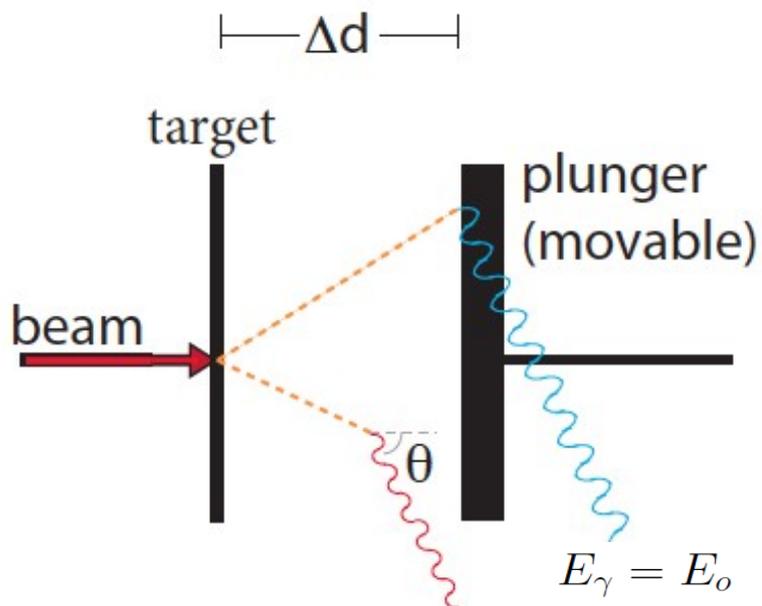


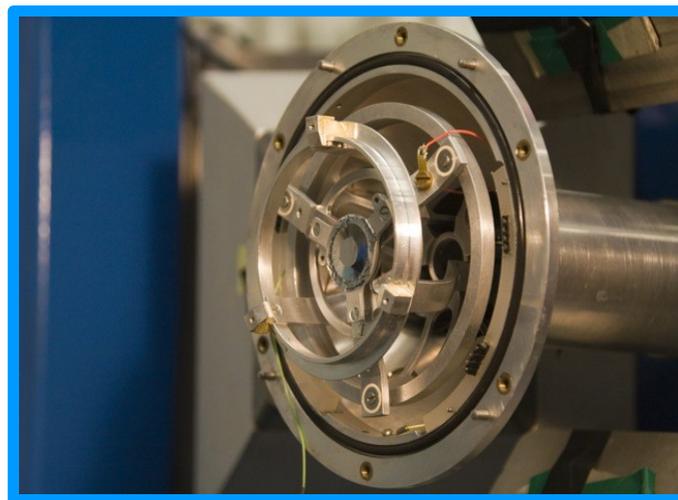
Overview Lecture 2:

- Inverse Kinematics Lifetimes and g Factors – **g - Plunger**
 - „Troubles” in Inverse Kinematics, and how to use them
 - Proof of principle: Pd Chain
 - Next Projects ...
- The femto-second regime – **Nuclear Resonance Fluorescence**
 - Introduction to Photon-Scattering
 - Example: Investigation of ^{76}Se with Continuous and „Laser” Beams

Recoil Distance Doppler Shift (RDDS) method -> pico-second regime

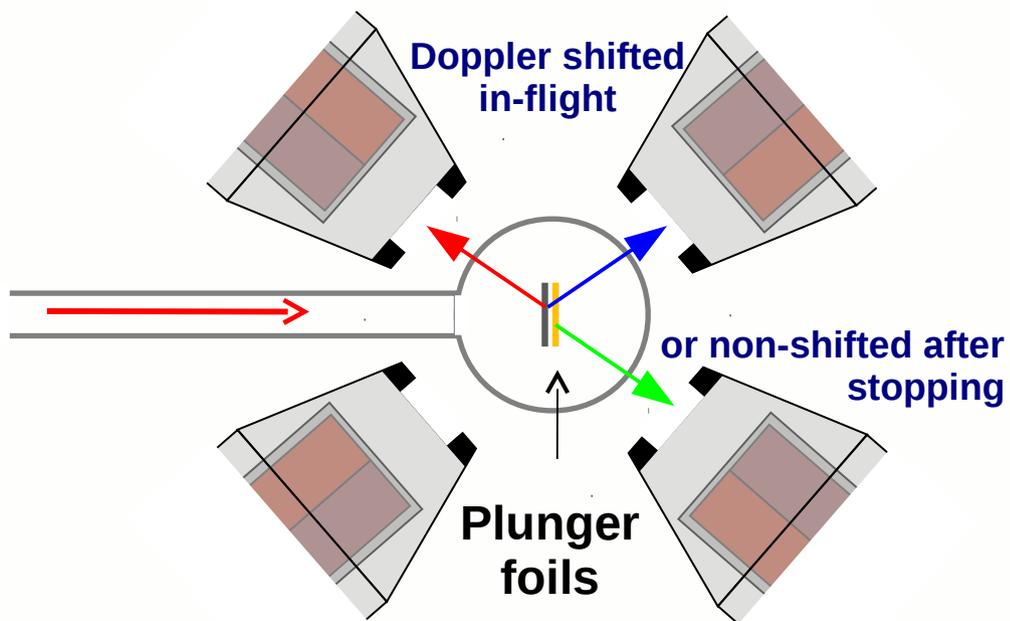
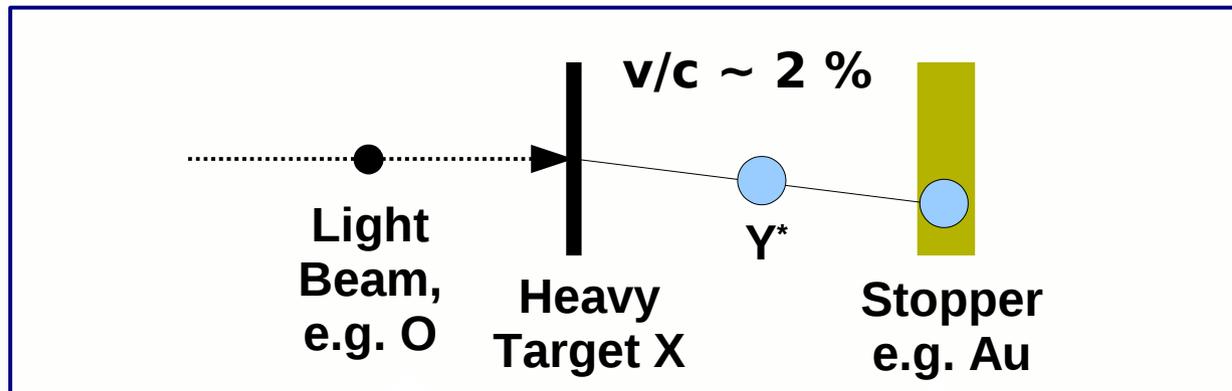


$$E'_\gamma = E_o \left(1 + \frac{v}{c} \cos(\theta)\right)$$



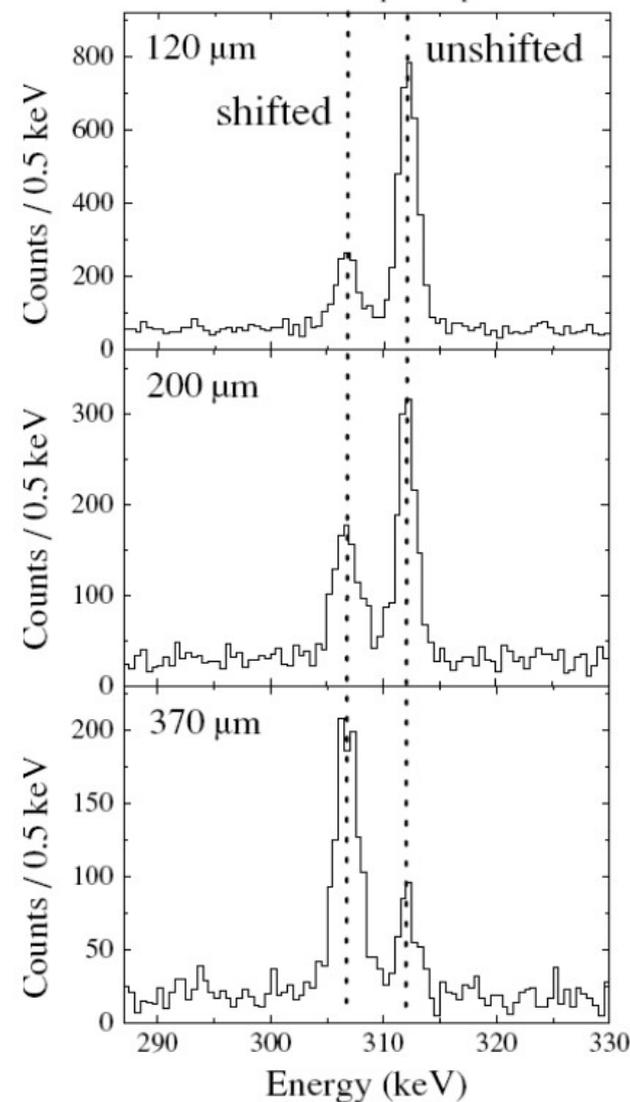
NYPD

Yale Plunger

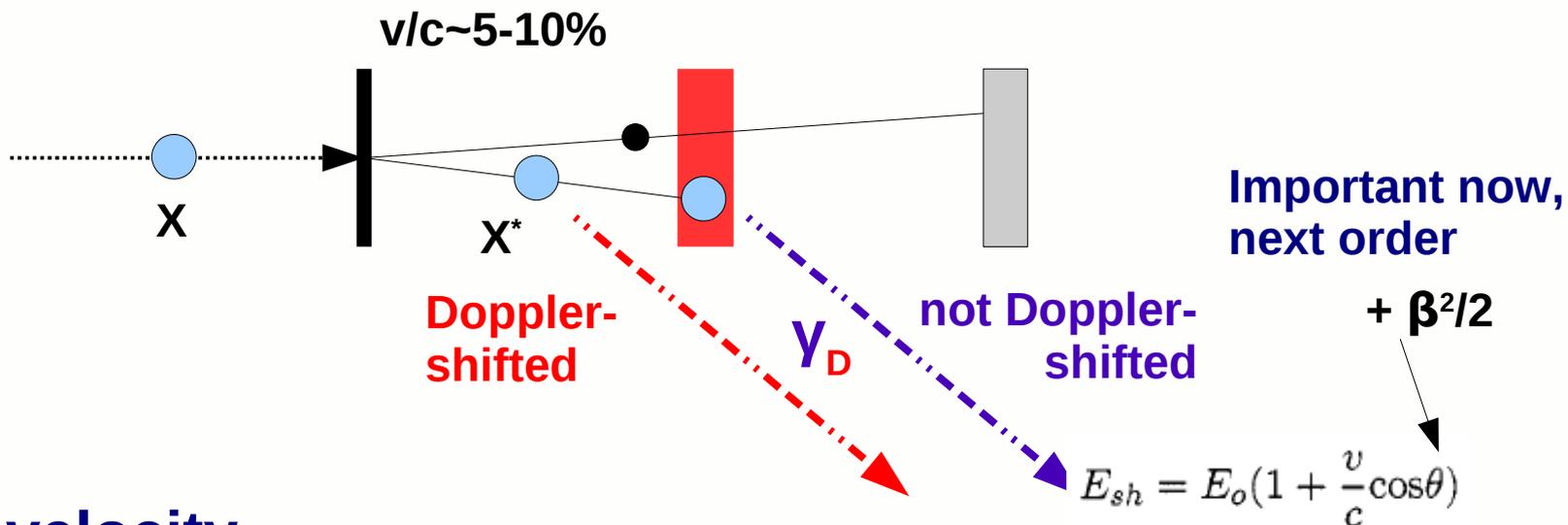


$$E_{sh} = E_0 \left(1 + \frac{v}{c} \cos\theta \right)$$

$^{166}\text{Hf}: 4_1^+ \rightarrow 2_1^+$



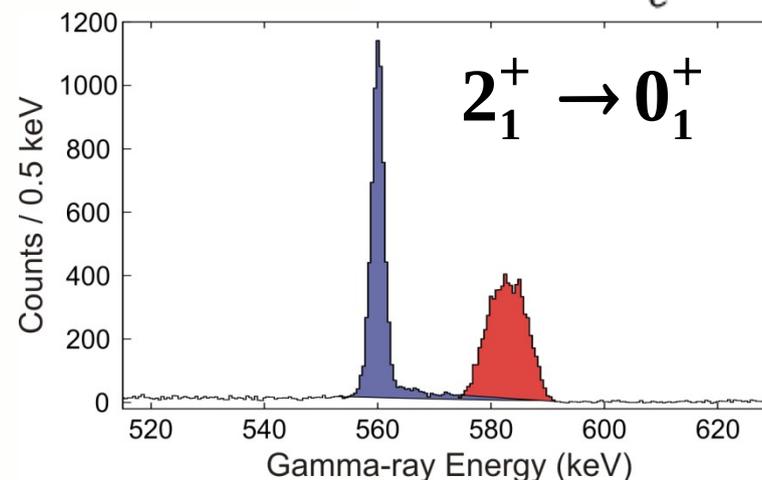
Recoil Distance Method



High recoil velocity

-> large separation of peaks
(and some problems we didn't have before....)

All I show is Coulomb Excitation
-> direct excitation, no feeding !



Intensity correction of γ rays

Attenuation coefficients (solid angle) of the detectors - Q

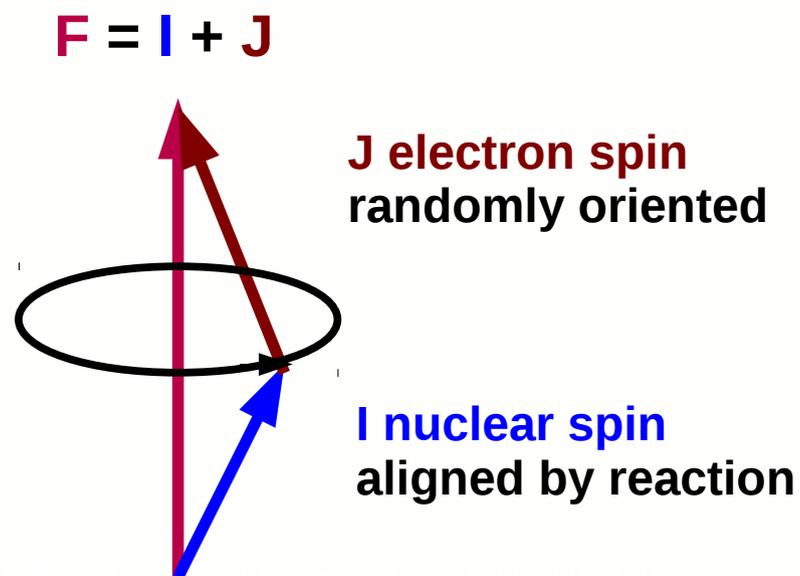
Solid angle of the particle detector – **attenuation of the angular distribution**

Lorentz boost $d\Omega/d\Omega' = (E_\gamma/E_{\gamma_0})^2 = [1 + (E_\gamma - E_{\gamma_0})/E_{\gamma_0}]^2$

Nuclear Deorientation

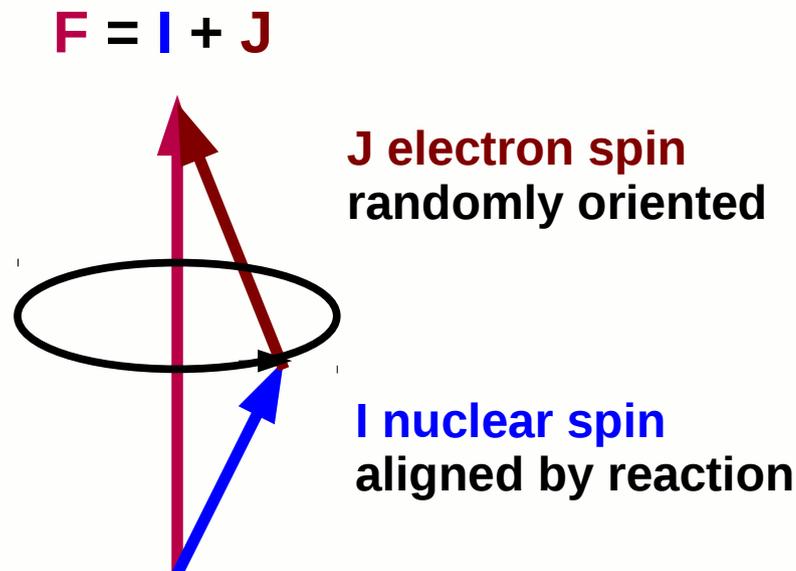
Hyperfine Interaction:

Precession of the **nuclear spin I** and the **electron spin J** about the **total spin F**



Make use of “Recoil Into Vacuum” (RIV)

=> Angular distribution is attenuated!
 By precession of the nuclear spin due to the **hyperfine interaction**
 → deorientation coefficients.



$$W(\theta) = 1 + \sum_{i=2,4} G_i(t) Q_i B_i F_i P_i(\cos \theta)$$

G_i depend on magnetic moment (interacting with electrons)

$$G_k(t) = \alpha_k + (1 - \alpha_k) \cdot \exp[-(g \cdot d) / (v \cdot C_k)] \Rightarrow 3 \text{ parameters: } \alpha_k, g, C_k$$

A. Stuchbery et al., PRC 76, 034307 (2007)

Distance dependent angular distribution:

$$\frac{A_{2/4}^{exp}}{A_{2/4}^{coul} (d = 0)} = G_{2/4}$$

$$W_0(\Theta) = \sum_k A_k P_k(\cos \Theta)$$

$$A_k = \sqrt{2I + 1} \rho_0^k R_k Q_k = B_k R_k Q_k$$

Initial alignment characterized by: $B_k = \sqrt{2I + 1} \rho_0^k$

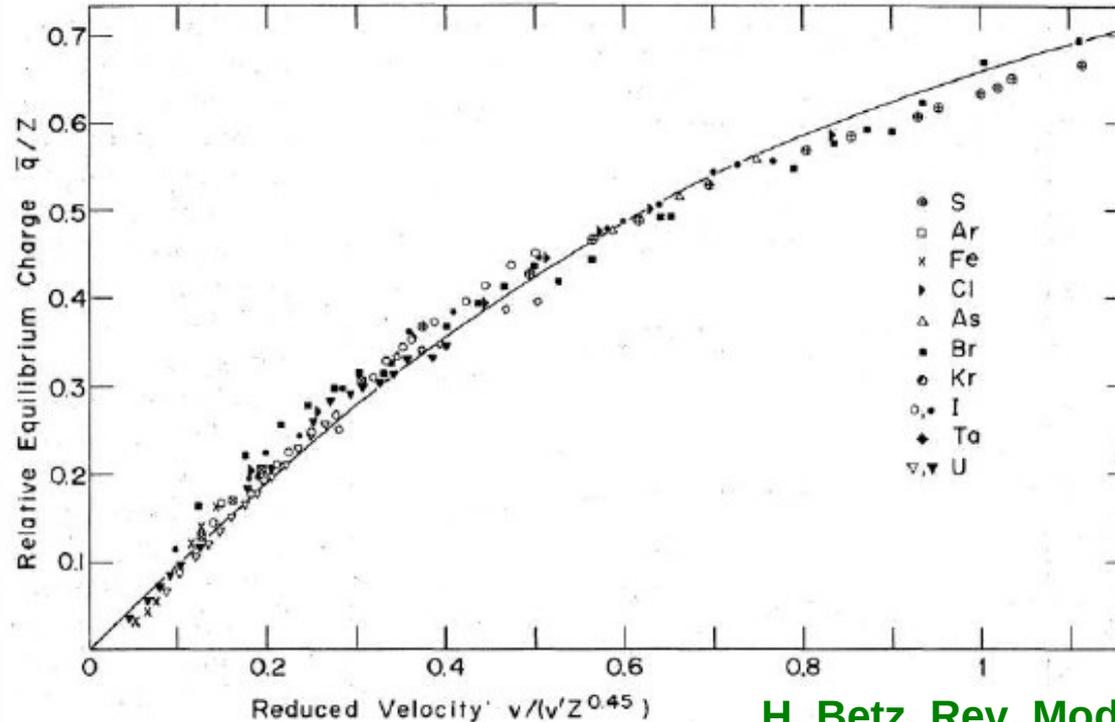
$$\rho_q^k = \sum_{mm'} (-1)^{I+m'} \langle I - m' I m | k q \rangle \rho_{m'm} \quad \text{„statistical tensor”}$$

and $\rho_{m,m'} = a_m a_{m'}^*$ a_m is the m component of the nuclear WF, and m is the component of the spin along the z-axis

$R_k Q_k$ stat. coefficients and attenuation due to solid angle... can be calculated analytically

Since we use Coulomb excitation, which is a well-known E-M process, all the above can be calculated from Coulex Theory.

Charge state of the ion exiting the target.



H. Betz, Rev. Mod. Phys. 44, 465 (1972)

Depends on velocity. Average charge state is reached while passing through the target foil.

(Avg. charge state reached within a fraction of the target at these velocities.)

