

# An overview of MC Tools at BNL for an EIC

Matt Lamont  
Brookhaven National Lab

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# EIC Task Force at Brookhaven

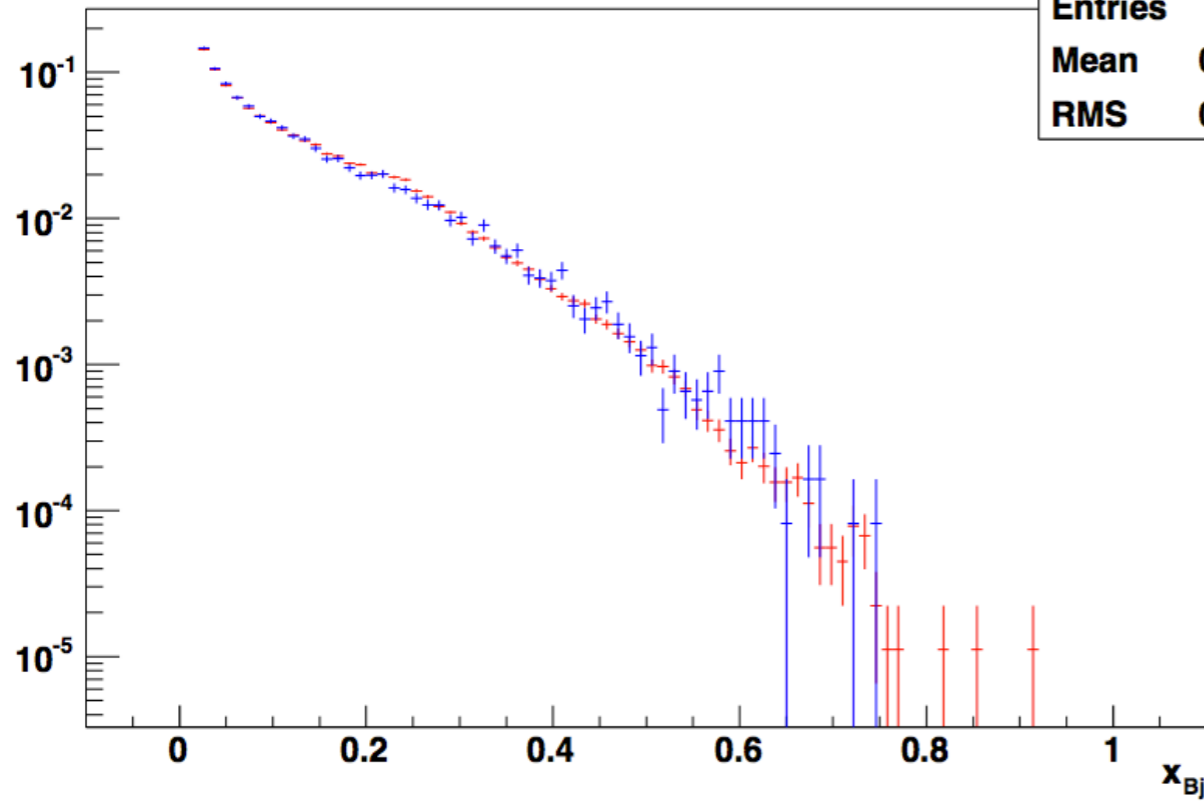
- Task Force Leaders
  - ➔ Elke Aschenauer (Spin); Thomas Ullrich (Heavy Ions)
- Active Task Force Members
  - ➔ MACL, Ramiro Debbe, Jamie Dunlop (Heavy Ions)
  - ➔ J-H. Lee, Wlodek Guryn (pp2pp - Roman Pot expertise)
  - ➔ Pavel Nevski (Simulation framework)
- New Post-doc hires
  - ➔ Thomas Burton + 1 other (spin)
  - ➔ Tobias Toll (theory) - student of Hannes Jung in Hamburg and background with Lund group
- Students from Stony Brook
  - ➔ Michael Savastio, Anders Kirleis, Will Foreman and Peter Schnatz
- + large contribution from Collider-Accelerator Department (CAD)
  - ➔ led by Vadim Ptitsyn, Vladimir Litvinenko + many others

# gmc\_trans code (spin physics)

- [https://wiki.bnl.gov/eic/index.php/Gmc\\_trans](https://wiki.bnl.gov/eic/index.php/Gmc_trans)
- gmc\_trans: MC generator for SIDIS
  - ➔ simulates single hadron production from lepton scattering off a transversely polarised hadron
  - ➔ includes the hadron transverse spin (transversity) distribution and transverse-momentum dependent (TMD) distributions, e.g. Sivers function
- Code developed for HERMES (27.57 GeV electron on stationary proton target)
  - ➔ Code re-written by Tom Burton for collider kinematics for arbitrary electron/proton energies
  - ➔ Code written in Fortran with small amount of “C”
    - ▶ “C” used to interface with Gnu Scientific Library’s VEGAS integration routine

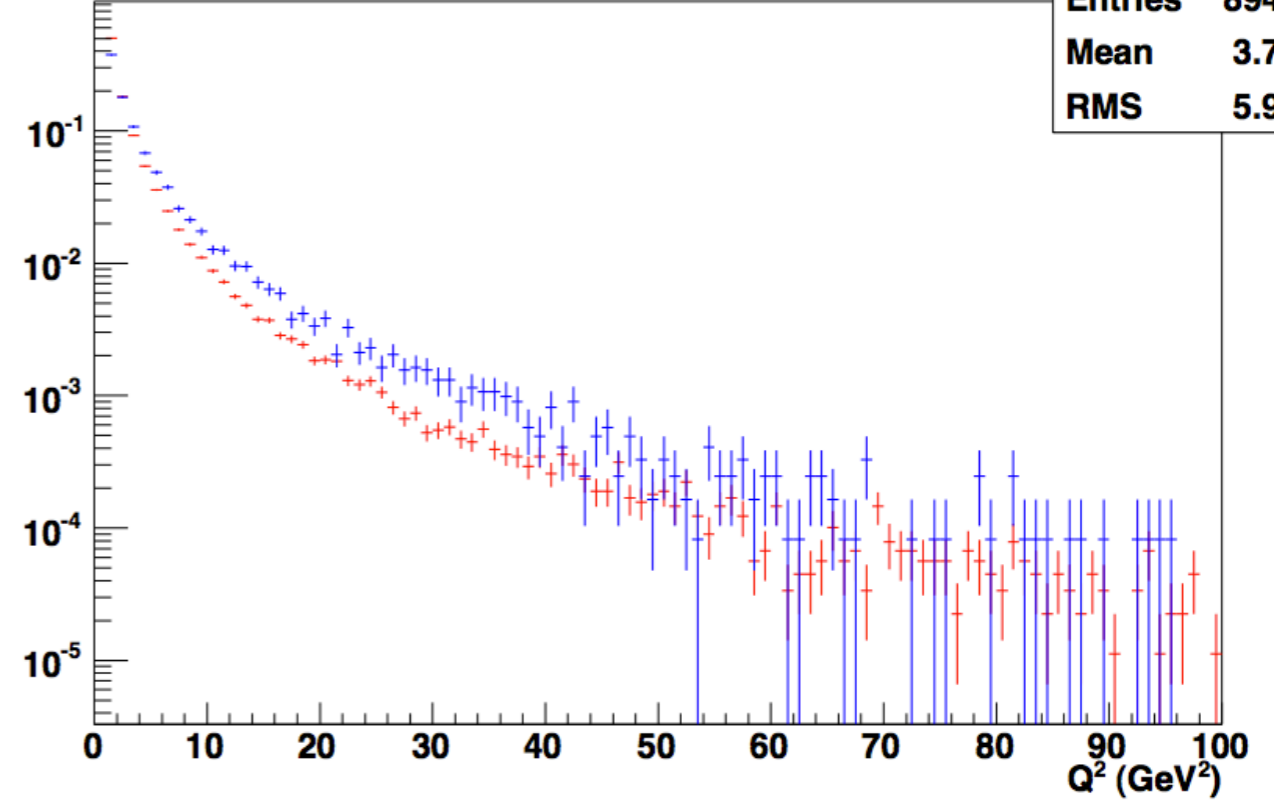
# gmc\_trans code (spin physics)

