 0.85$
  - Might be possible to reach interesting  $x$  range
    - *Need factor of 10, 100, 1000 to reach  $x \approx 1.0, 1.15, 1.30$*
    - *Need to evaluate statistics for lower  $s$* 
      - Can one run below the nominal minimum with reduced luminosity?
    - *Not clear just how high in  $x$  required to isolate short-range structure that we're interested in*

Fin



# Scaling of the nuclear structure functions



←  $F_2(x, Q^2)$  consistent with QCD evolution in  $Q^2$  for low  $x$  values ( $x < 0.5$ )

Huge scaling violations at large  $x$  (especially for  $x > 1$ )

$F_2(\xi, Q^2)$  consistent with QCD evolution in  $Q^2$  to much larger  $\xi$  values

Scaling violations are mostly the “target-mass” corrections  
(plus clear contribution from the QE peak)

→ Nearly independent of  $A$