-> Avg. charge state determines atomic physics (electron-configurations)

$$E_{\text{HF}} = -\vec{\mu}_I \vec{B}_{\text{HF}} \quad \vec{B}_{\text{HF}} \propto \vec{J} \quad \vec{\mu}_I = g_I \vec{I} \mu_N$$

$$E_{\text{HF}} = A \frac{\vec{I} \cdot \vec{J}}{\hbar^2}$$

$$\vec{F} = \vec{I} + \vec{J} \quad \langle \vec{I} \cdot \vec{J} \rangle = \frac{1}{2} \hbar^2 [F(F+1) - I(I+1) - J(J+1)]$$

Typical values: HF – splittings $10^{-6} - 10^{-7}$ eV ; $B_{\text{HF}} \sim 2\text{-}3$ kT

We don't quite know the atomic physics (values of I).

Since the nuclear ensemble is deorienting with time, we need a factor (function) to take this into account:

$$W(\Theta, t) = \sum_k G_k(t) A_k P_k(\cos \Theta)$$

If there is no stopper (that is „normal” Recoil Into Vacuum – RIV):

$$W_p(\Theta) = \langle W(\Theta, t) \rangle = \frac{1}{\tau} \int_0^{\infty} e^{-t/\tau} W(\Theta, t) dt = \sum_k A_k G_k(\infty) P_k(\cos(\Theta))$$

$$G_k(\infty) = \langle G_k(t) \rangle = \frac{1}{\tau} \int_0^{\infty} e^{-t/\tau} G_k(t) dt \quad \text{with excited state lifetime } \tau$$

If we would *know* the electron configurations (but we *don't*)

$$G_k(t) = \sum_{F, F'} C_{IJ}^{F, F'}(k) \cos(\omega_{F, F'} t) \quad C_{IJ}^{F, F'}(k) = \frac{(2F + 1)(2F' + 1)}{2J + 1} \begin{pmatrix} F & F' & k \\ I & I & J \end{pmatrix}^2$$

$$\omega_{F, F'} = g \frac{\mu_N}{\hbar} B_{\text{HF}} \frac{F(F + 1) - F'(F' + 1)}{2J} \quad \text{(for each electron configuration)}$$

We need a more empirical approach:

$$G_k(t) = \sum_i q(J_i) \sum_{F, F'} C_{IJ}^{F, F'}(k) \cos(\omega_{FF'} t)$$

$q(J)$ is a distribution of electron configurations.

Let us assume that electronic configurations (states) are much *longer-lived* than the excited nuclear state -> **Static Limit !**

If the electronic states have a broad distribution, then the Larmor frequencies of the precessions are also broadly distributed.

-> Broad distribution of Larmor frequencies with some Lorentzian distribution width Γ_k , which depends on the nuclear magnetic moment.

Broad distribution leads to exponential behavior of G_k , and the initial orientation will never *completely* be destroyed -> „hard-core” parameter α_k

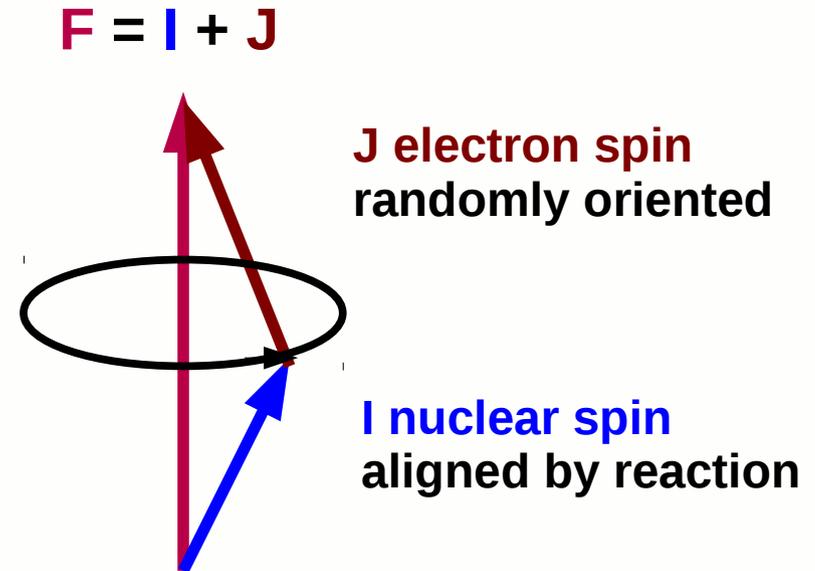
$$G_k(t) = \alpha_k + (1 - \alpha_k) \cdot \exp(-\Gamma_k t)$$

$$\alpha_k = \sum_F \frac{(2F + 1)^2}{2J + 1} \begin{pmatrix} F & F' & K \\ I & I & J \end{pmatrix}^2$$

we use as a parameter, since F, J unknown

Make use of “Recoil Into Vacuum” (RIV)

=> Angular distribution is attenuated!
 By precession of the nuclear spin due to the **hyperfine interaction**
 → deorientation coefficients.



$$W(\theta) = 1 + \sum_{i=2,4} \mathbf{G}_i(t) Q_i B_i F_i P_i(\cos \theta)$$

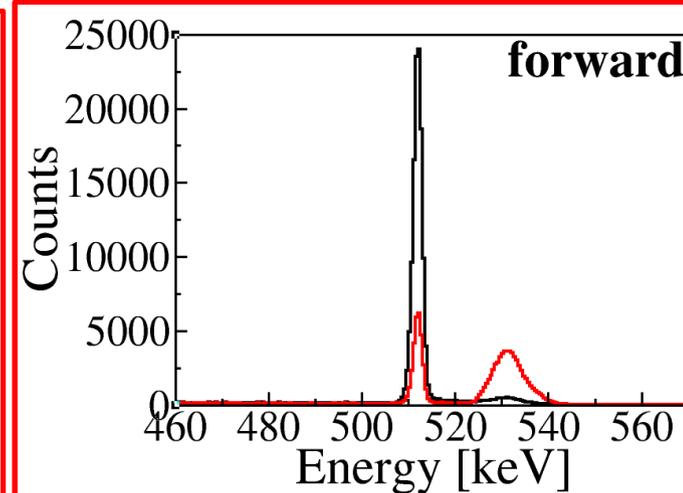
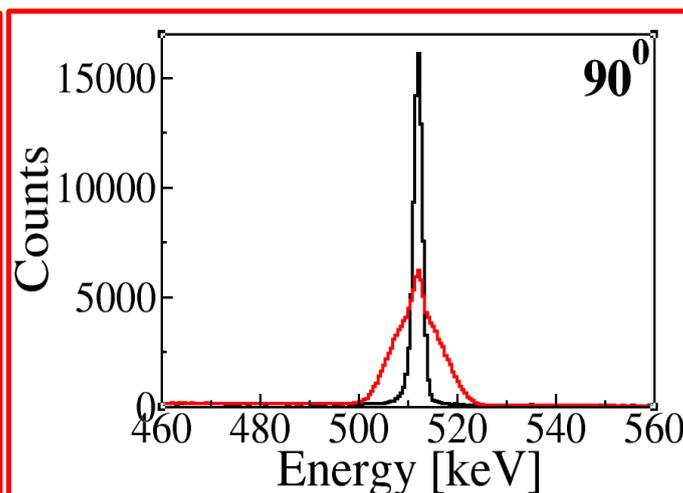
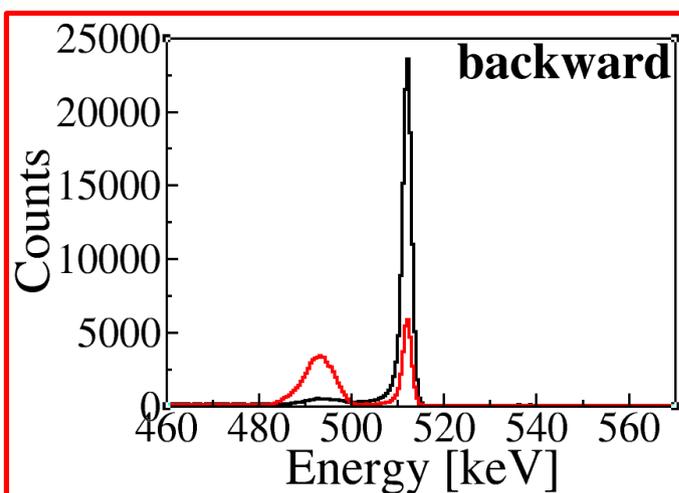
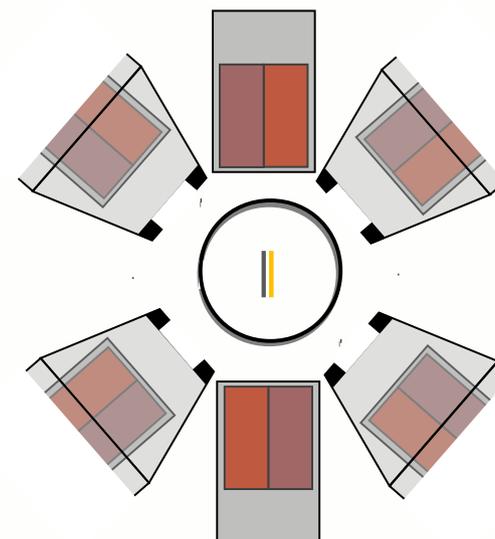
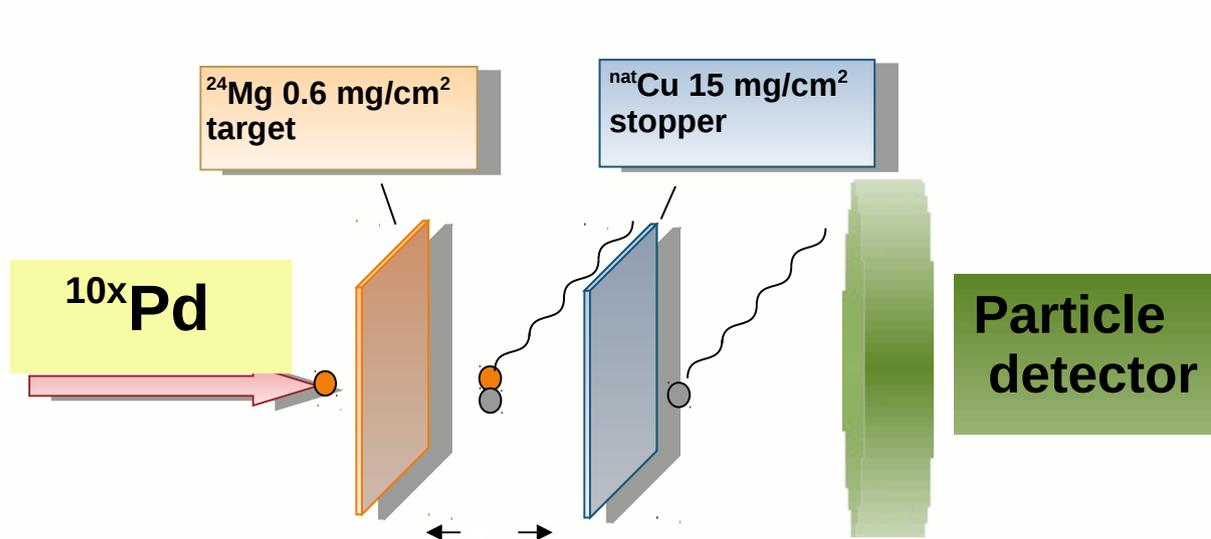
G_i depend on magnetic moment (interacting with electrons)

$$\mathbf{G}_k(t) = \alpha_k + (1 - \alpha_k) \cdot \exp[-(g \cdot d) / (v \cdot C_k)] \Rightarrow 3 \text{ parameters: } \alpha_k, g, C_k$$

A. Stuchbery et al., PRC 76, 034307 (2007)

Distance dependent angular distribution:

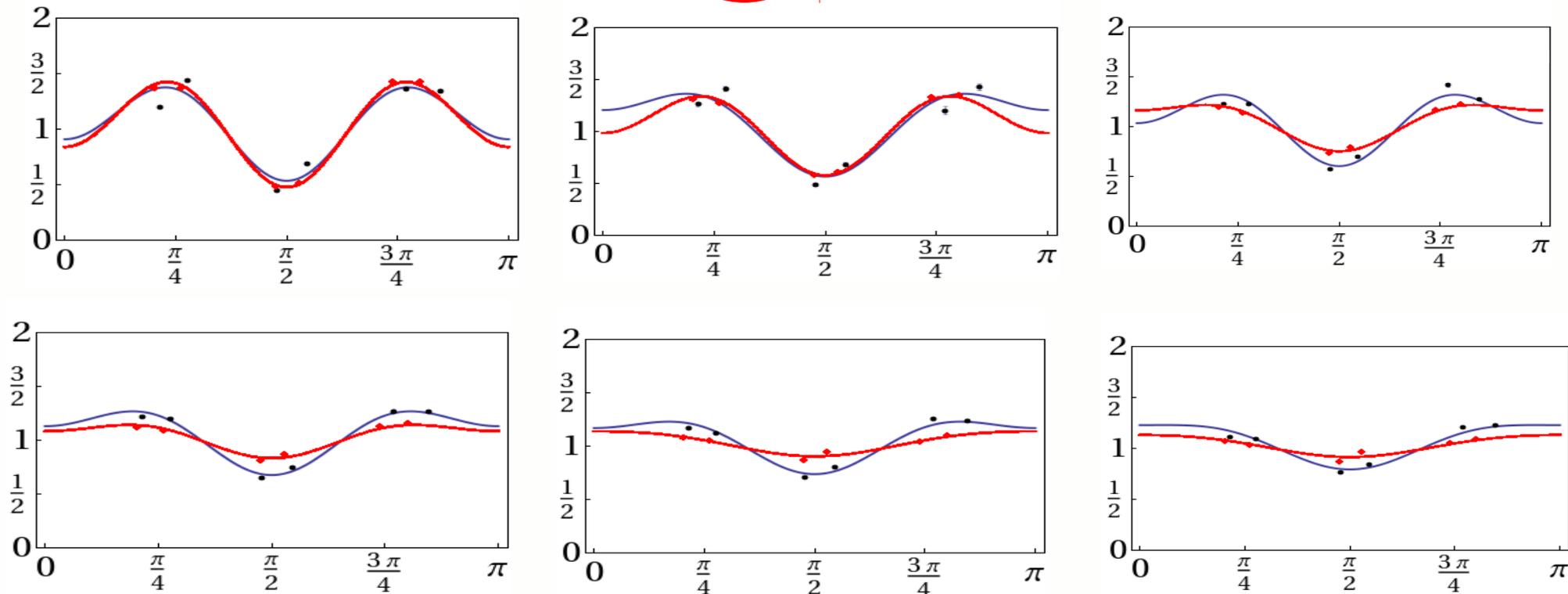
$$\frac{A_{2/4}^{exp}}{A_{2/4}^{coul} (d = 0)} = G_{2/4}$$



High recoil velocity ($v/c \sim 6\%$)

-> large Doppler shift allows precise lifetime measurement

$$W(\theta) = 1 + \sum_{i=2,4} G_i(t) Q_i B_i F_i P_i(\cos \theta)$$



- Doppler-shift
- Stopped

Example of experimental and theoretical calculation of angular distribution for the stopped and the Doppler shift component

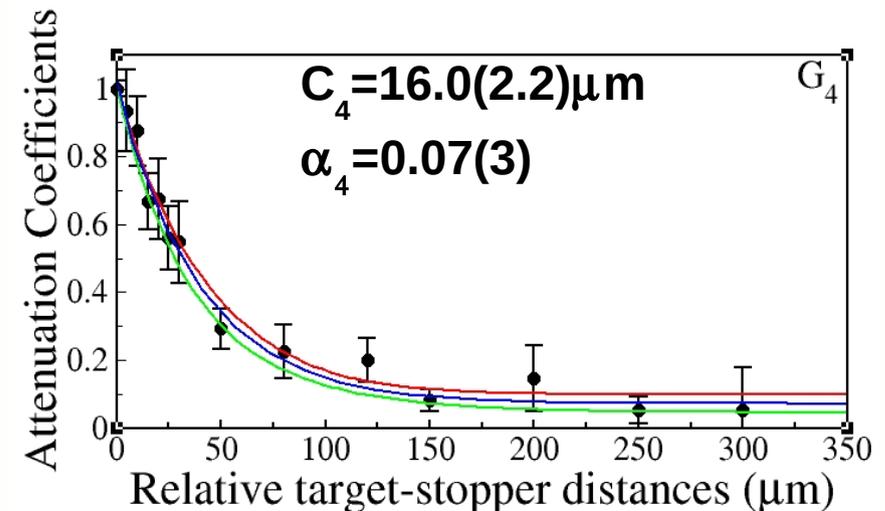
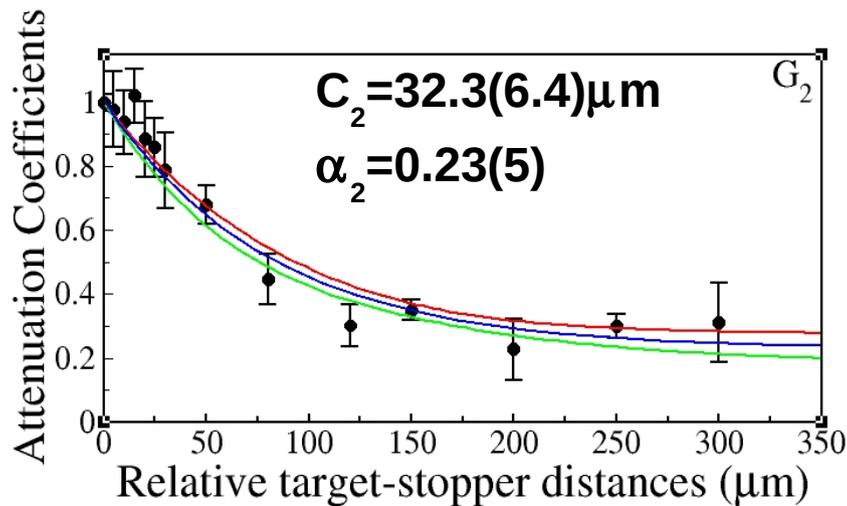
$$G_k(t) = \alpha_k + (1 - \alpha_k) \cdot \exp[-(g \cdot (d - d_0) / (v \cdot C_k))]$$

A. Stuchbery et al., PRC 76, 034307 (2007)

“calibrate” C_k of in one isotope with known g factor (^{106}Pd)

- measure the time dependent attenuation
- “calibrate” an isotopic chain

$$g(2_1^+; ^{106}\text{Pd})^{\text{NNDC}} = +0.398(21)$$



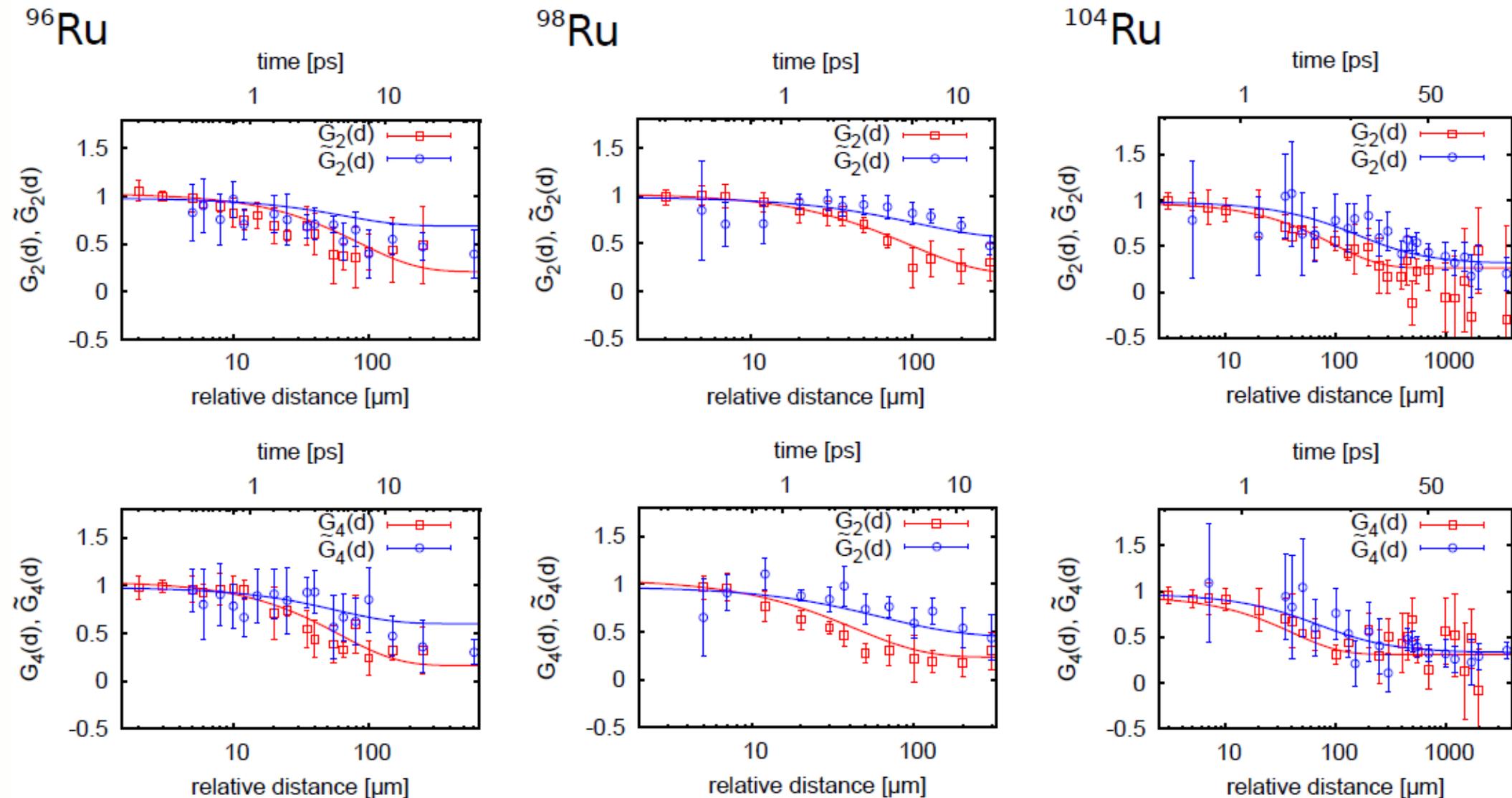
$$W(\Theta, t) = \sum_k G_k(t) A_k P_k(\cos \Theta)$$

stopped peak: $G_k(t) = \alpha_k + (1 - \alpha_k) \cdot \exp(-\Gamma_k t)$

flight peak (decayed somewhere on the way):