Bjorken x of event,  $x_B$



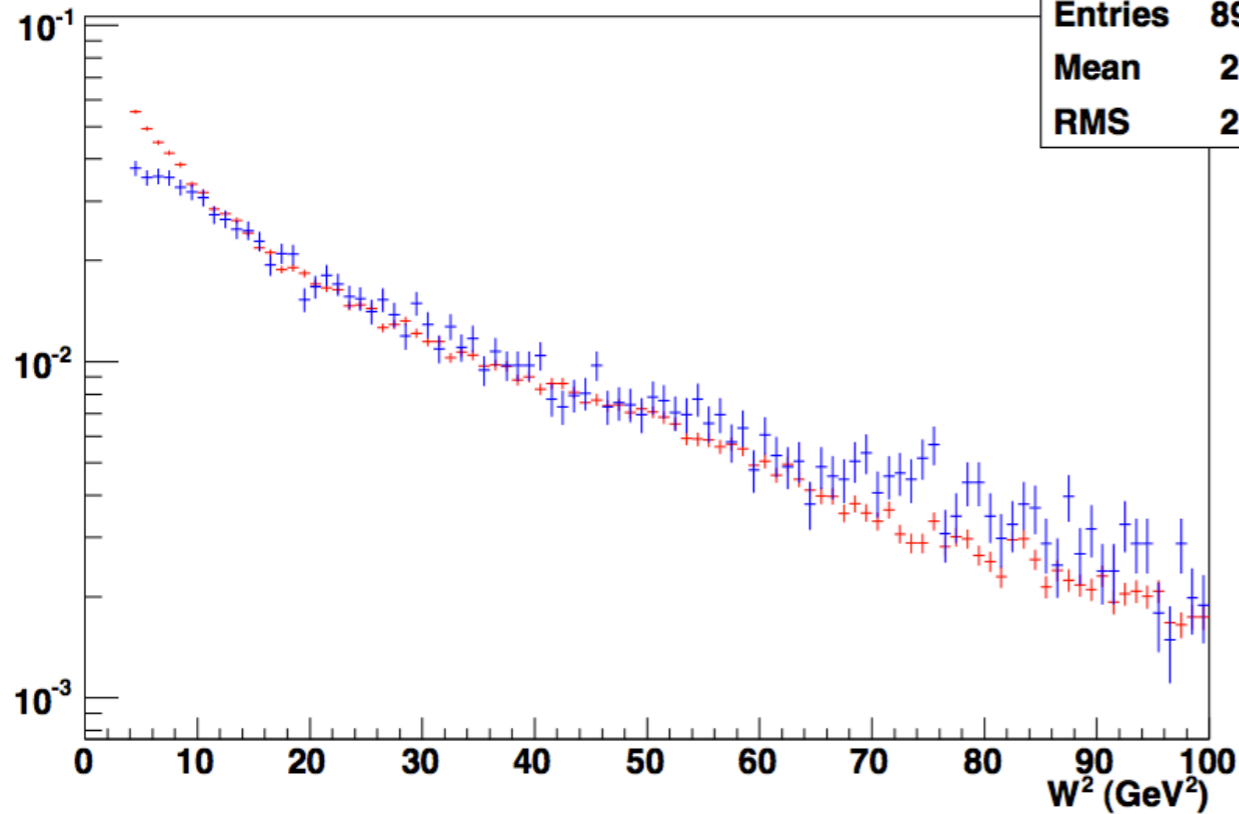
x	
Entries	89444
Mean	0.1256
RMS	0.1044

Virtuality of exchanged  $\gamma$ ,  $Q^2$



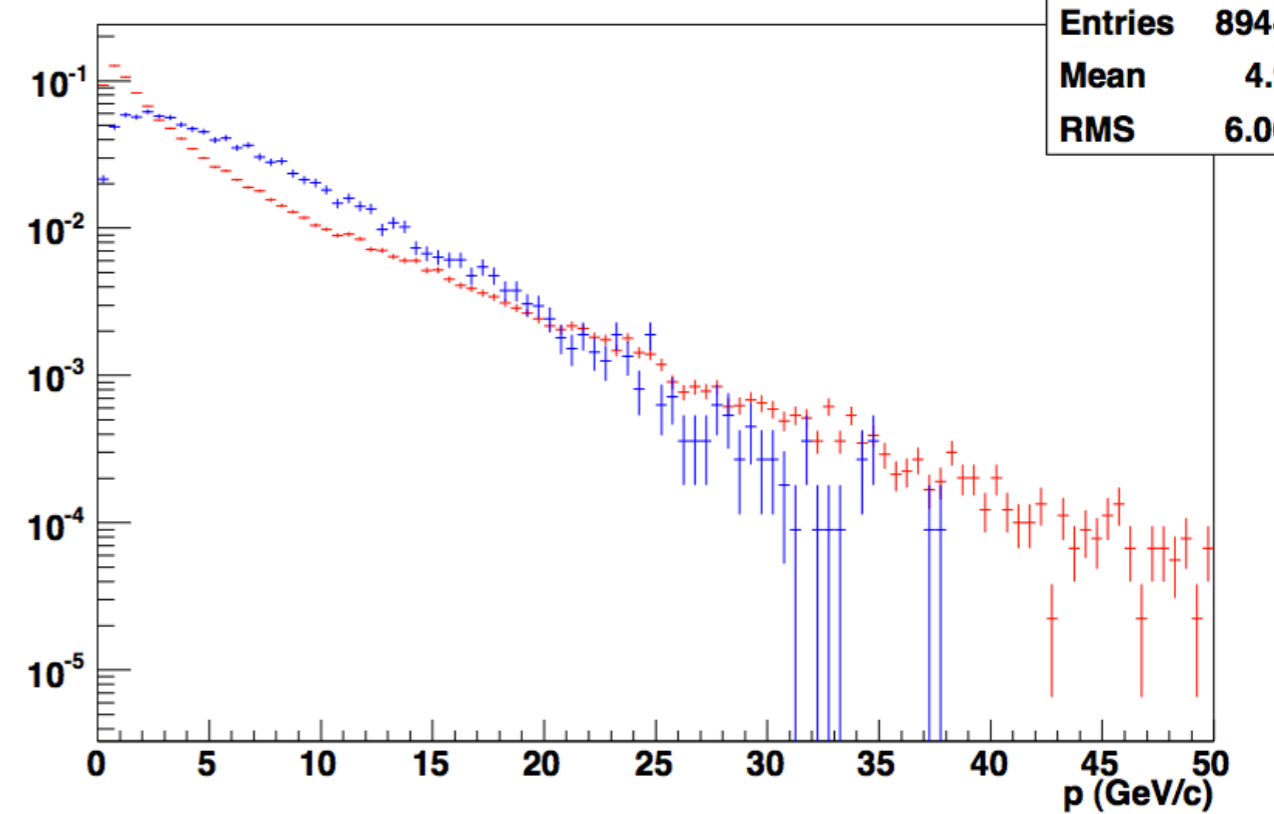
QSquared	
Entries	89444
Mean	3.759
RMS	5.943