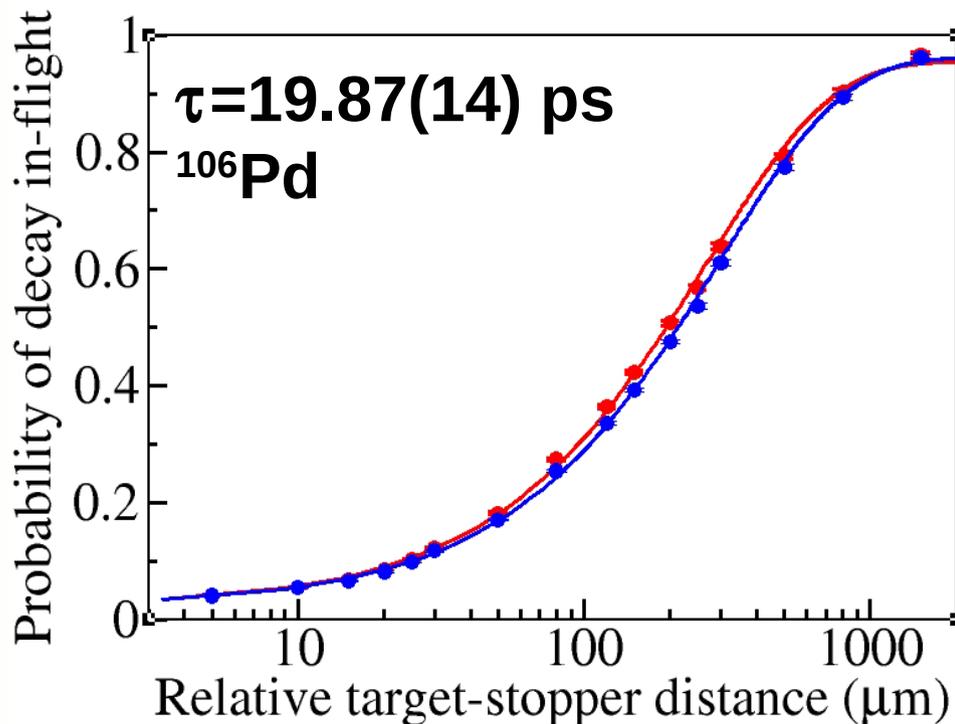
$$G_k^{(\tau)}(d) = \frac{\int_0^d \left(\alpha_k + (1 - \alpha_k) \exp \left(-\Gamma_k \frac{x - d_0}{v} \right) \right) \cdot \exp \left(-\lambda \frac{x - d_0}{v} \right) dx}{\int_0^d \exp \left(-\lambda \frac{x - d_0}{v} \right) dx}$$

$$= \alpha_k + \frac{(1 - \alpha_k) \cdot \exp \left((-\Gamma_k - \lambda) \frac{d - d_0}{v} \right) \cdot \frac{\lambda}{\Gamma_k + \lambda}}{1 - \exp \left(-\lambda \frac{d - d_0}{v} \right)}$$

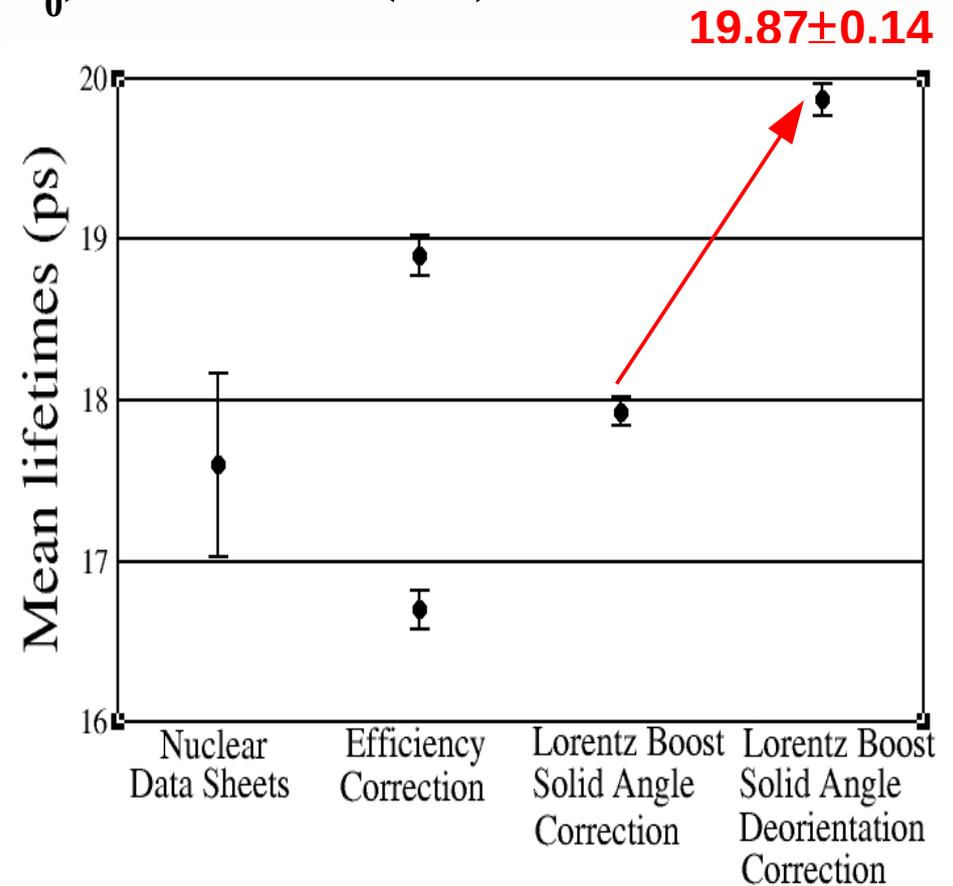


Negligible feeding => simple decay curve: $P(d) = \frac{I_{\gamma}^{(\text{doppler-shift})}}{I_{\gamma}^{(\text{total})}}$

$$P(d) = 1 - \exp[-\lambda \cdot (d - d_0)] ; \quad \lambda = 1 / (v \cdot \tau)$$



- without deorientation correction
- with deorientation correction



(The method **does not give the sign** of the g factor !)

		<i>Reference</i>	
Adopted value¹	+0.46(4)	+0.398(21)	+0.36(3)
g(2₁⁺)	¹⁰⁴Pd	¹⁰⁶Pd	¹⁰⁸Pd
This work	 0.52(10) 	0.40(2)	 0.32(5)
IBM-2²	0.42	0.392	0.366
Shell-Model		0.5	

¹Evaluated Nuclear Structure Data File

²Kim, Gelberg, Mizusaki, Otsuka, von Brentano, Nucl. Phys. A 604, 163 (1996)

³G. Gurdal et al., Phys. Rev. C 82, 064301 (2010); SM-Int: JJ45PN (Hjorth-Jensen), Ni-core, fpg, dg

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Ref ³		0.48(1)(?)	
This w. Rescaled	0.62(10)	0.48(1)	0.38(5)
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(The method **does not give the sign** of the g factor !)

		<i>Reference</i>	
Adopted value ¹ $g(2_1^+)$	+0.46(4) ¹⁰⁴ Pd	+0.398(21) ¹⁰⁶ Pd	+0.36(3) ¹⁰⁸ Pd
This work	 0.52(10) 	0.40(2)	 0.32(5)
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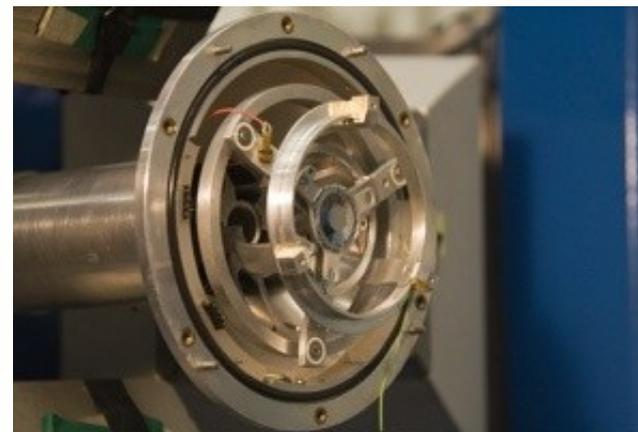
Adopted value $\tau(2_1^+)$	14.9(9) ¹⁰⁴ Pd	17.6(6) ¹⁰⁶ Pd	34.6(18) ¹⁰⁸ Pd
This work	15.64(18)	19.87(14)	39.05(67)

Even worse: This change in τ will affect the g factor as well!

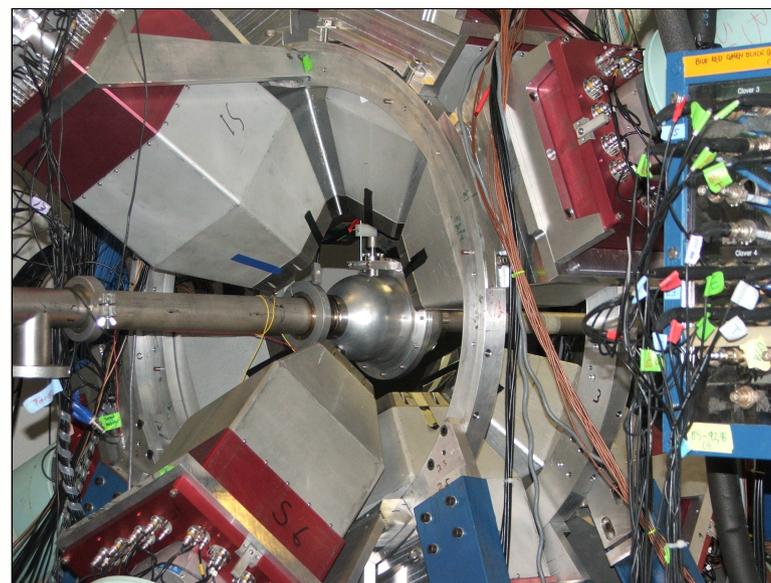
Use of stable beams at the WNSL Tandem accelerator.

Restricted to stable beams, understaffed

-> ceased operation in 2011.



Used the YRAST-Ball array – work to be continued at other facilities with stable AND unstable beams !



104-108Pd: G. Ilie, in preparation & CGS 14
96,98,104Ru: D. Radeck, PRC 85, 014301 (2012)
92,94Zr: Matt Hinton, MPhys U. Surrey (UK)



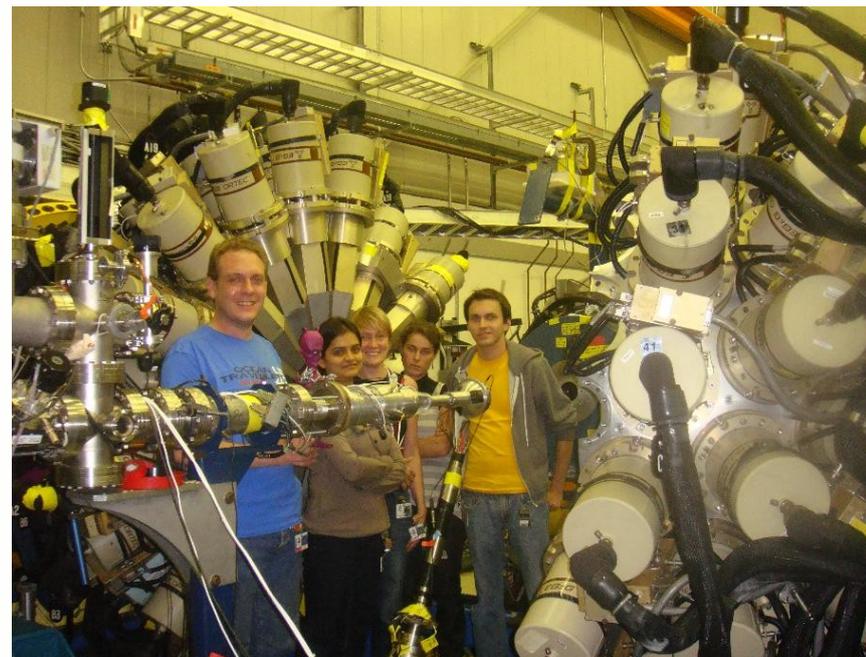
**First g-plunger experiment
device at ATLAS / Gammasphere:**

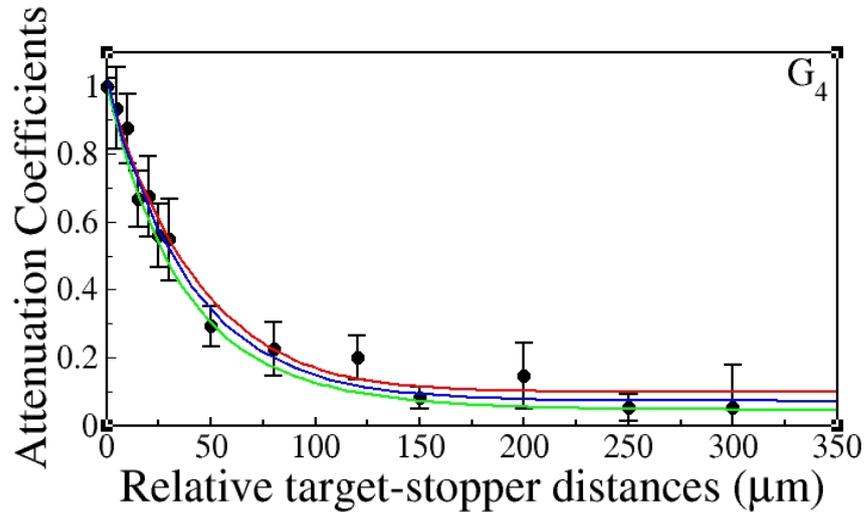
$^{138,142}\text{Ce}$

**October 2011 – analysis with F. Naqvi
Plan: use radioactive CARIBU beams
in future experiments. Later: ReA3
Beams at NSCL.**

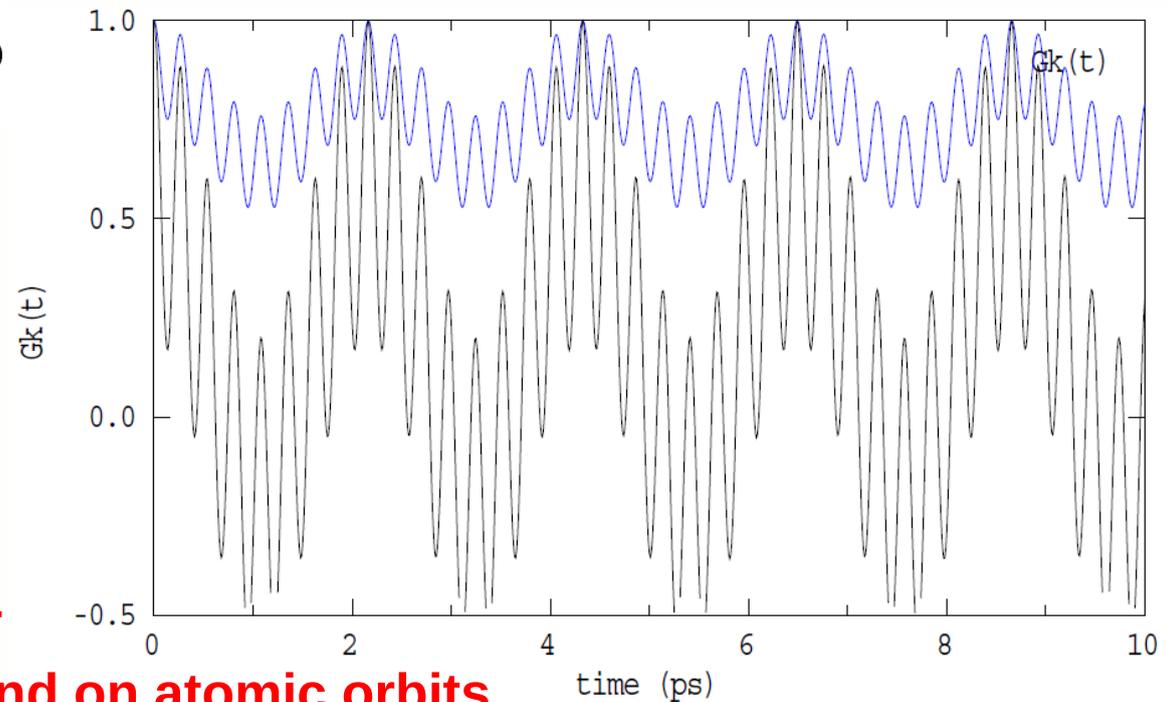
**New plunger to be built for experiments with
Re-accelerated radioactive beams.**

**New approach to test the g-plunger technique with
relativistic beams. Has to overcome one complication!**





$v/c \sim 6\%$, Charge State $\sim 8-12+$
 \rightarrow nice exponential behavior...

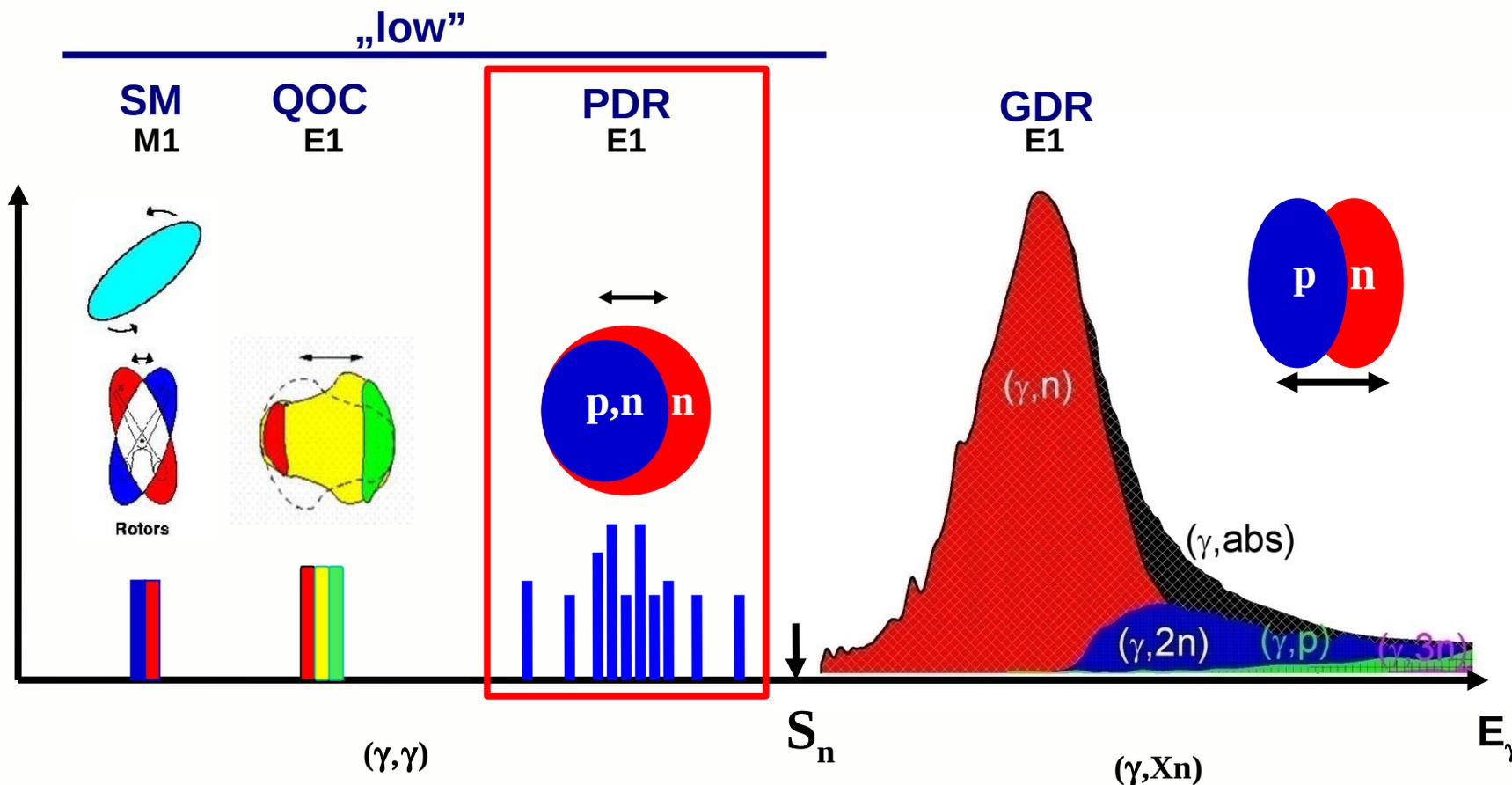


$v/c \sim 40\%$, Charge State $\sim Z - 1+$
 \rightarrow fast oscillations, details depend on atomic orbits

Needs understanding and testing with stable beams first.

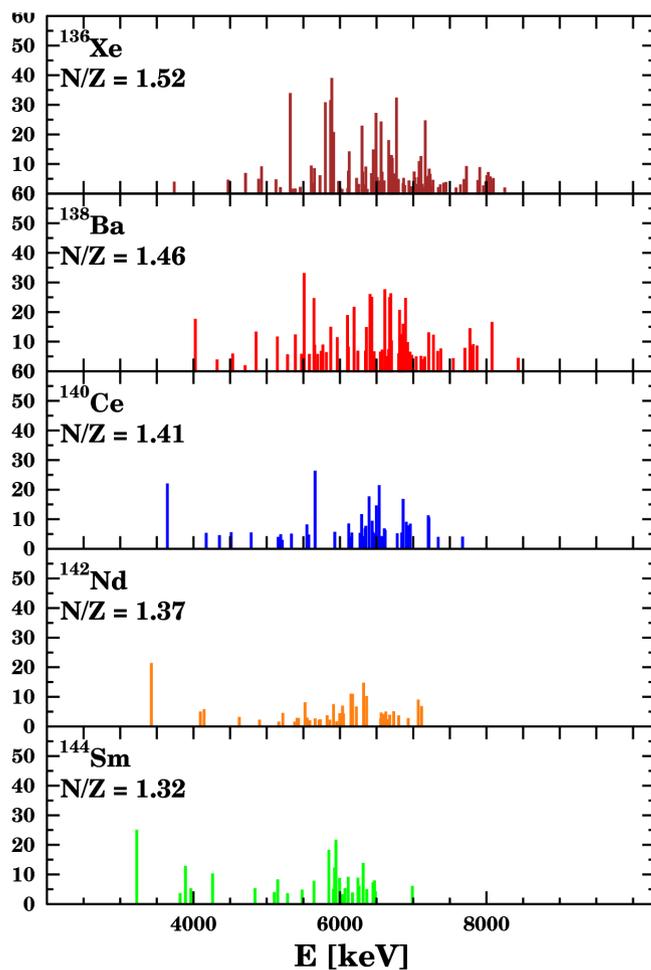
fs - regime

(One way to get there is similar to plunger, but by looking at the stopping process leading to a Doppler-Lineshape – we saw this. Alternative: cross-section measurements!)



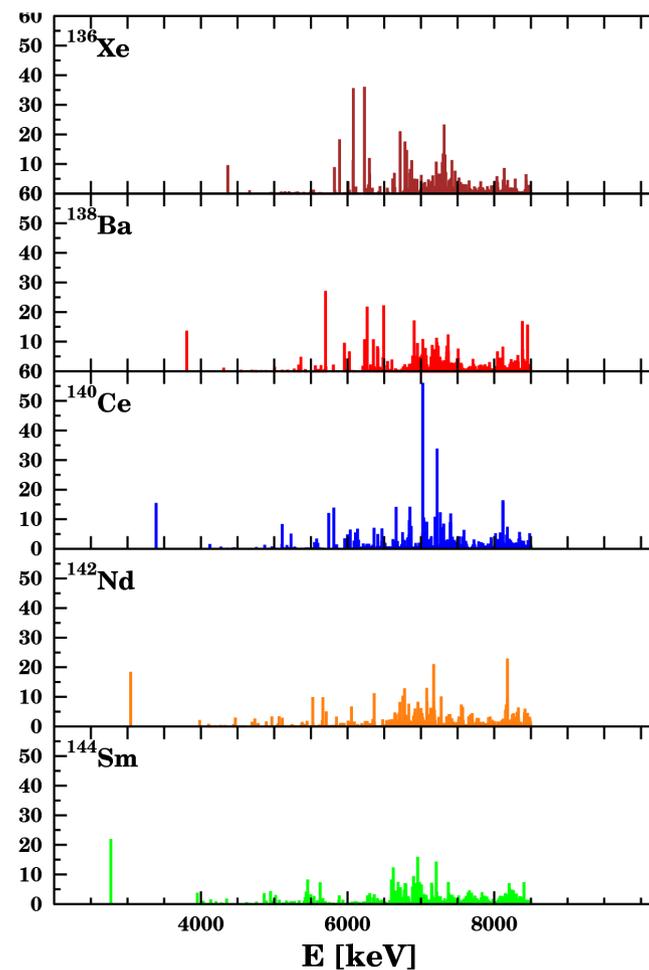
- GDR** • Giant Dipole Resonance: $E_x \sim 10 - 20$ MeV, $B(E1) \sim 5 - 10$ W.u.
- SM** • Orbital “Scissors” mode: $E_x \sim 3$ MeV, $B(M1) \sim 3 \mu_N^2$
- QOC** • Two Phonon Excitation: $E_x \sim 4$ MeV, $B(E1) \sim 10^{-3}$ W.u.
- PDR** • **Pygmy Dipole Resonance ?**

Experiment

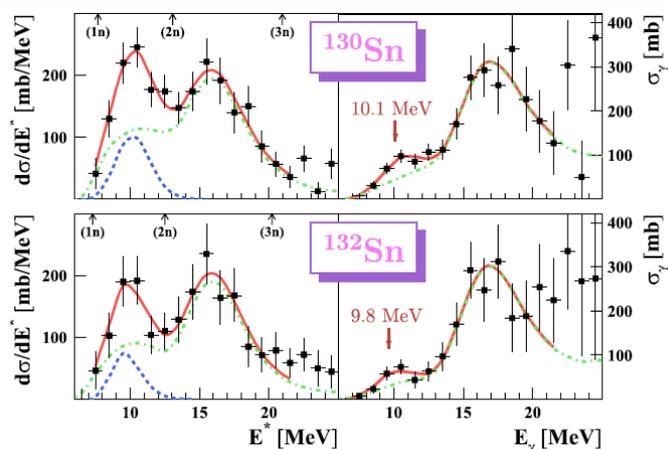


S. Volz et al., Nucl. Phys. **A779** (2006) 1

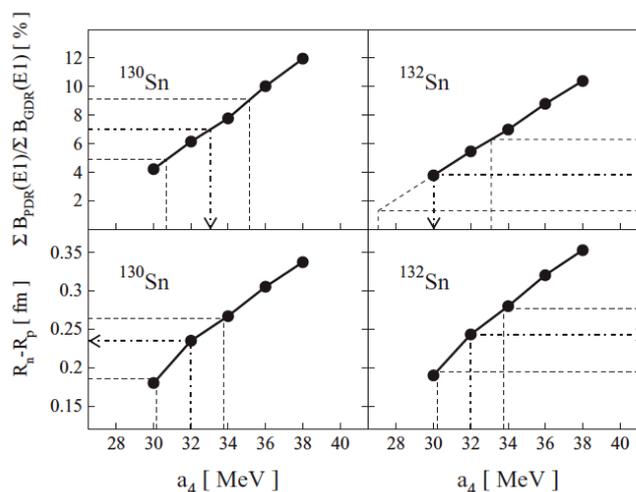
Quasiparticle-Phonon-Model (QPM)



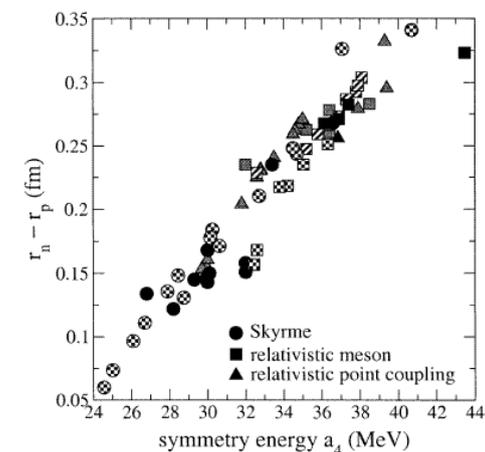
V. Yu. Ponomarev



P. Adrich et al., PRL 95 (2005) 132501



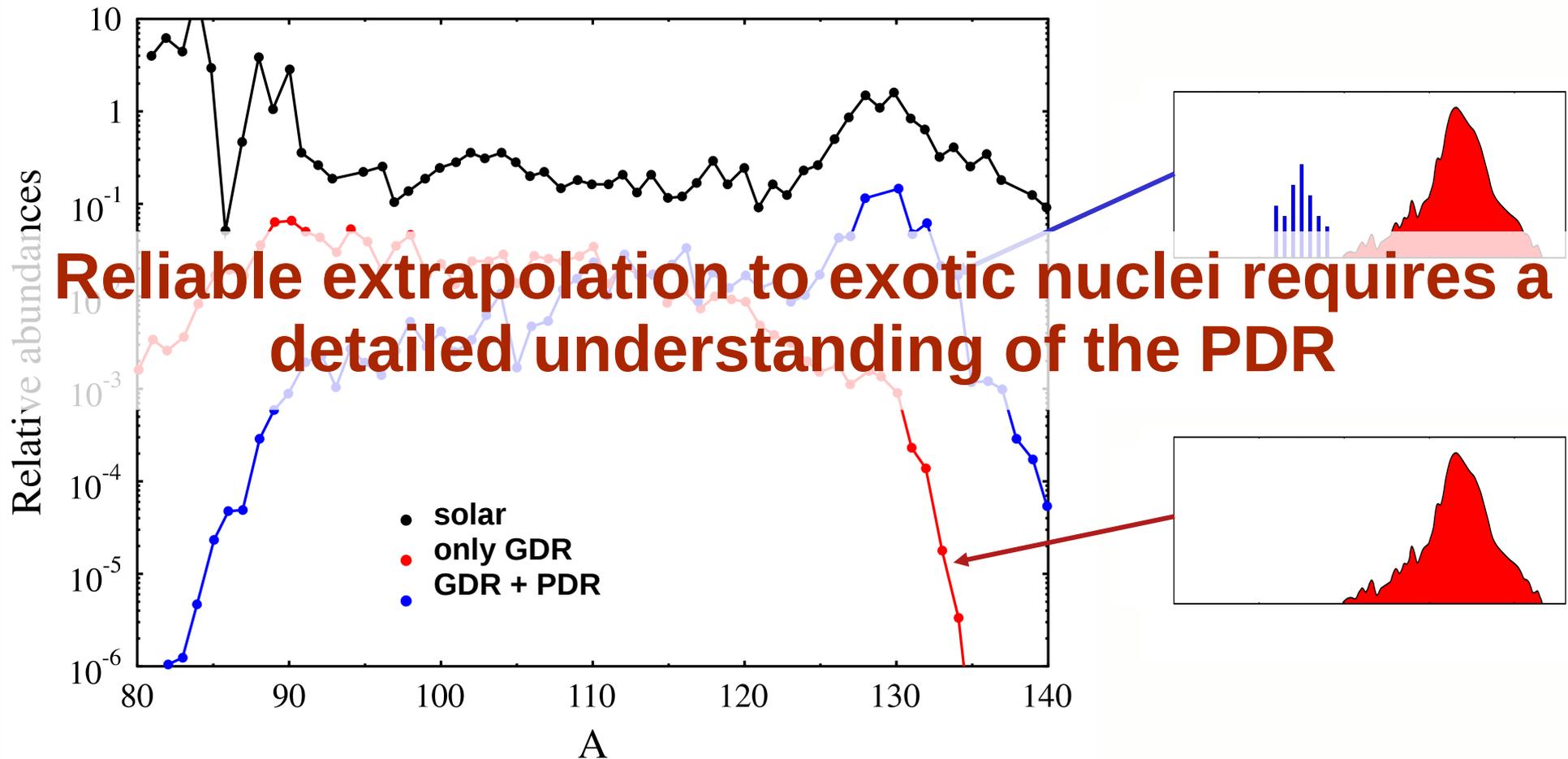
A. Klimkiewicz, Nils Paar et al,
PRC 76 (2007) 051603(R)



R.J.Furnstahl NPA 706(2002)85-110

Clear dependence on neutron skin !

Possible influence of the PDR on the r-process:



S. Goriely, Phys. Lett. B 436 (1998) 10

- **Structural Motivation: Evolution of the PDR toward deformed nuclei !**
- „Side Motivation“:

An odd situation:

Learn about a weakly interacting particle by look at a strongly interacting system.

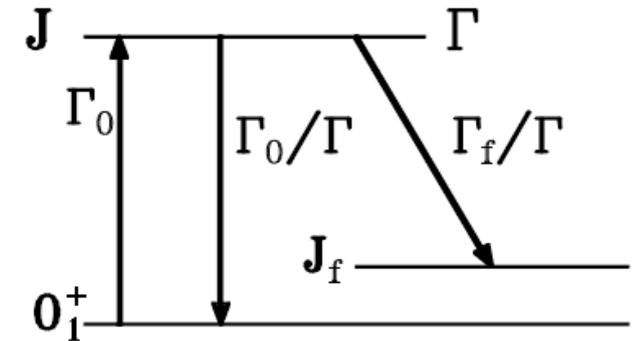
- **Why nuclear structure?**
- **First claim on the observation of $0\nu 2\beta$ decay $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$ has been made (Heidelberg-Moscow)**
- **New experiments just started or are about to start (GERDA / MAJORANA)**
- **Observation of the decay rate is not sufficient to extract masses**
- **Need: Nuclear Matrix Elements !!**
- **Can only be extracted from nuclear theory**
- **=> scrutinize involved theories**

- **Some selected experiments going that way:**
- **Schiffer et al.: ground state wave functions from transfer reactions**
- **WNSL: gamma-spectroscopy on intermediate nuclei**
- **HIGS/TUNL/Darmstadt(GER): dipole response of $0\nu 2\beta$ candidates**
- **UK Lexington: γ -spectroscopy after neutron scattering**
- **ANU (Australia): electron spectroscopy**
- **TRIUMF: in-trap spectroscopy => EC decay branchings**

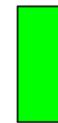
$\Pi\lambda$ - strengths

$\Delta J = 1, 2$

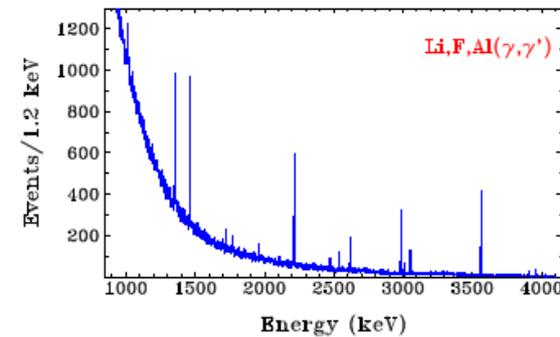
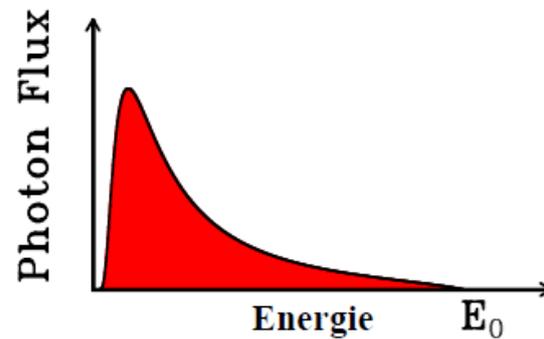
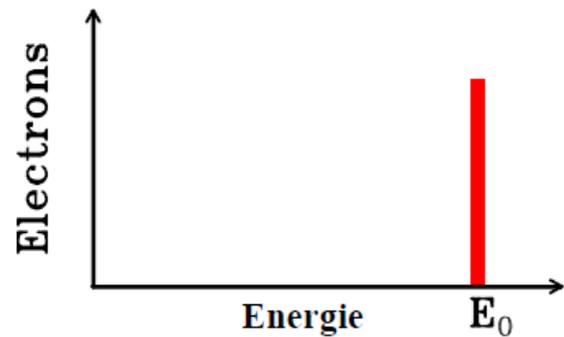
high energy resolution



$e^- \rightarrow$



HPGe



In a nutshell – description of resonance: Breit-Wigner

$$\frac{d^2\sigma_{abs}(E)}{d\Omega dE} = \pi\lambda^2 \cdot \frac{2j+1}{2(2j_0+1)} \cdot \frac{\Gamma_0\Gamma_f}{(E-E_r)^2 + \frac{1}{4}\Gamma^2} \cdot \frac{W(\theta)}{4\pi}$$

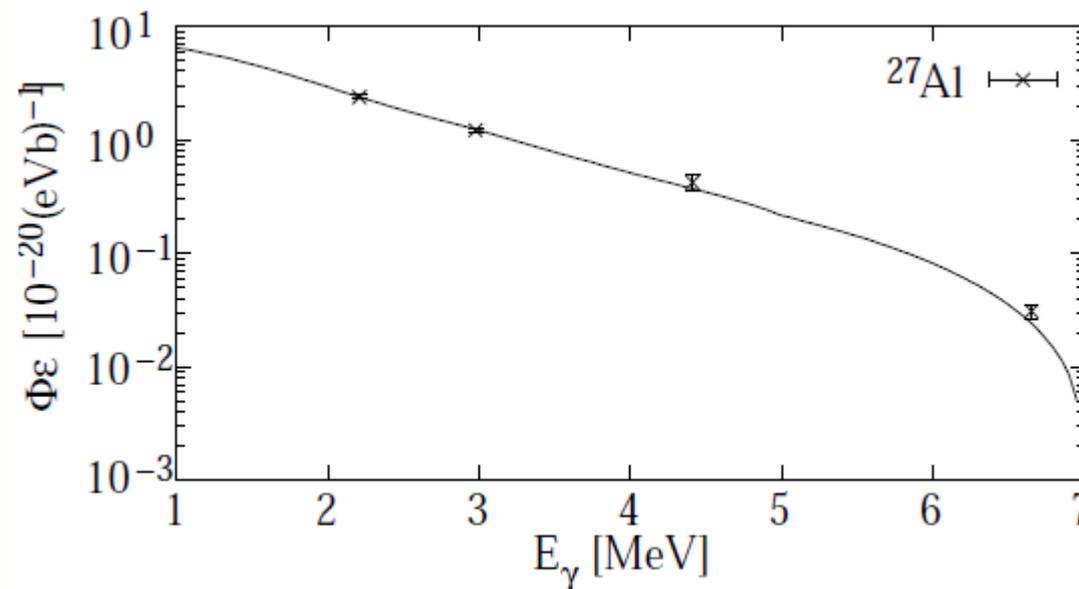
Integrate that over solid angle and the resonance:

$$I_{s,f} = \pi^2\lambda^2 \cdot \frac{2J+1}{2J_0+1} \cdot \frac{\Gamma_0\Gamma_f}{\Gamma}$$

Integrated cross-section from size of the observed peak to „f”inal state.

Measurement of σ -sections always relative to a standard!
 For example, ^{27}Al / ^{11}B have well-known cross-sections.