Invariant mass of hadronic system,  $W^2$



WSquared	
Entries	89444
Mean	27.94
RMS	22.95

p of  $\pi^+$



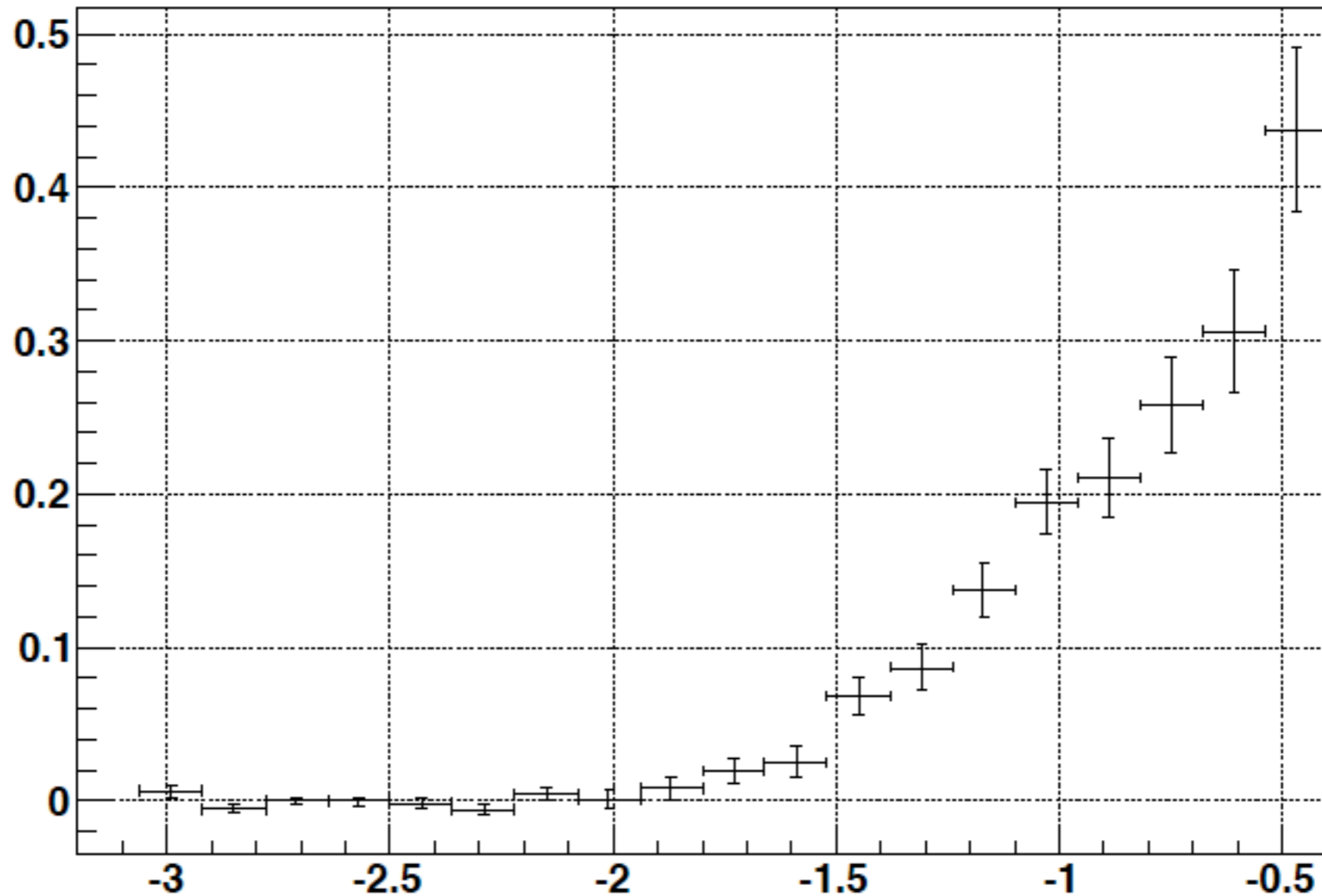
pLeadingParticle	
Entries	89444
Mean	4.97
RMS	6.007

# PEPSI - Polarised Electron Proton Scattering Interaction

- MC code for polarised deep inelastic lepto-production via EM interaction based on LEPTO
  - ➔ Generates hard  $\gamma^*$ -parton scattering according to polarisation dependent cross-section
  - ➔ Has inbuilt  $\Delta q(x)$  and  $\Delta g(x)$  distributions and supports user-implemented distributions