Measure Al/B states, measure / simulate detector efficiency
 => Photon Flux / Cross-section calibration



Extract:

$$\frac{\Gamma_0^2}{\Gamma} = \frac{2j_0 + 1}{2j + 1} \cdot \left(\frac{E_\gamma}{\pi \hbar c} \right)^2 \cdot I_{s,0}$$

Resonance width:

$$\Gamma = \frac{\Gamma_0^2}{\Gamma} \cdot \left(1 + \sum_{f>0} \frac{\Gamma_f}{\Gamma_0} \right)^2$$

(if branchings known)

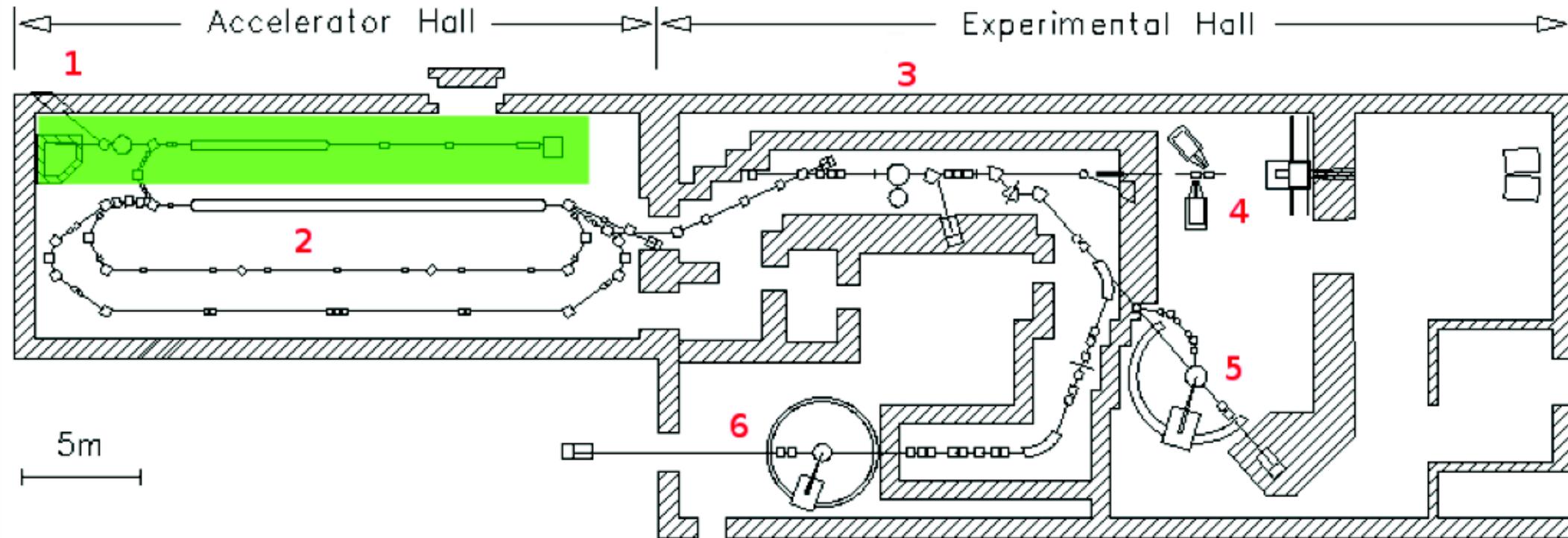
And the relation to lifetimes is:

$$1/\tau = \Gamma = \sum_{f \geq 0} \Gamma_f$$

Typical lifetimes for strongly dipole-excited states: *femto- / attoseconds !*

NRF is a model-independent way to measure lifetimes!

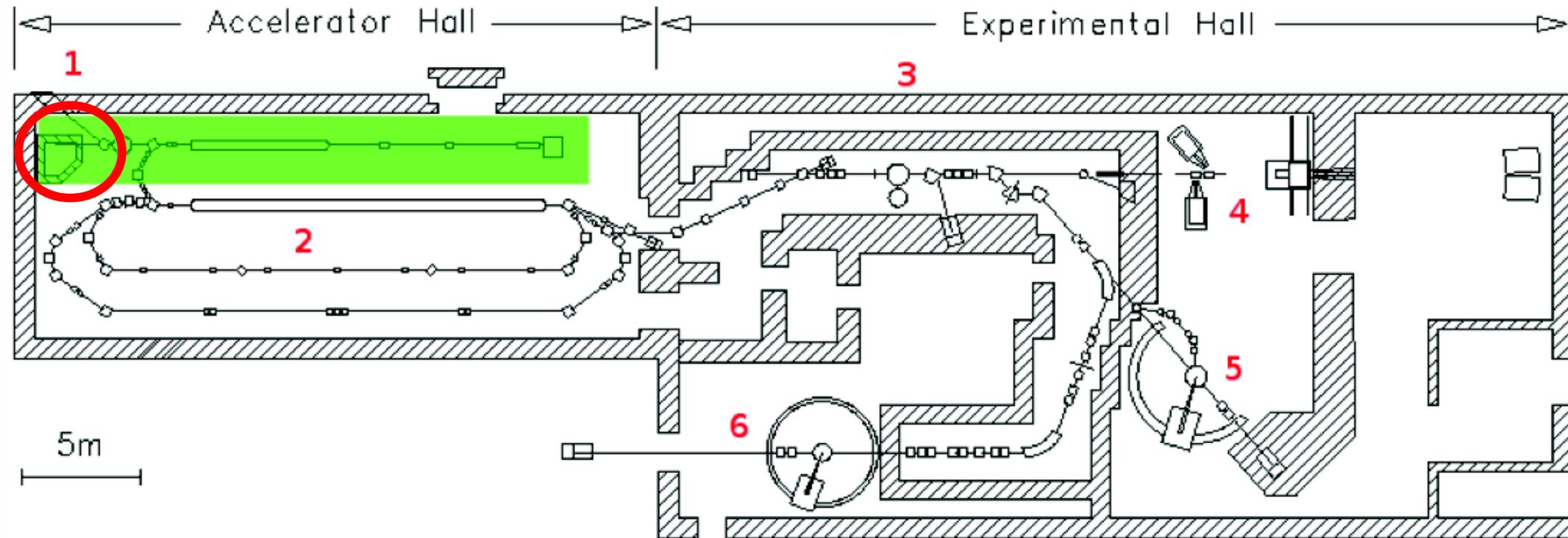
Superconducting Darmstadt LINear ACcelerator



**Continuous Bremsstrahlung beams allow to identify dipole-excited states!
 Parity determination is possible via polarimetry, but difficult.
 (Figures of merit of polarimeters are not favorable, especially at high energies.)**

Target ~ 4 g enriched ^{76}Se

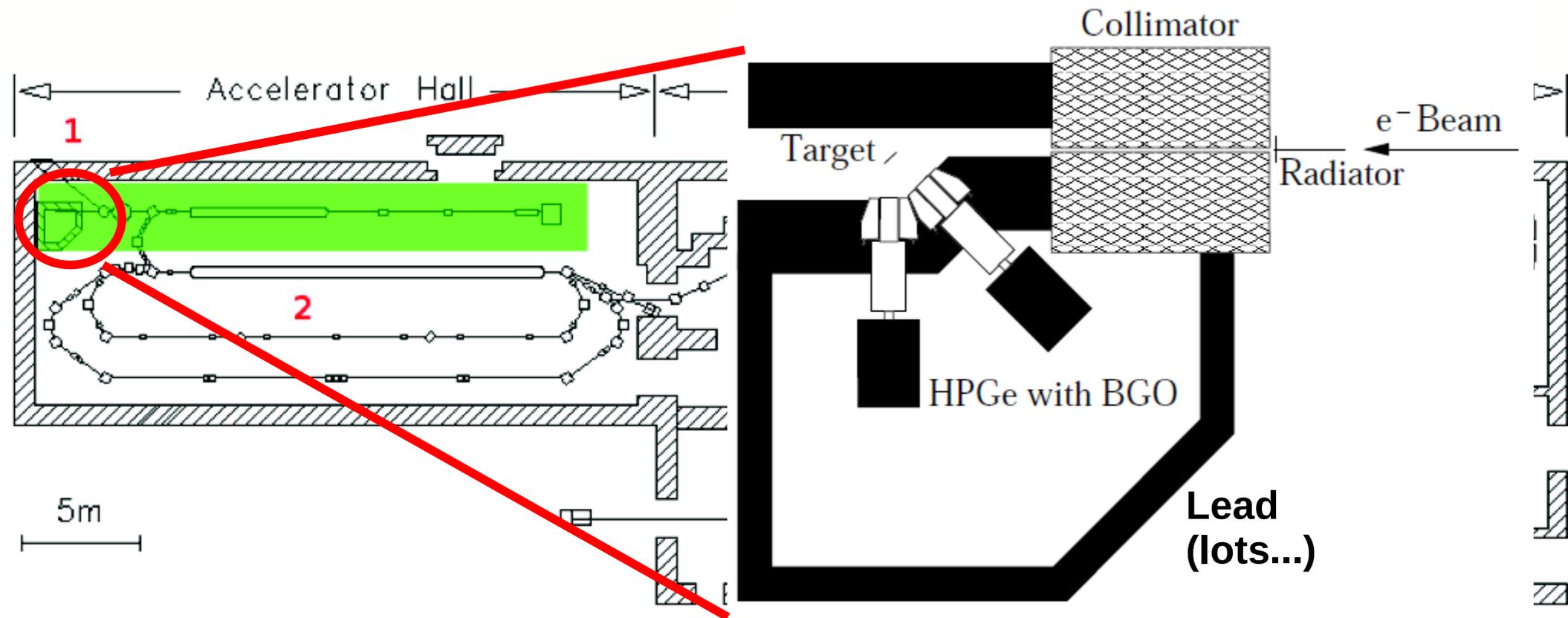
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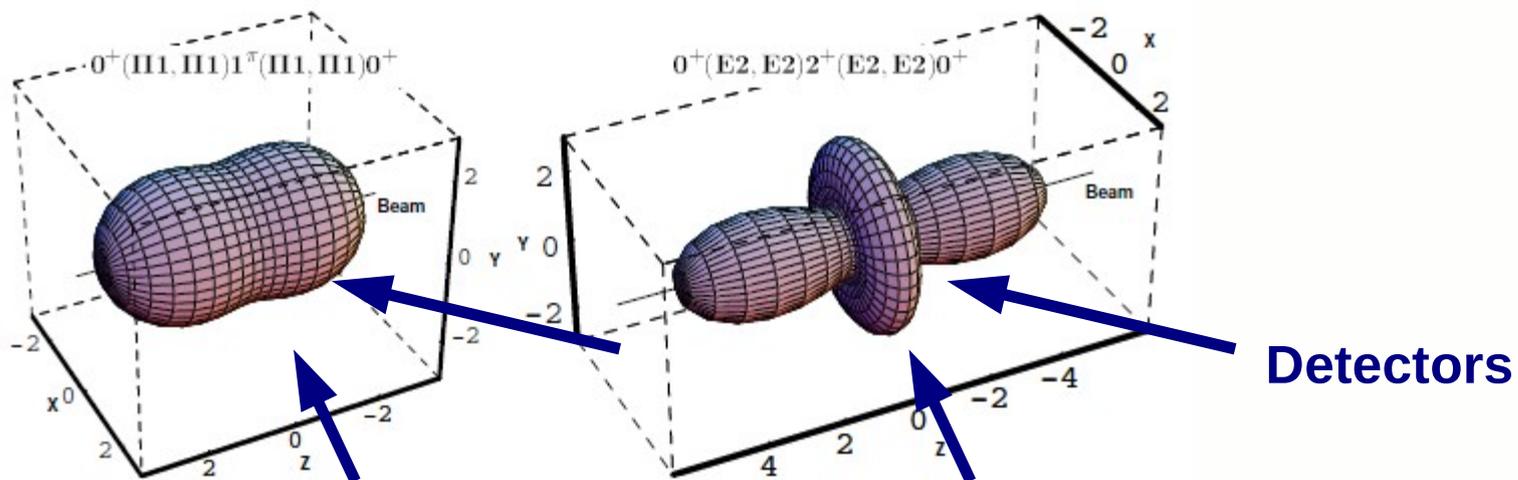
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Superconducting DArmstadt LINear ACcelerator

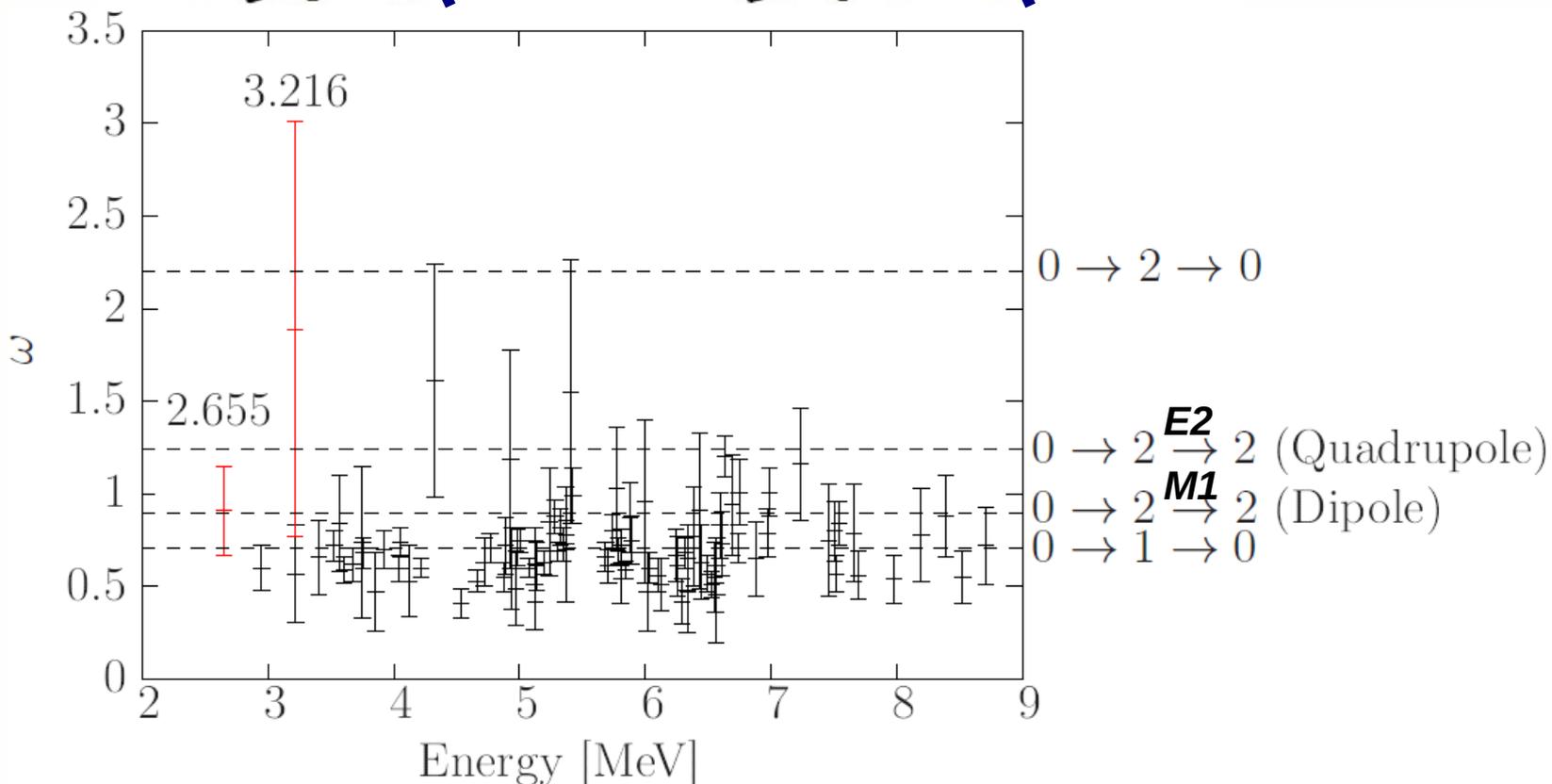


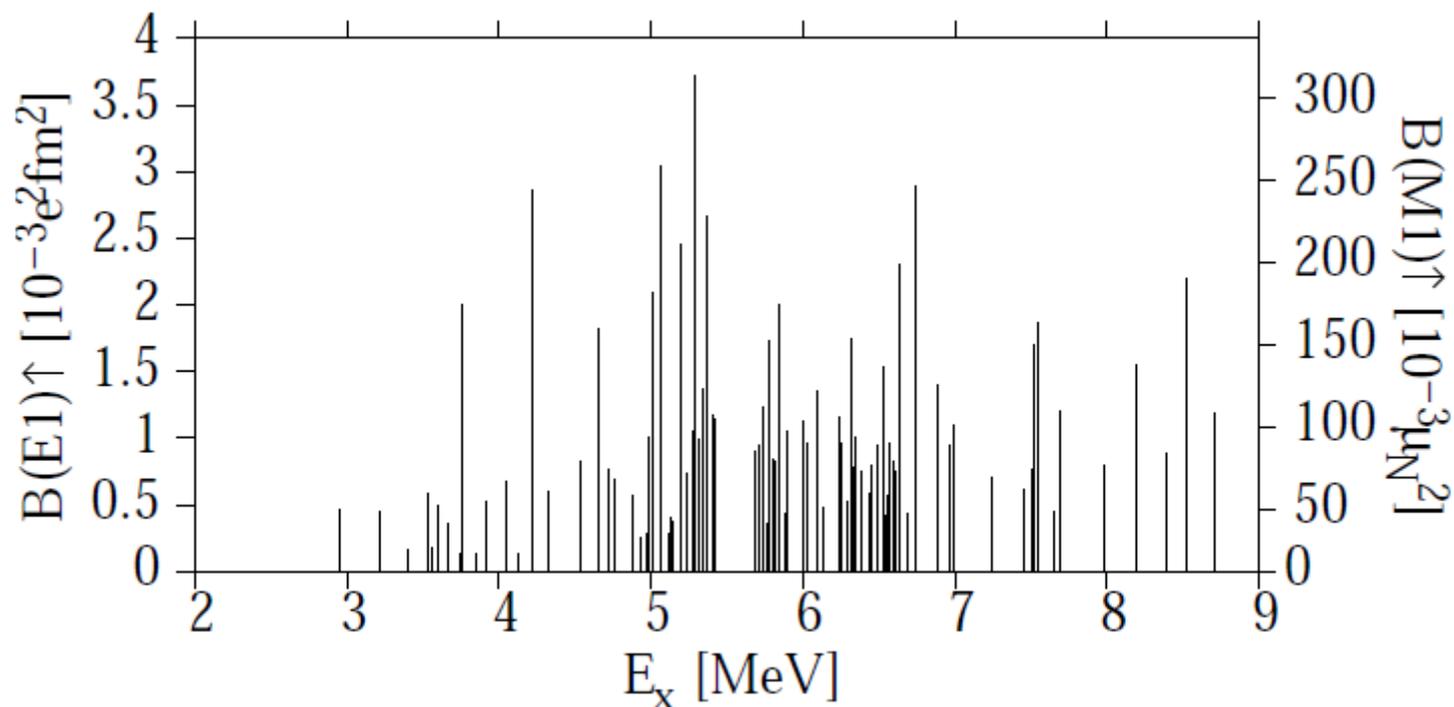
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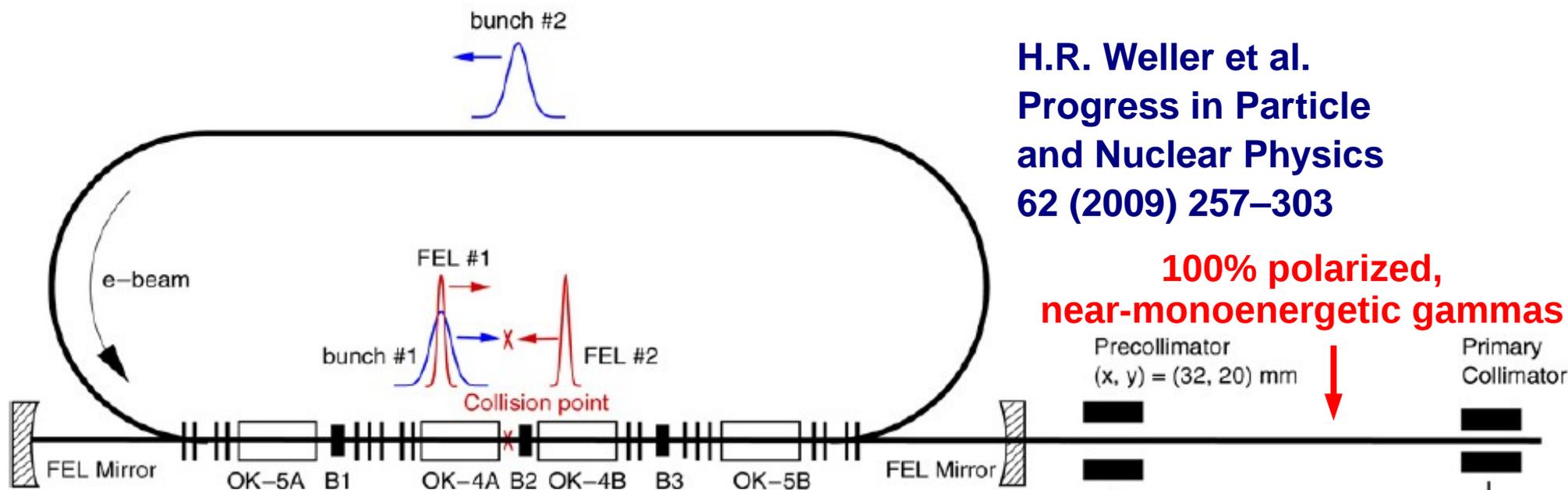
$W(90^\circ) / W(130^\circ)$