# PEPSI - Polarised Electron Proton Scattering Interaction

A1



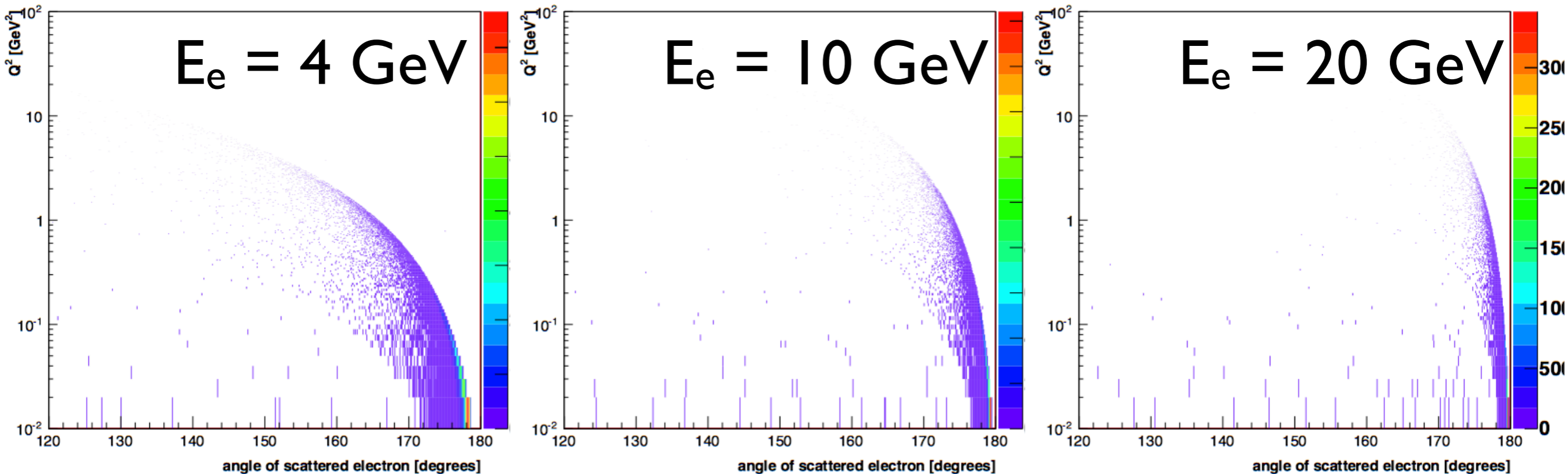
A1 - helicity asymmetries in  $\gamma^*$  absorption cross-section

# PYTHIA MC Generator

- <https://wiki.bnl.gov/eic/index.php/PYTHIA>
- MC generator for both DIS and diffractive e+p collisions (no rapidity gaps)
  - ➔ Using version 6.4.13 of PYTHIA for e+p collisions
    - ▶ e+p collisions not implemented in version 8 (C++)
  - ➔ Radiative corrections are included (radgen)
  - ➔ Lots of processes can be simulated
    - ▶ elastic VMD, diffractive VMD, LO DIS, QCDC, PGF ....