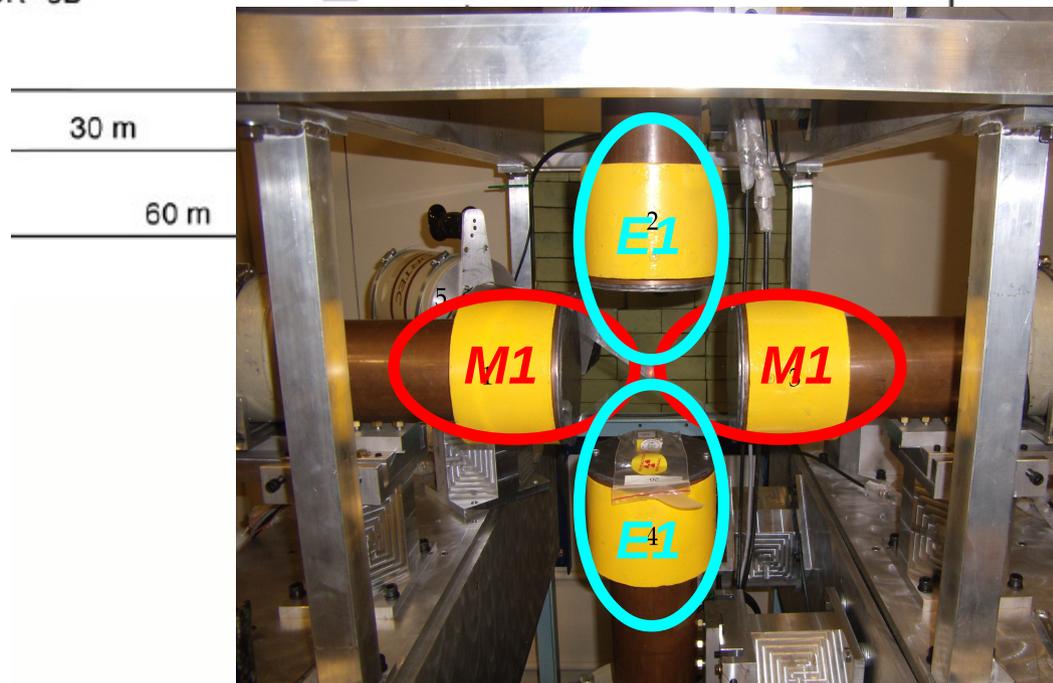
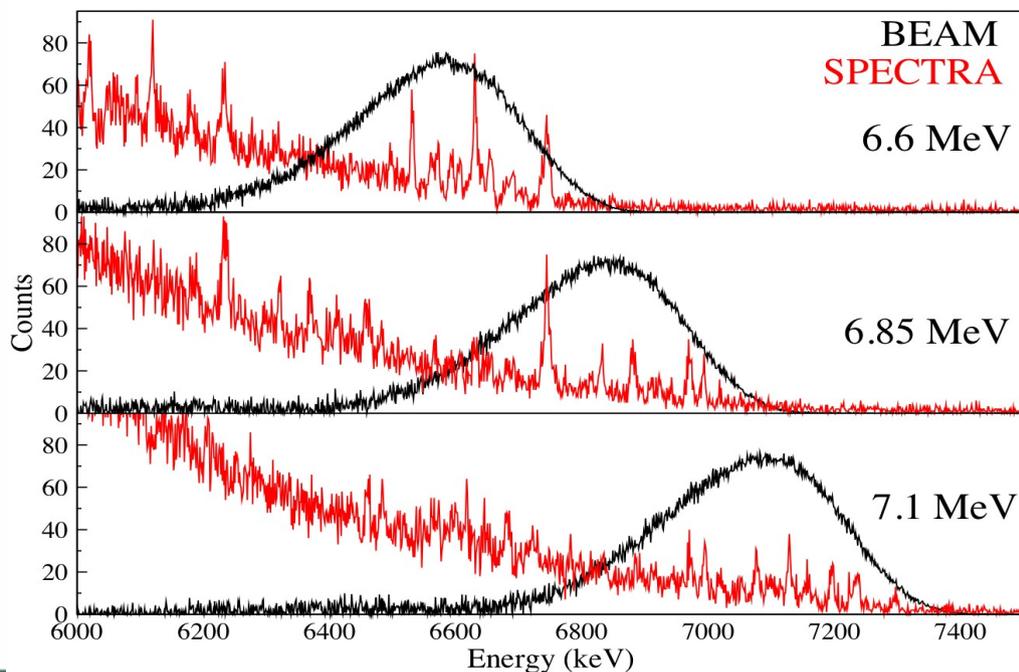


Strength concentrations – E1?

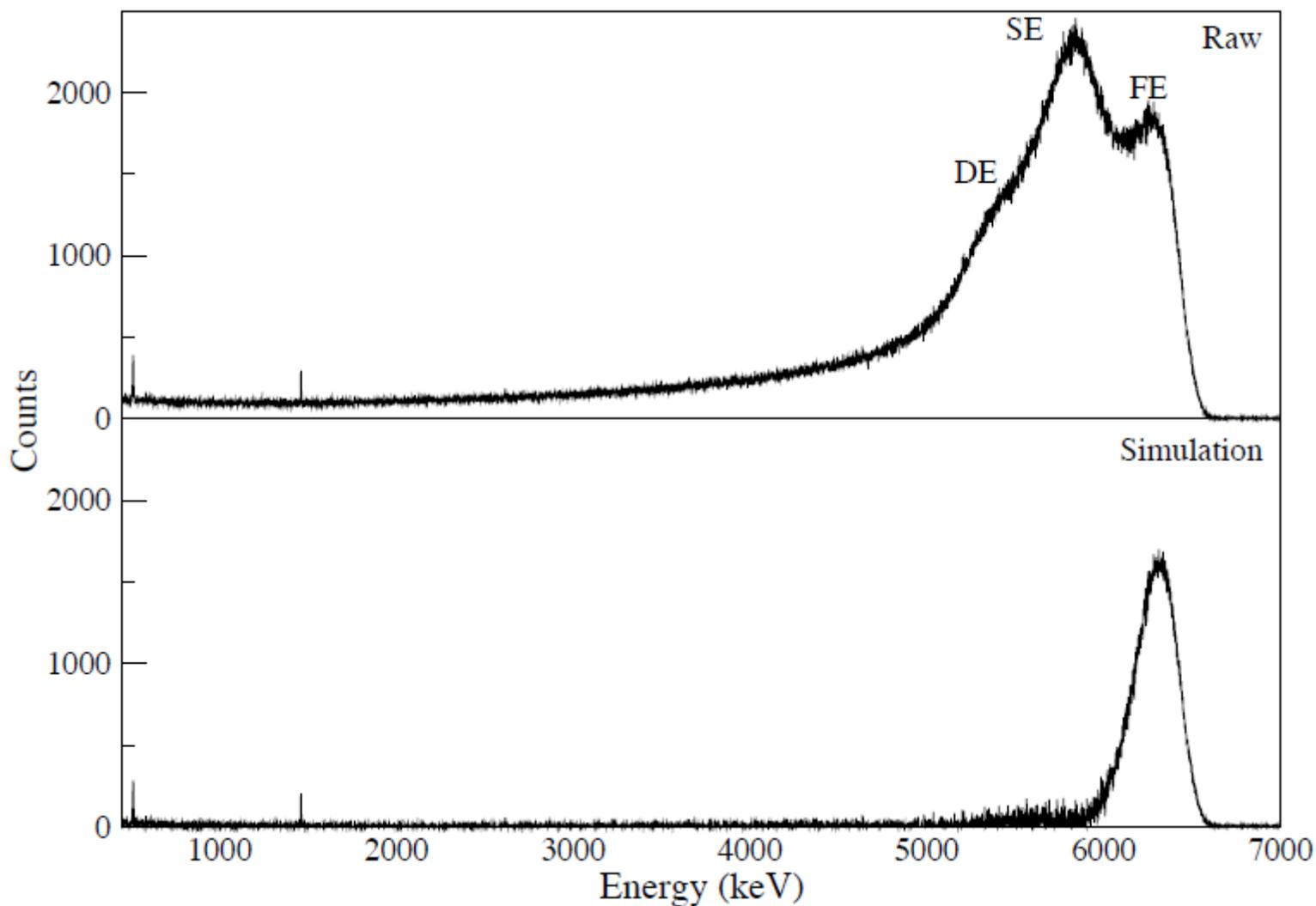
H.R. Weller et al.
 Progress in Particle
 and Nuclear Physics
 62 (2009) 257–303

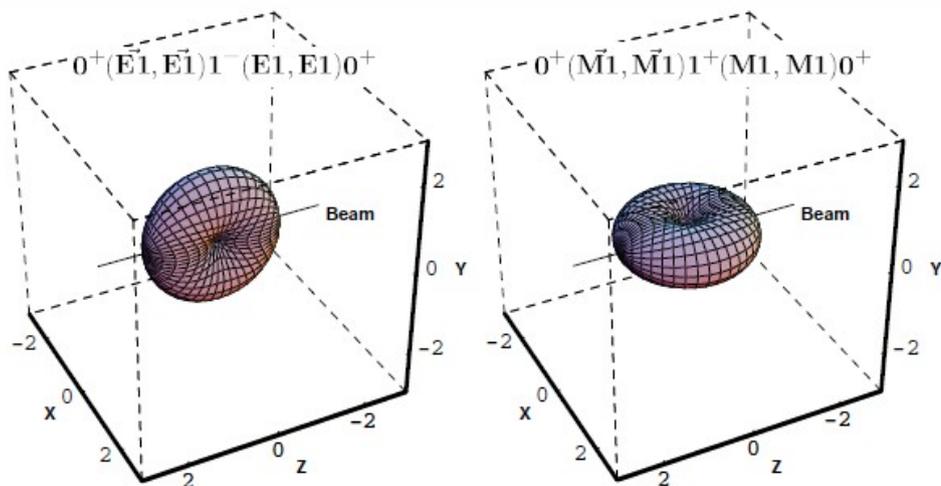


**100% polarized,
 near-monoenergetic gammas**



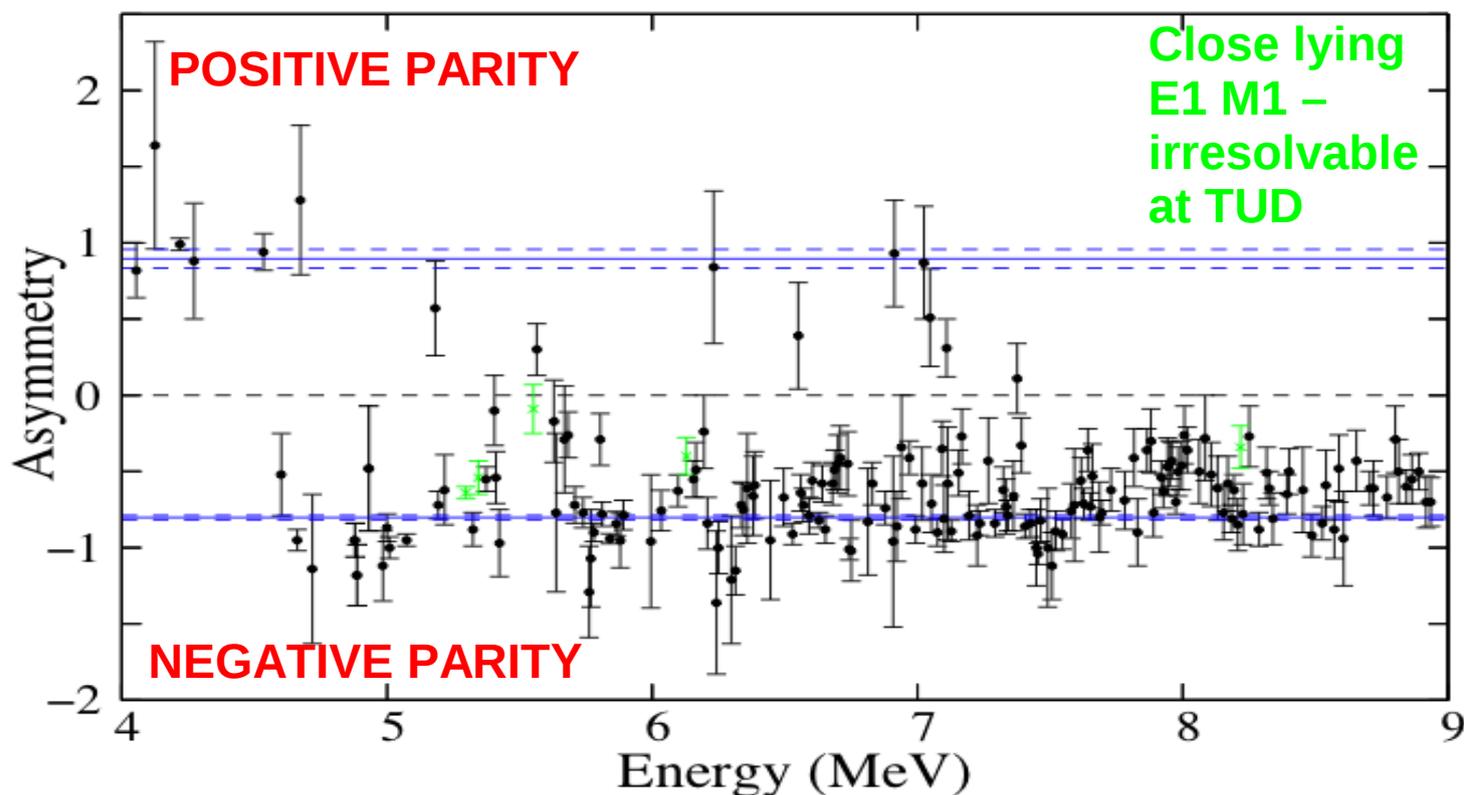
Actually beam profile derived from 0° HPGe spectrum and GEANT simulation.





Clear (and easy) identification
Of E1 excited states through
asymmetry horizontal/vertical

$$P_{ana} = \frac{W^{hor} - W^{ver}}{W^{hor} + W^{ver}}$$



M1

almost all:
E1

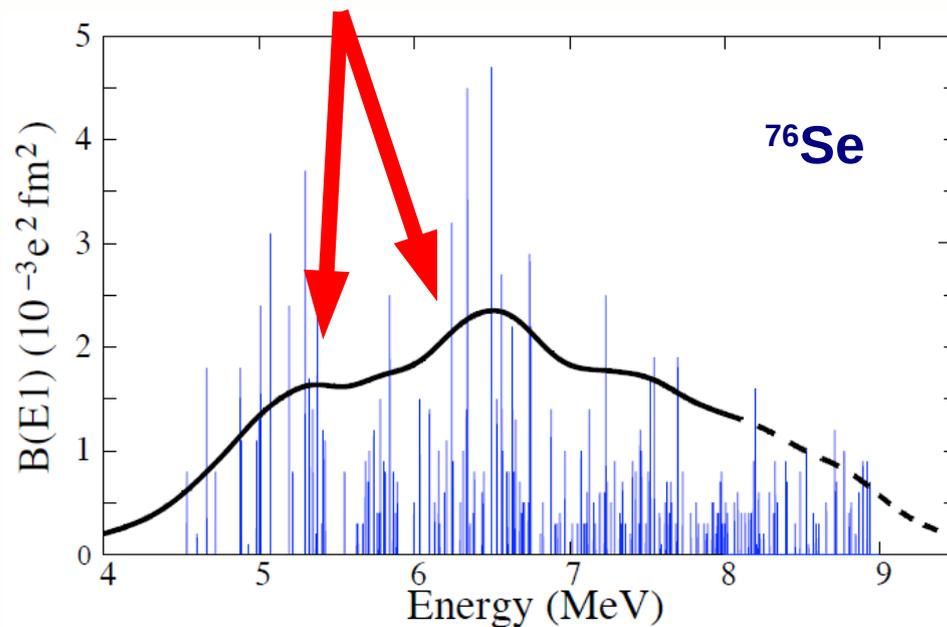
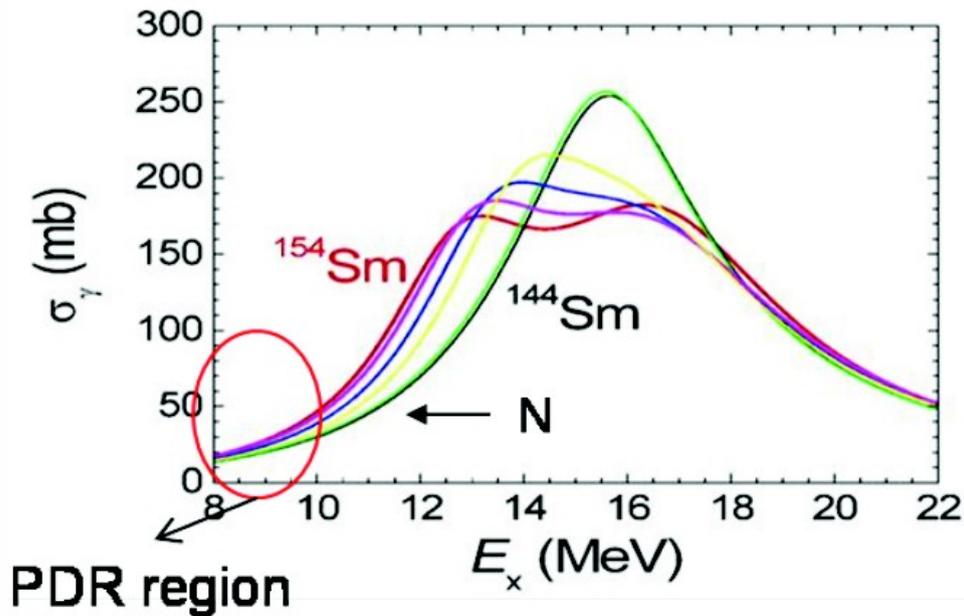
Between ~ 4-9 MeV: Cross sections from TU Darmstadt, parities from HIGS

Nathan Cooper, Yale
submitted to PRC

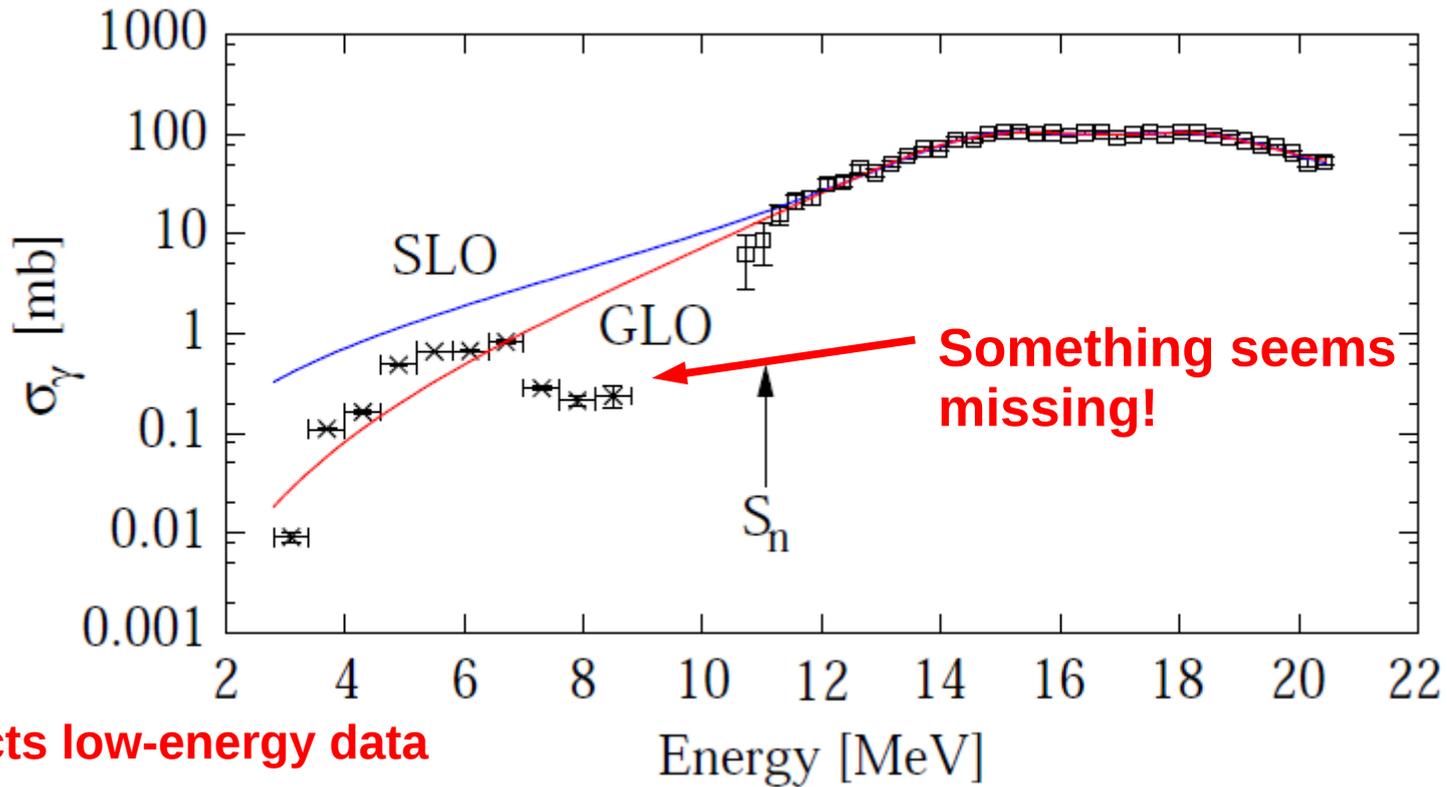
Phil Goddard, Yale/Surrey
MPhys thesis, in prep. for PRC

Deformation splitting of the
GDR (oscillations with respect
to two ellipsoid axes)

E1 strength distribution suggests
that Pygmy strength is split.
Splitting due to β -deformation?



Data from Bremsstrahlung only!
 Two Lorentzians fitted because ^{76}Se is deformed ($\beta \sim 0.31$)

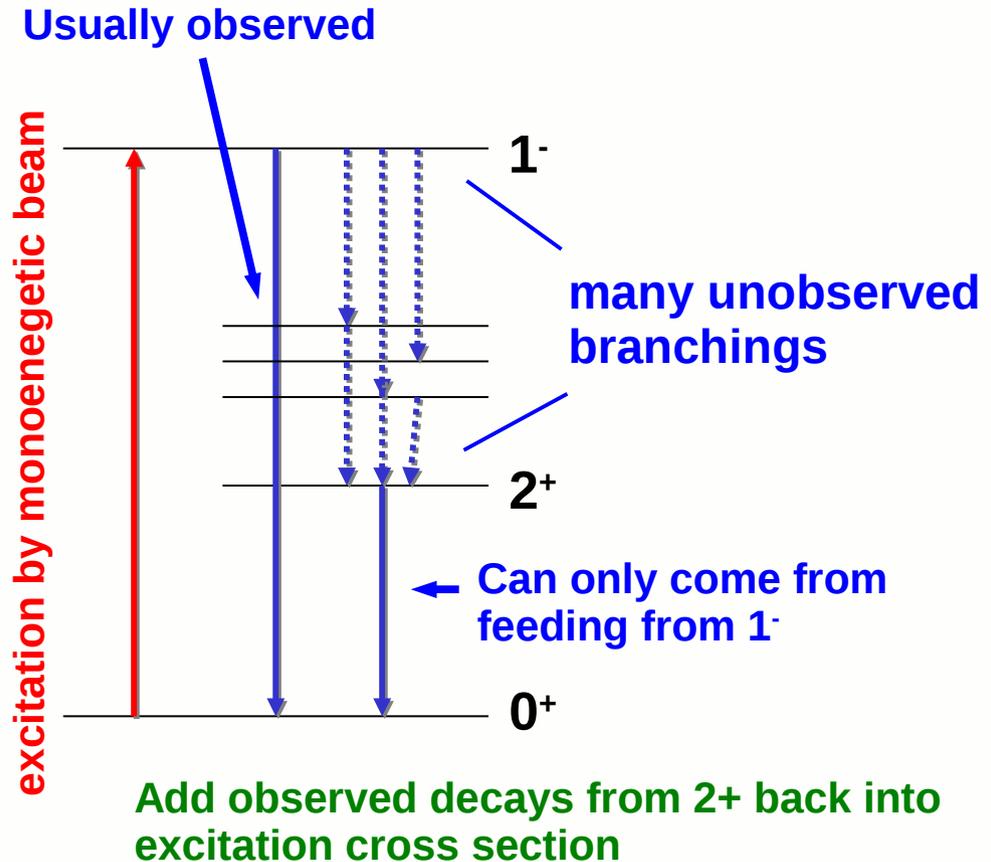
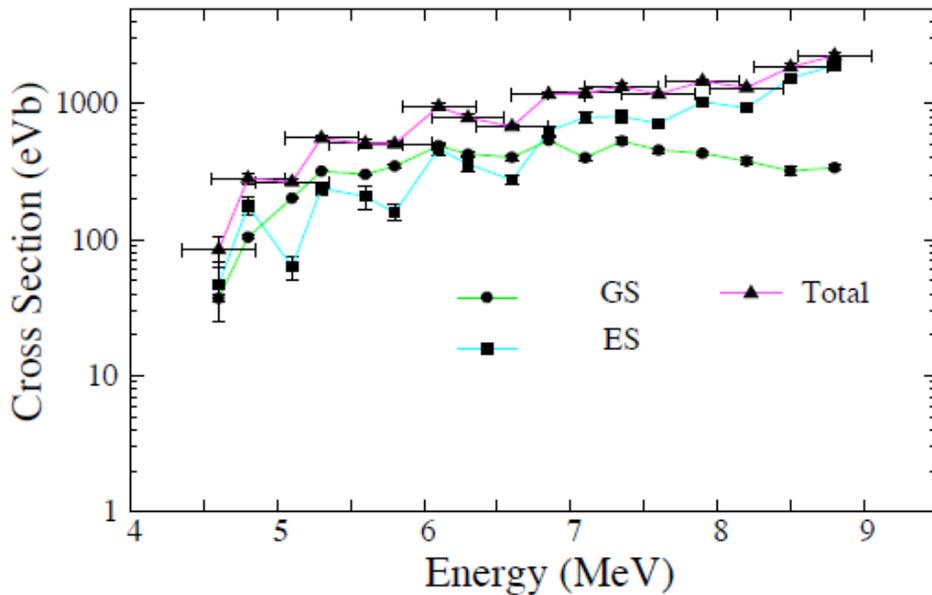


Overpredicts low-energy data

$$\sigma^{SLO} \propto \frac{E^2 \Gamma^2}{(E^2 - E_0^2)^2 + E^2 \Gamma^2} \quad \sigma^{GLO} \propto E \Gamma \left[\frac{E \Gamma(E)}{(E^2 - E_0^2)^2 + E^2 [\Gamma(E)]^2} \right]$$

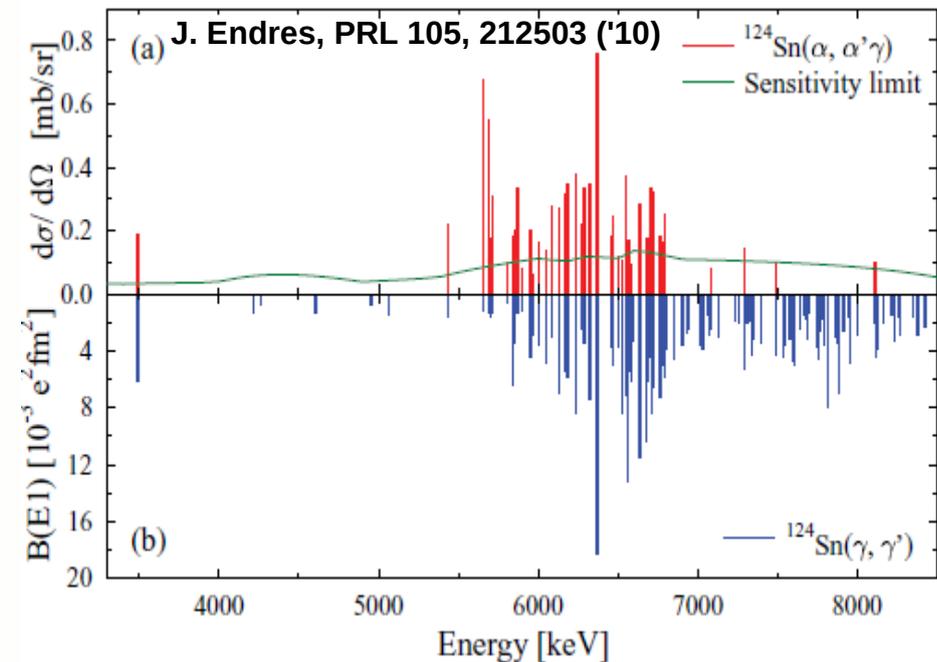
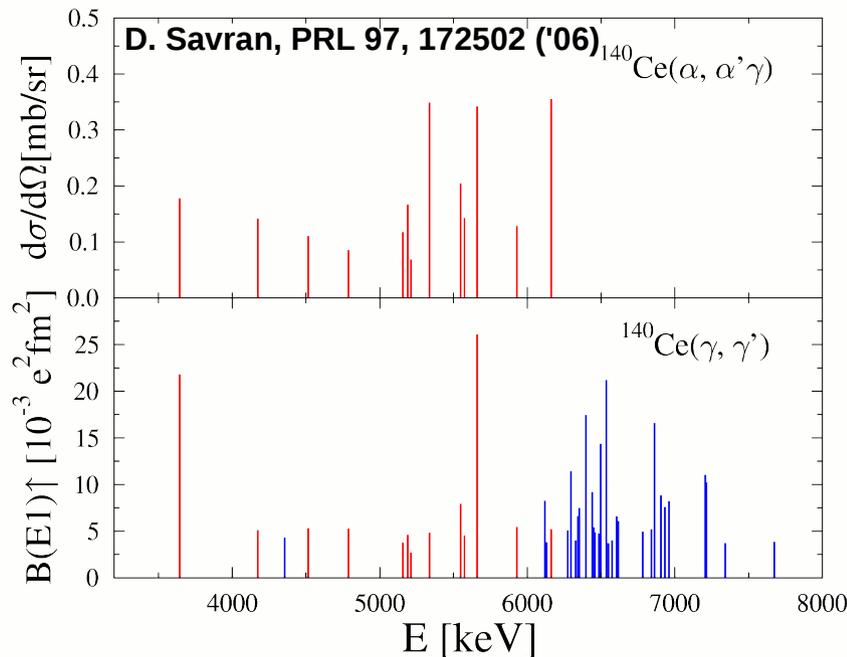
Now including HIGS Data:

Higher-lying states decay stronger to excited states – corrections to total E1 excitation strength!



- Could be an effect of structure of the higher (> 7 MeV) states \rightarrow GDR
- In Pygmy region: affects sum strength by a factor of 2 or more

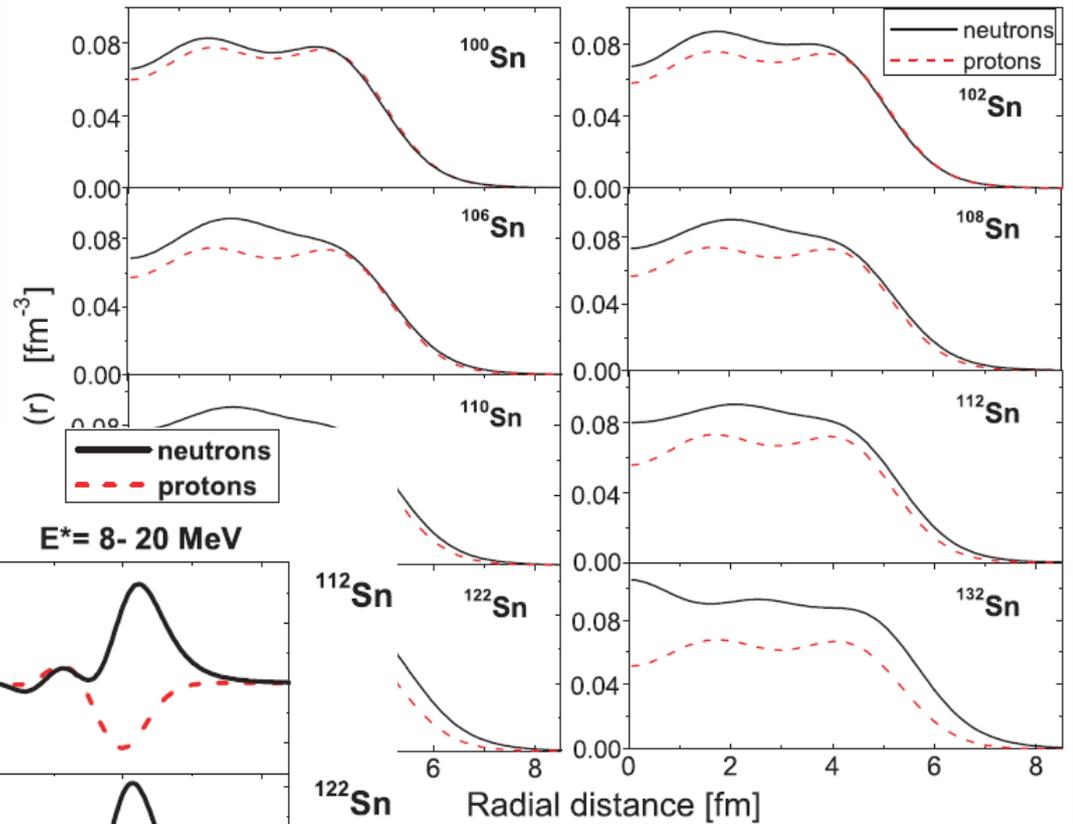
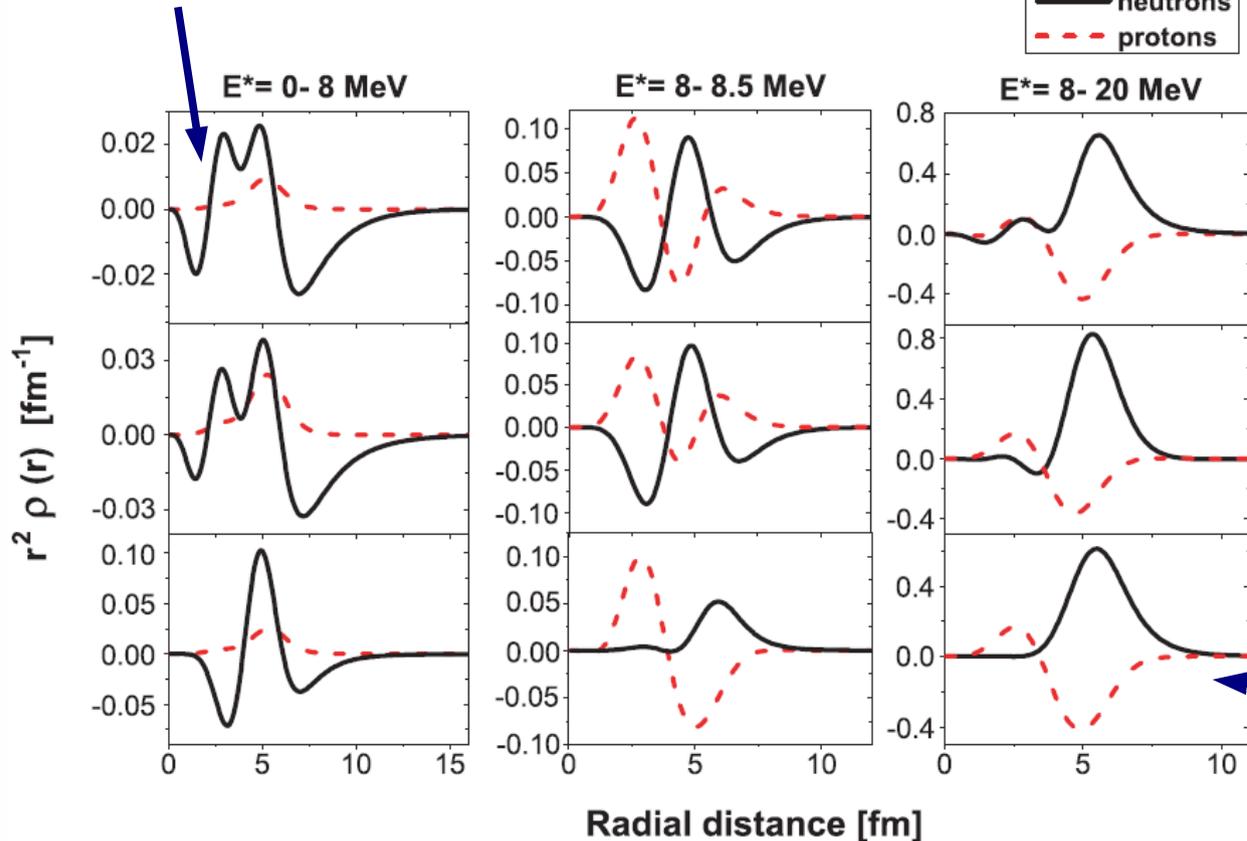
Another way of splitting the PDR



Higher lying states not excited in α -scattering
 \Rightarrow Different underlying structure
(isoscalar / isovector part)

Sn isotopes:
Calculated proton / neutron densities
-> neutron skin

Transition densities:
Isoscalar, n-oscillation on surface



Tsoneva / Lenske, PRC 77, 024321 ('08)
HFB + QPM

isovector -> GDR

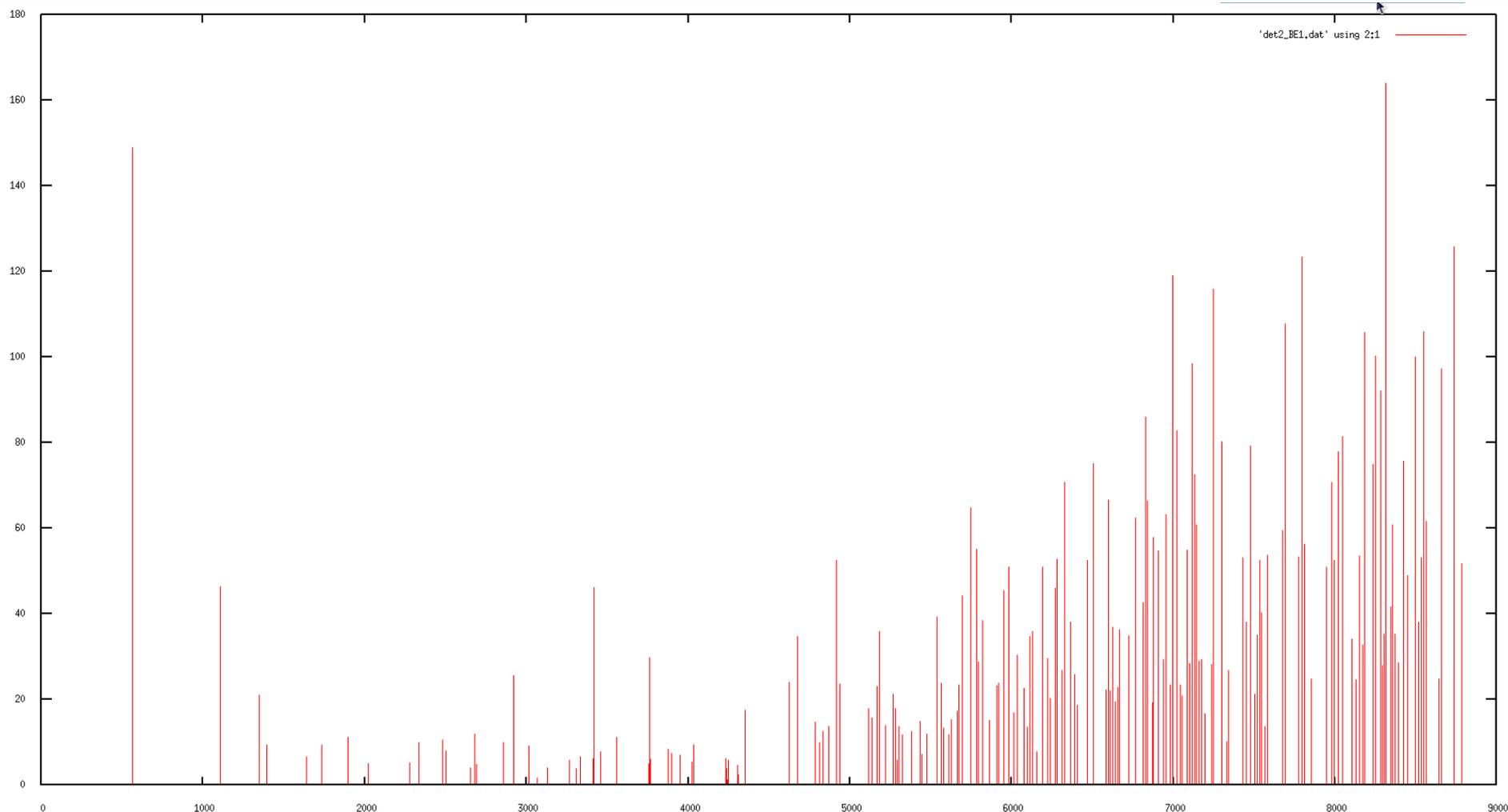
First: finish all corrections from HIGS data and refit Lorentzians!