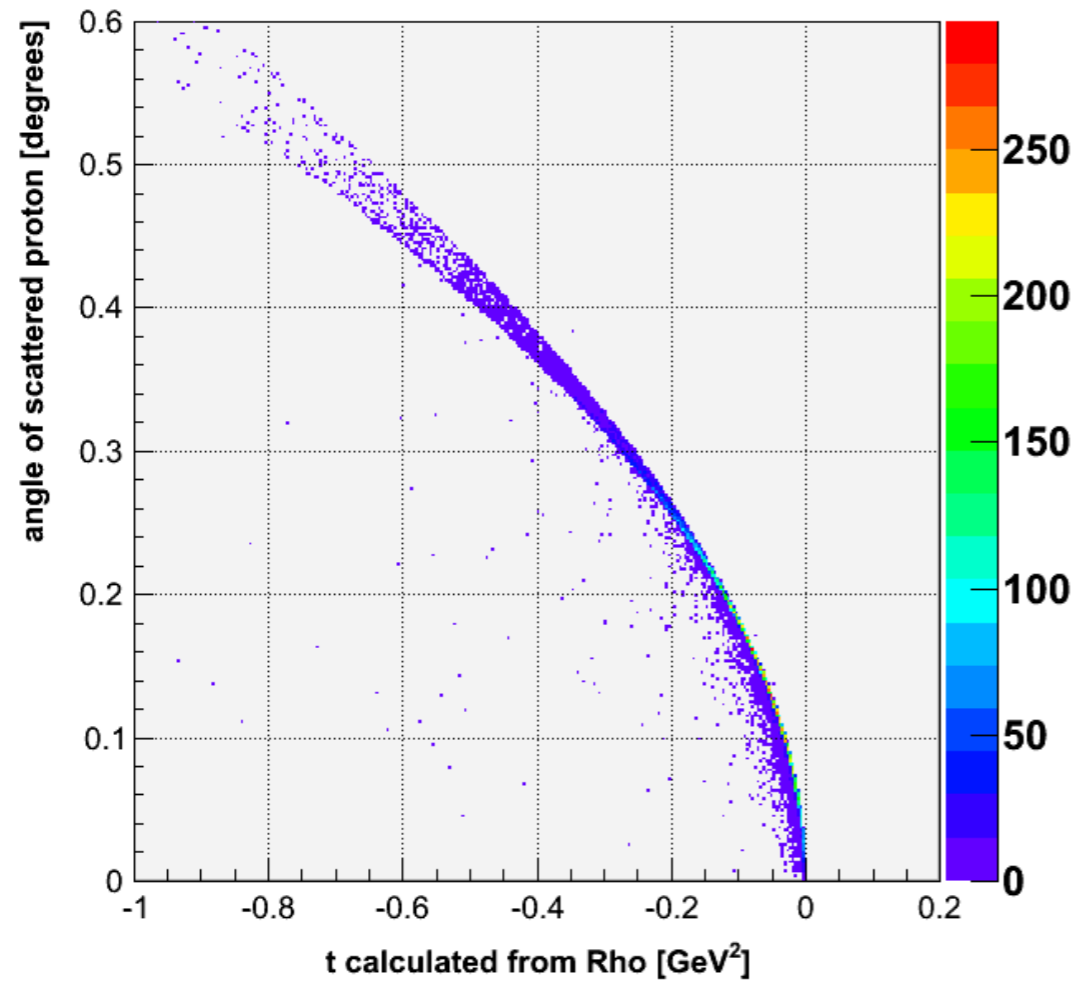


# PYTHIA MC Generator - diagnostic plots



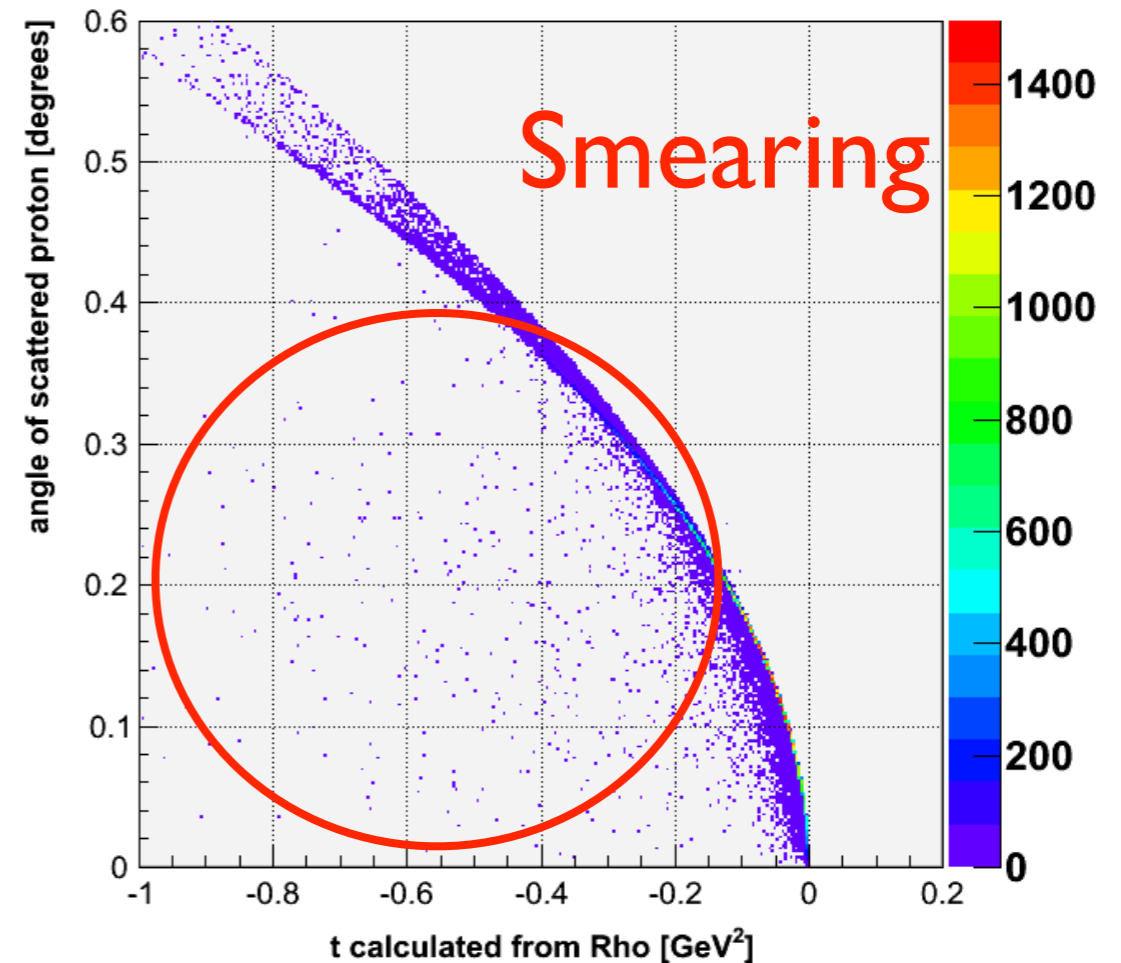
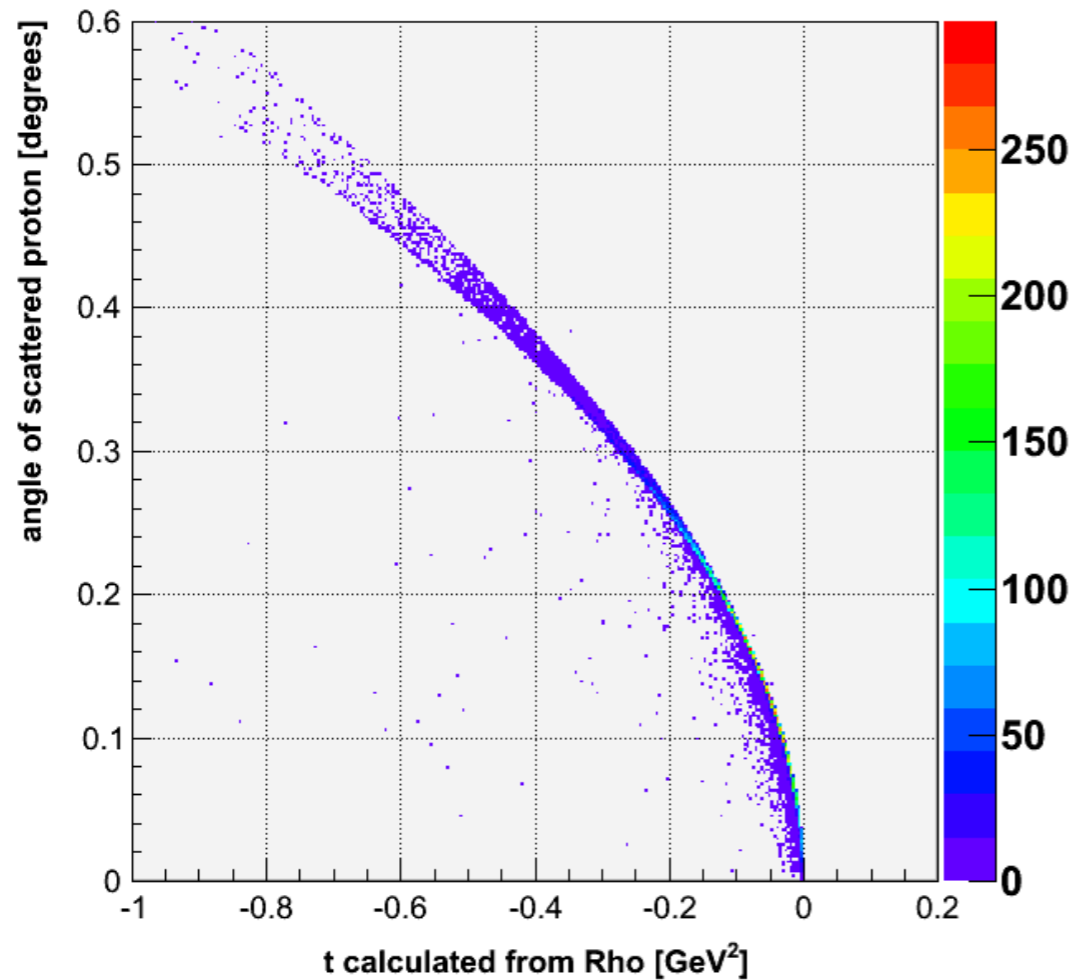
- Analysis of electron scattering angle in PYTHIA
  - ➔ higher energy electrons go at smaller angles wrt beam axis
    - ▶ harder to detect!!
    - ▶ independent of hadron energy

# PYTHIA MC Generator - radiative corrections



# PYTHIA MC Generator - radiative corrections

with radiative corrections



- Radiative corrections (via RADGEN)

- ➔ Smear the t calculation at the  $\rho$  vertex

- ➔ t calculated from the proton vertex is unaffected but harder to measure experimentally