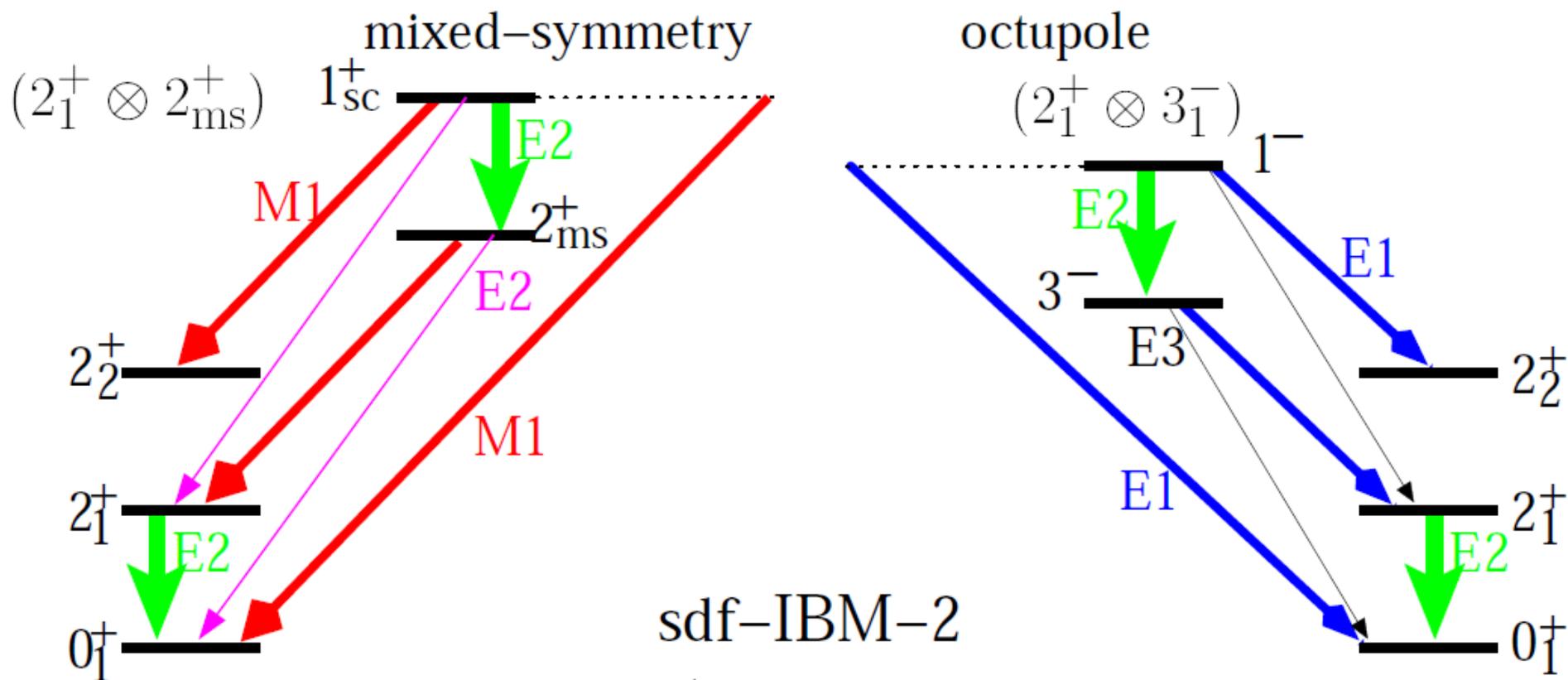
Comparison to 2β -decay partner ^{76}Ge

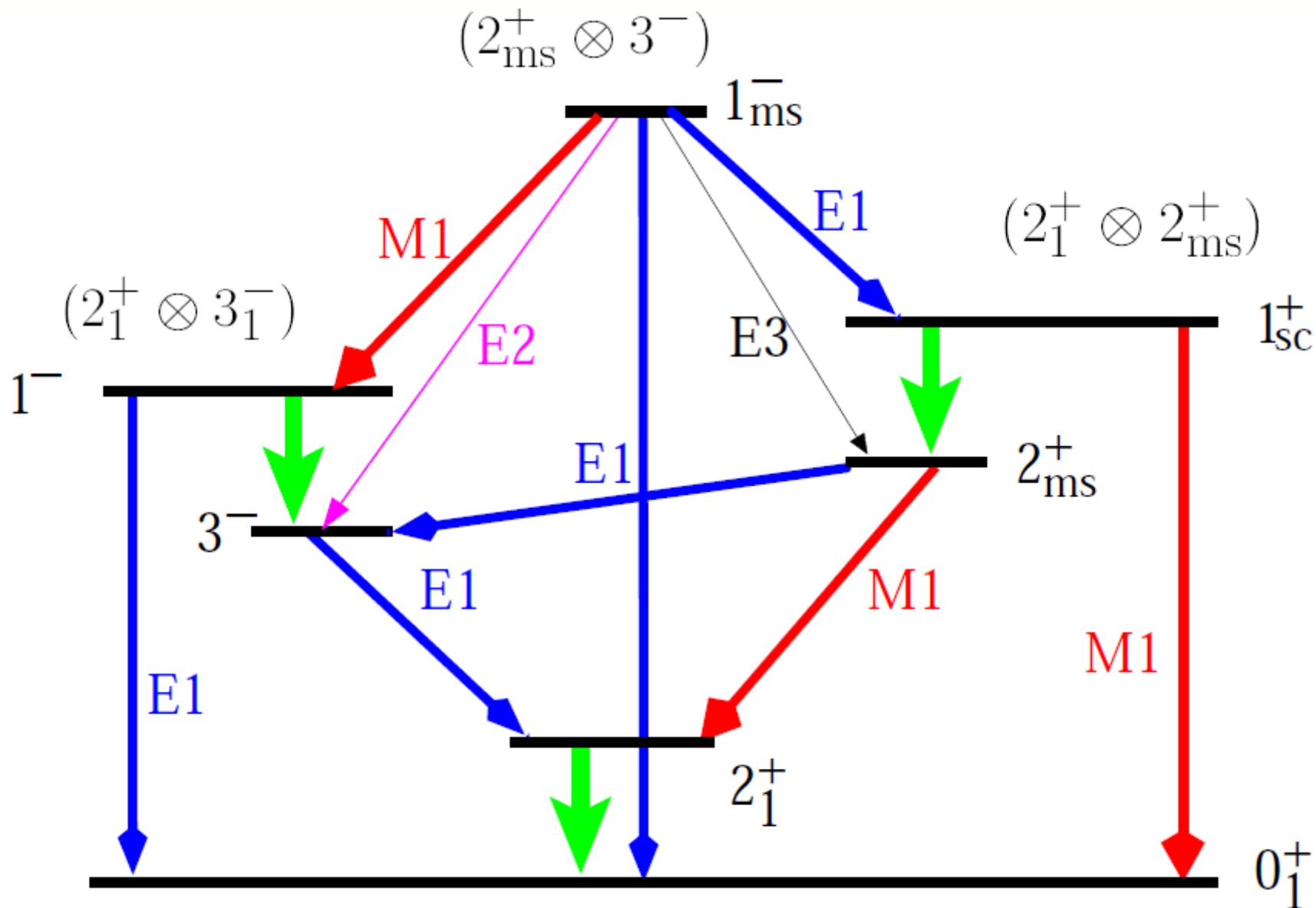
**We need a means of observing the intermediate transitions,
*Directly!***

Same holds for other excitation modes, few examples follow...

Pete Humby, Yale/Surrey, very first plot

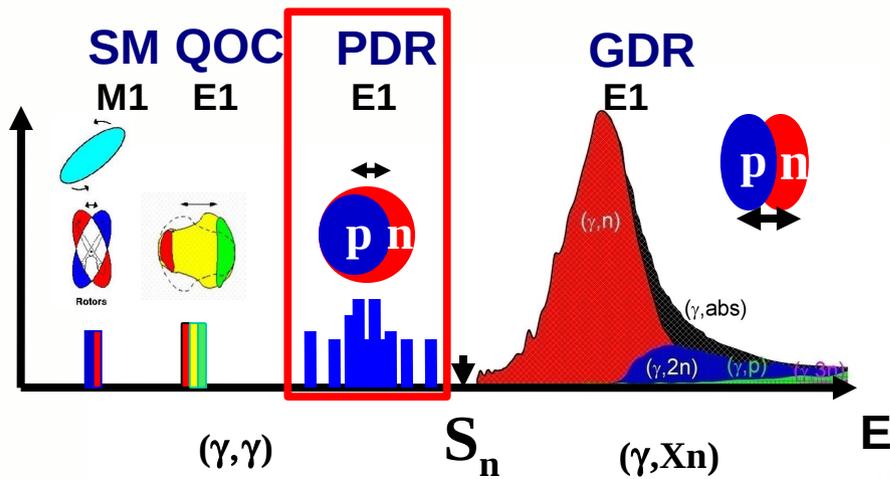






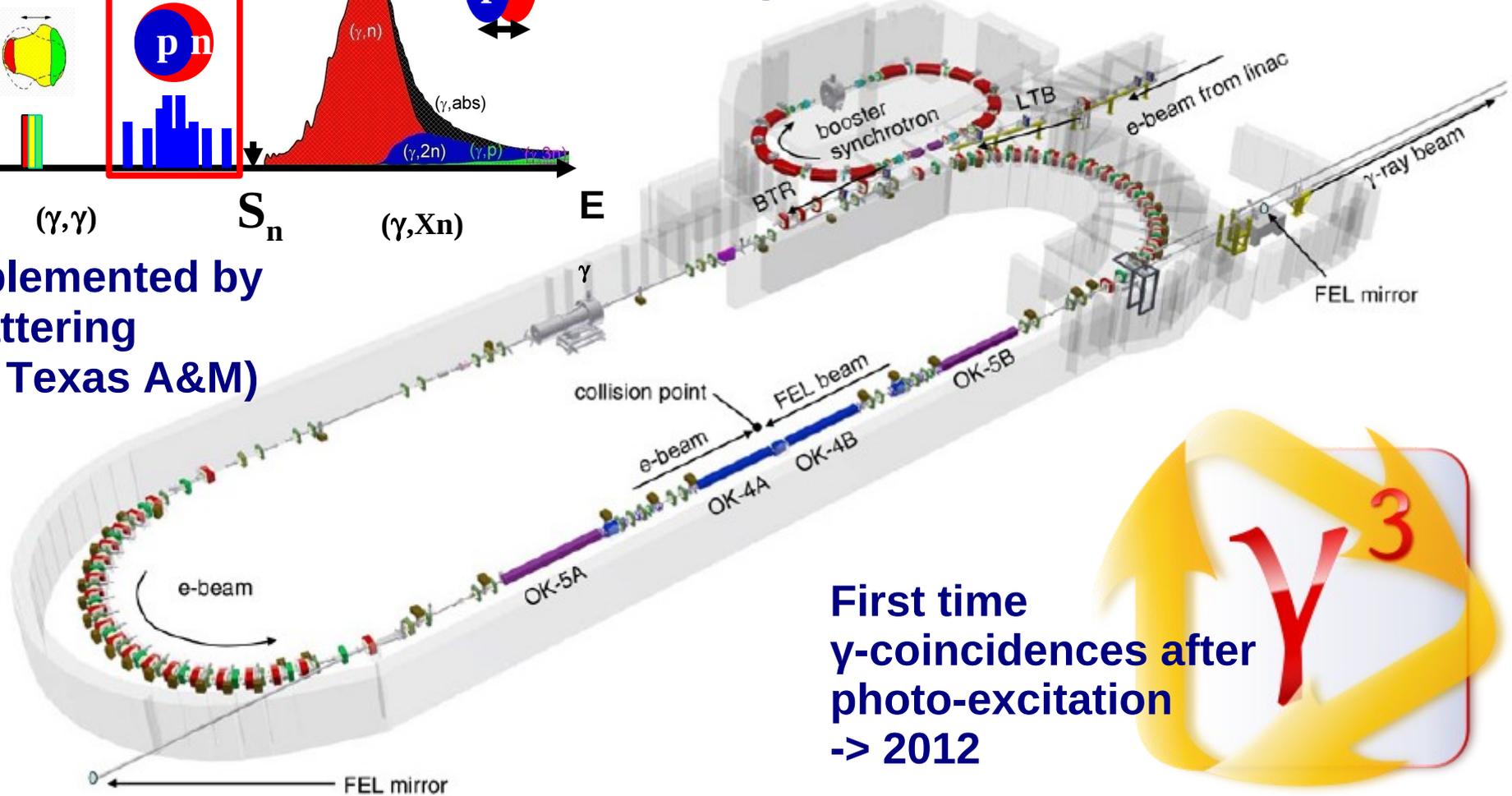
Smirnova et al., NPA 678, 235 (2000)

Missing so far: 3_{ms}^- state \rightarrow M. Scheck



**Study of the Pygmy Dipole Resonance
-> Neutron Skins
Study of Multi-Phonon States**

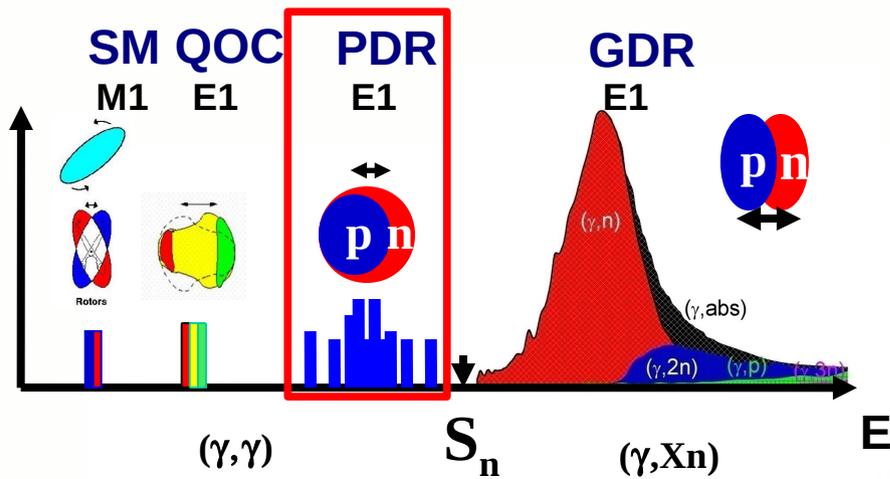
**Complemented by
 α -scattering
(KVI / Texas A&M)**



**First time
 γ -coincidences after
photo-excitation
-> 2012**

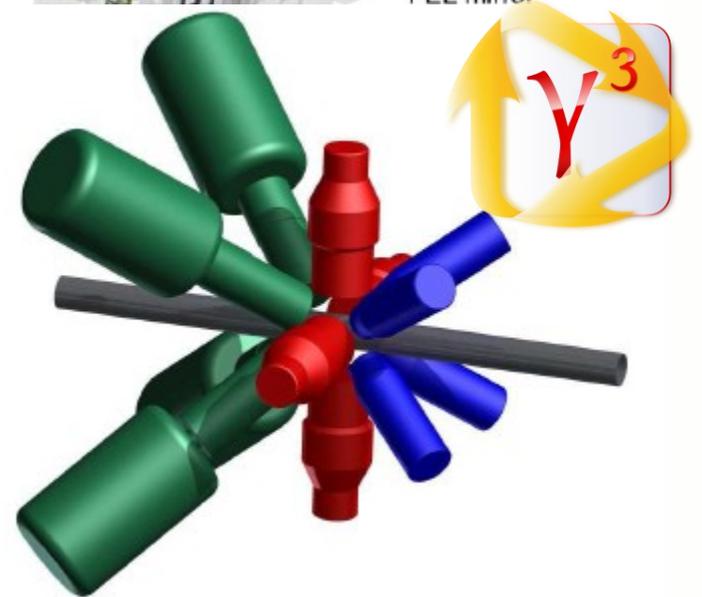
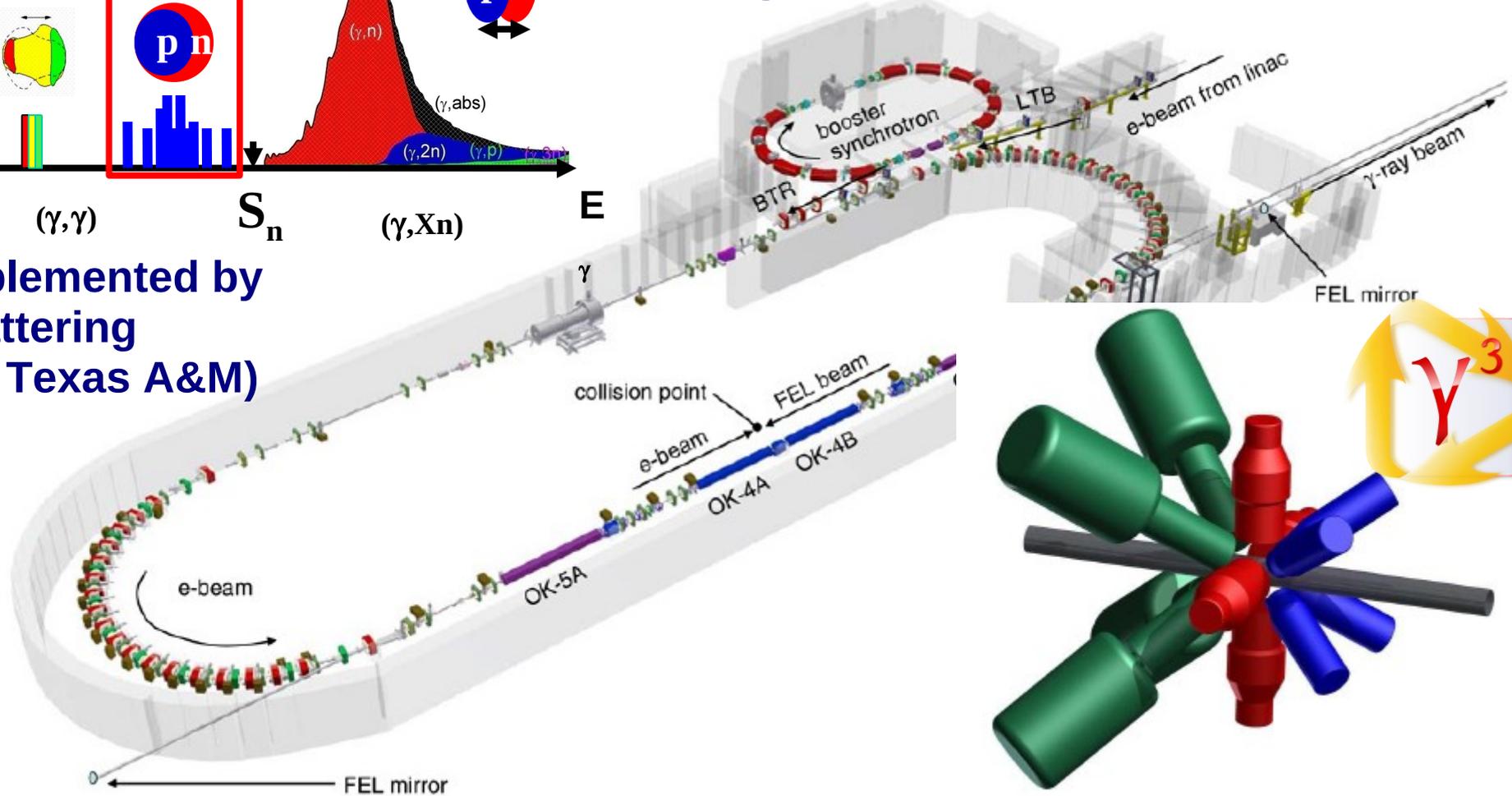


**A new project coming up: Extreme Light Infrastructure (ELI) in Europe
(Collide highly-intense electron beam high-power lasers)**



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The Yale Nuclear Structure Group 2012

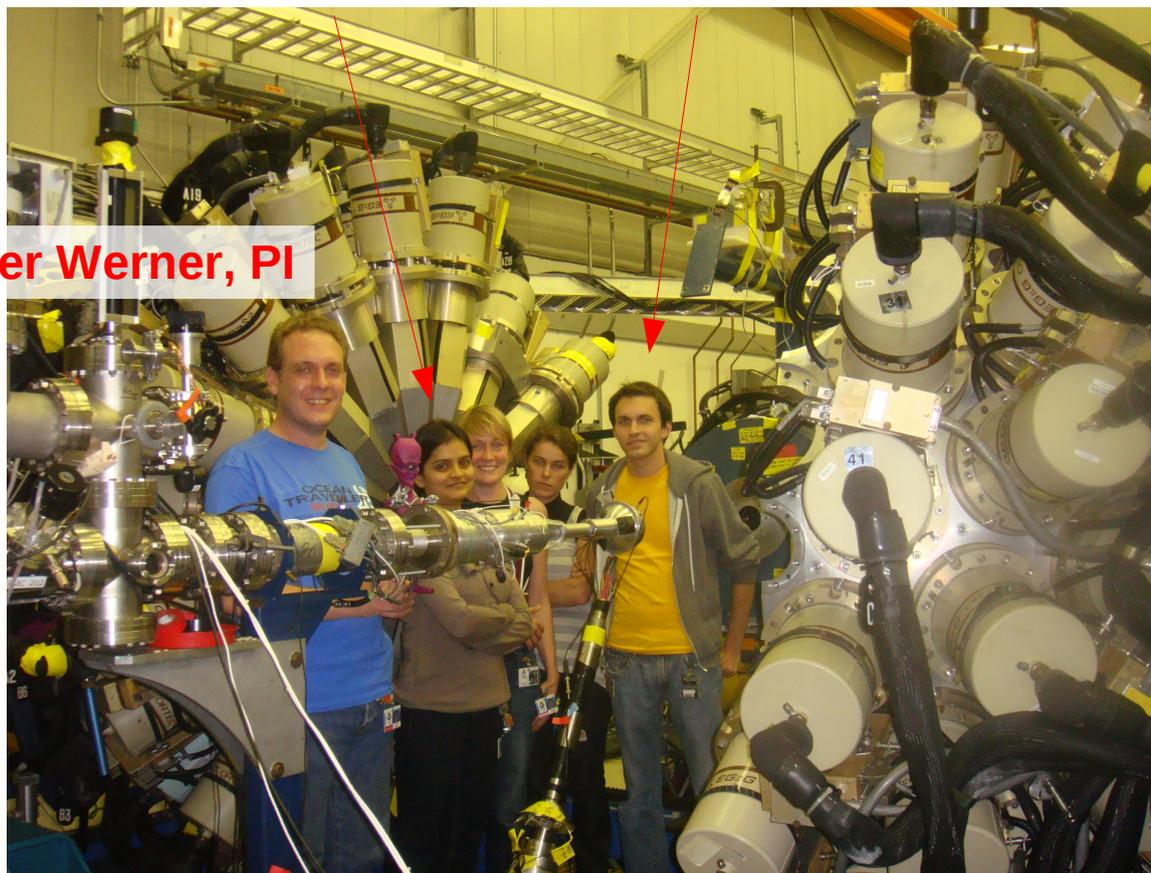
Farheen Naqvi, PD

Nathan Cooper, GS

Rick Casten, Prof.



Christian Bernards, PD



Volker Werner, PI

+ Peter Humby (MPhys Surrey) !!