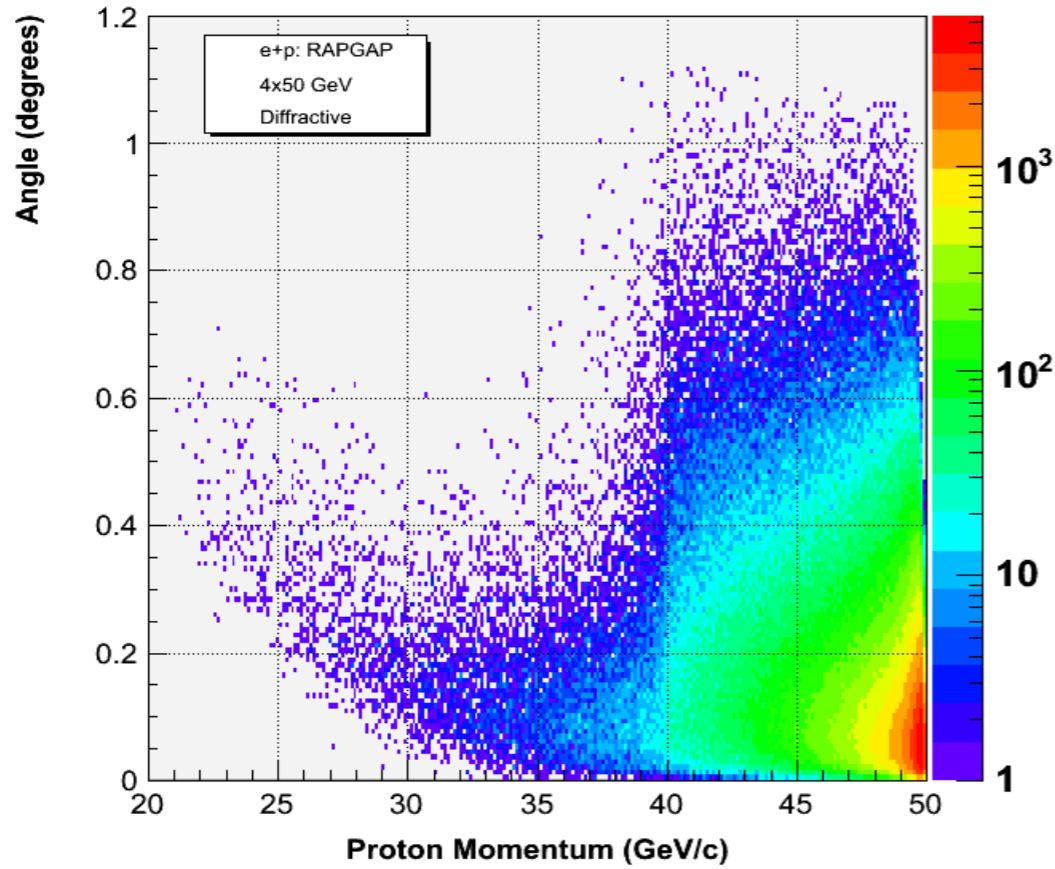
- ▶ need a proton spectrometer

# RAPGAP MC Generator

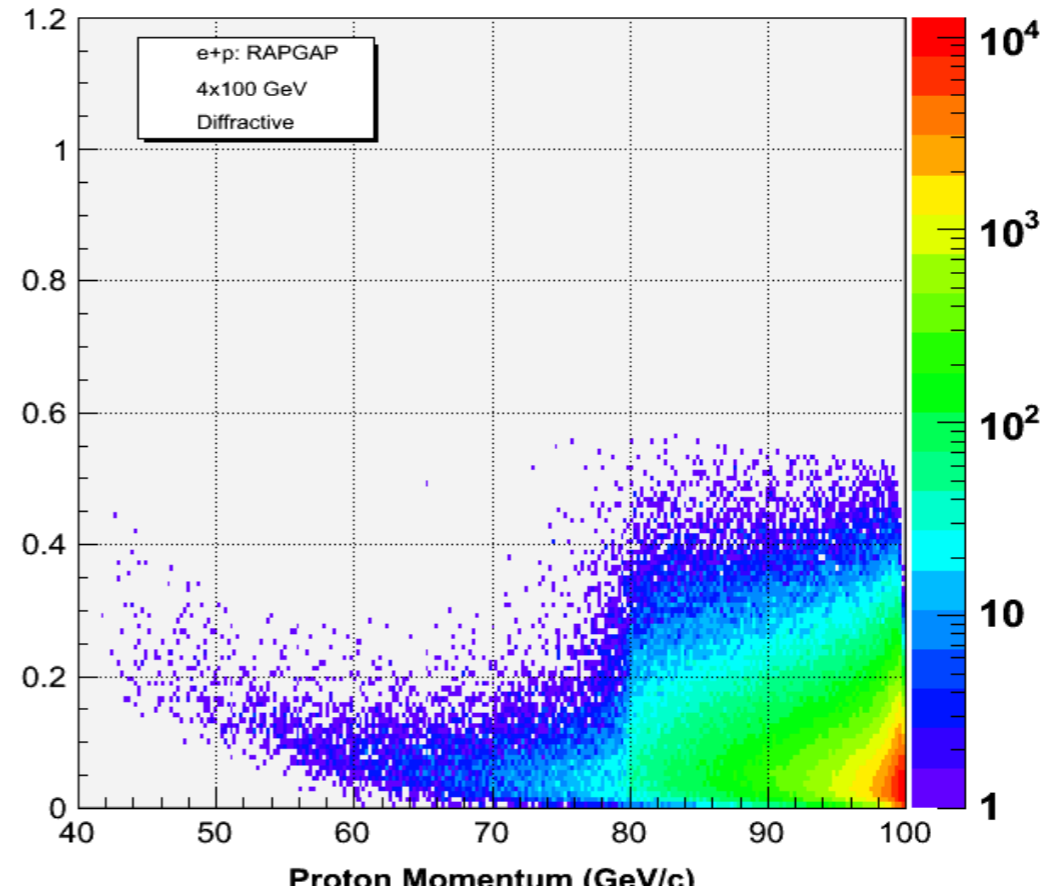
- <https://wiki.bnl.gov/eic/index.php/RAPGAP>
- MC generator for both DIS and diffractive e+p collisions (with rapidity gaps).
  - ➔ Diffractive collisions described by:
    - ▶ 2 gluon exchange (pQCD)
    - ▶ SATRAP
      - Saturation model (colour dipole) implemented by Henri Kowalski
  - ➔ Radiative corrections are included (utilising HERACLES)
- Need to use Rapgap version 3.2-beta-01 (released Feb 2010)
  - ➔ problem with proton kinematics we discovered has been corrected

# RAPGAP kinematics: scattered proton (diffractive)

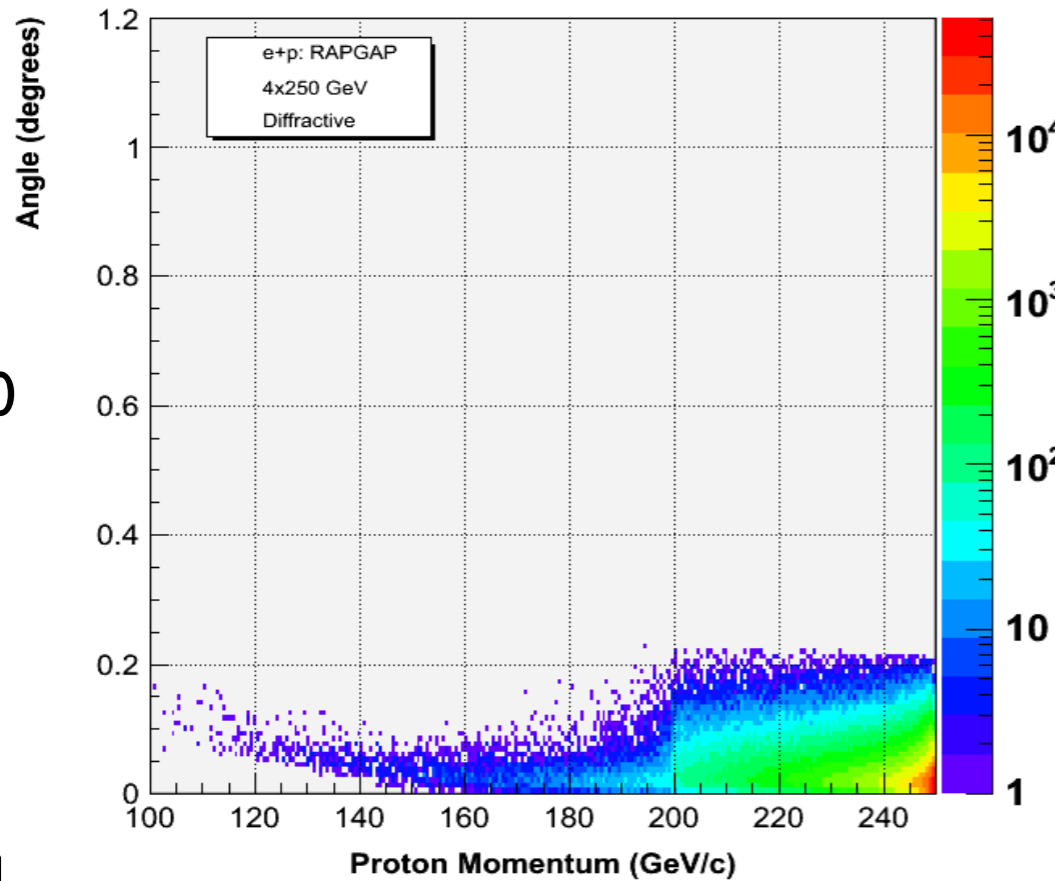
4x50



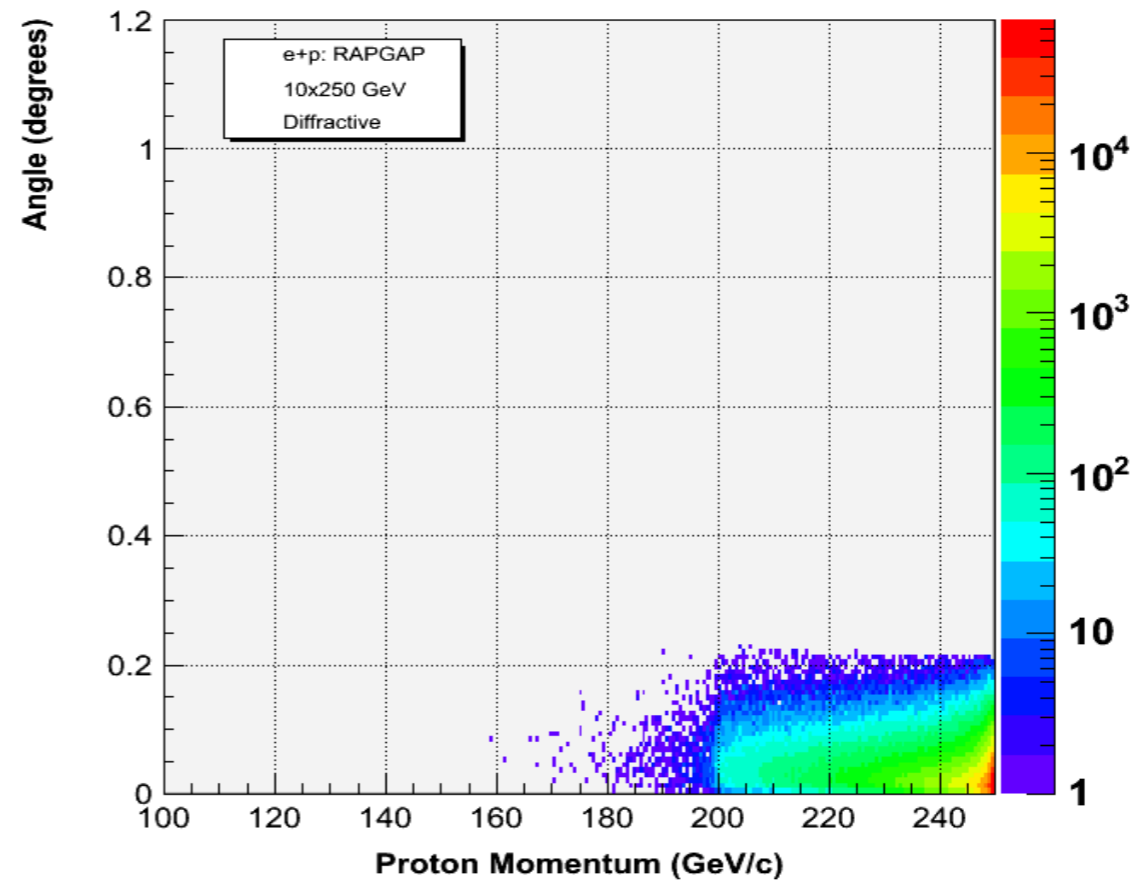
4x100



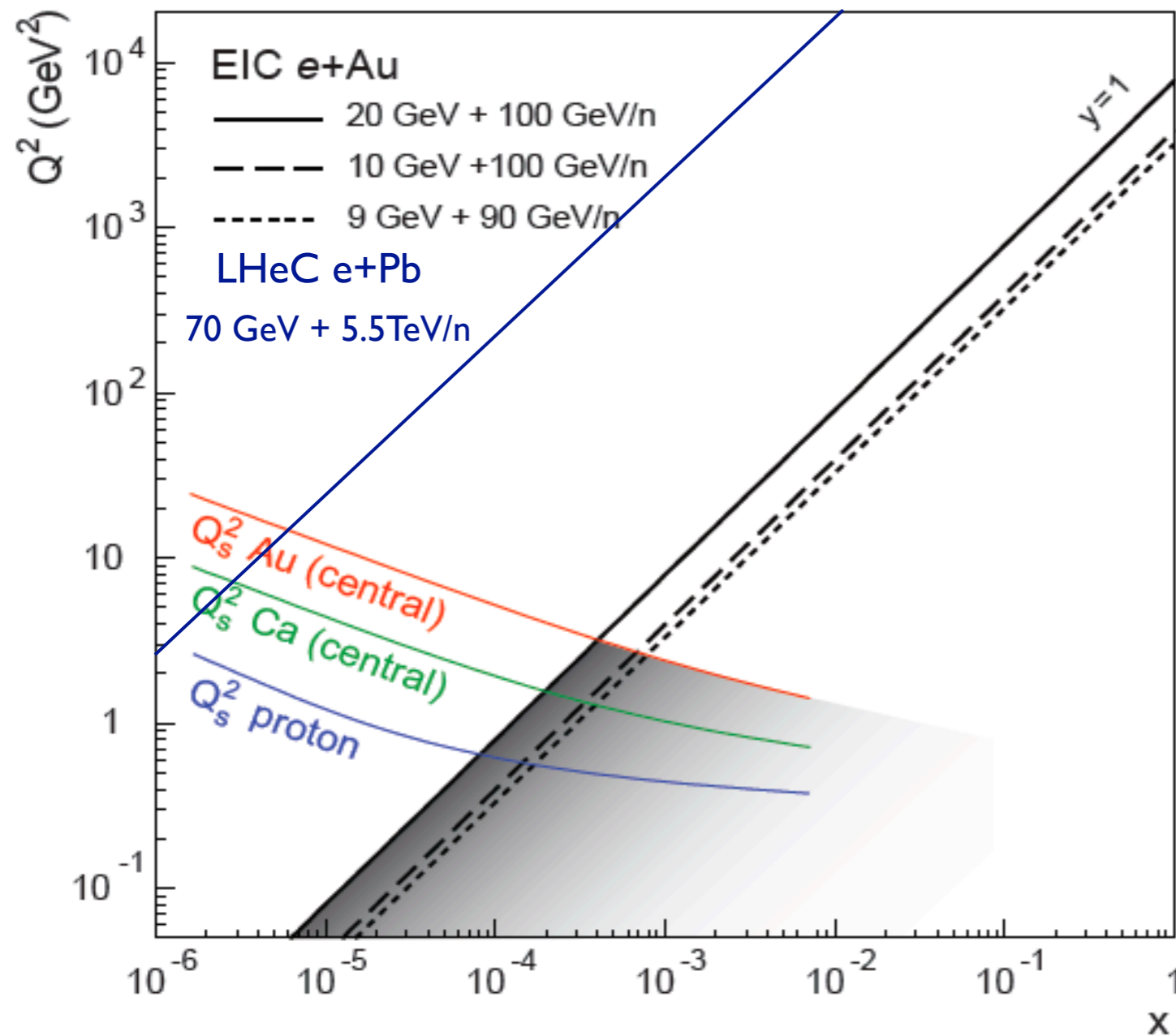
4x250



10x250

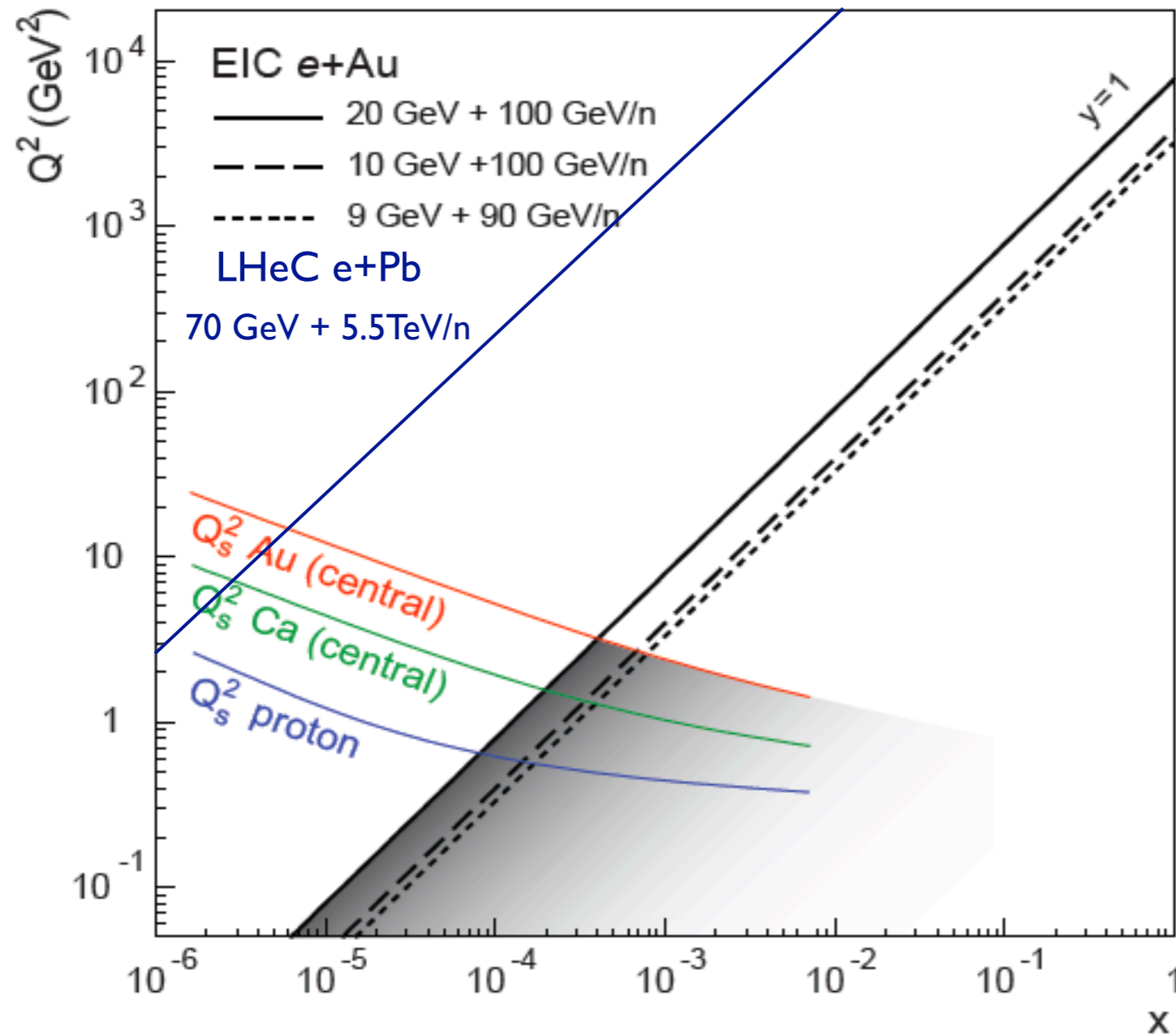


# Phase-space coverage of an e+p/h experiments



- Large coverage in  $x$ - $Q^2$  phase space
- Results from both collider and fixed-target experiments complement each other
- Onset of saturation possibly observed in collisions at HERA at very low- $x$
- calculations are difficult at small  $Q_s^2$  ( $< 2 \text{ GeV}^2$ )

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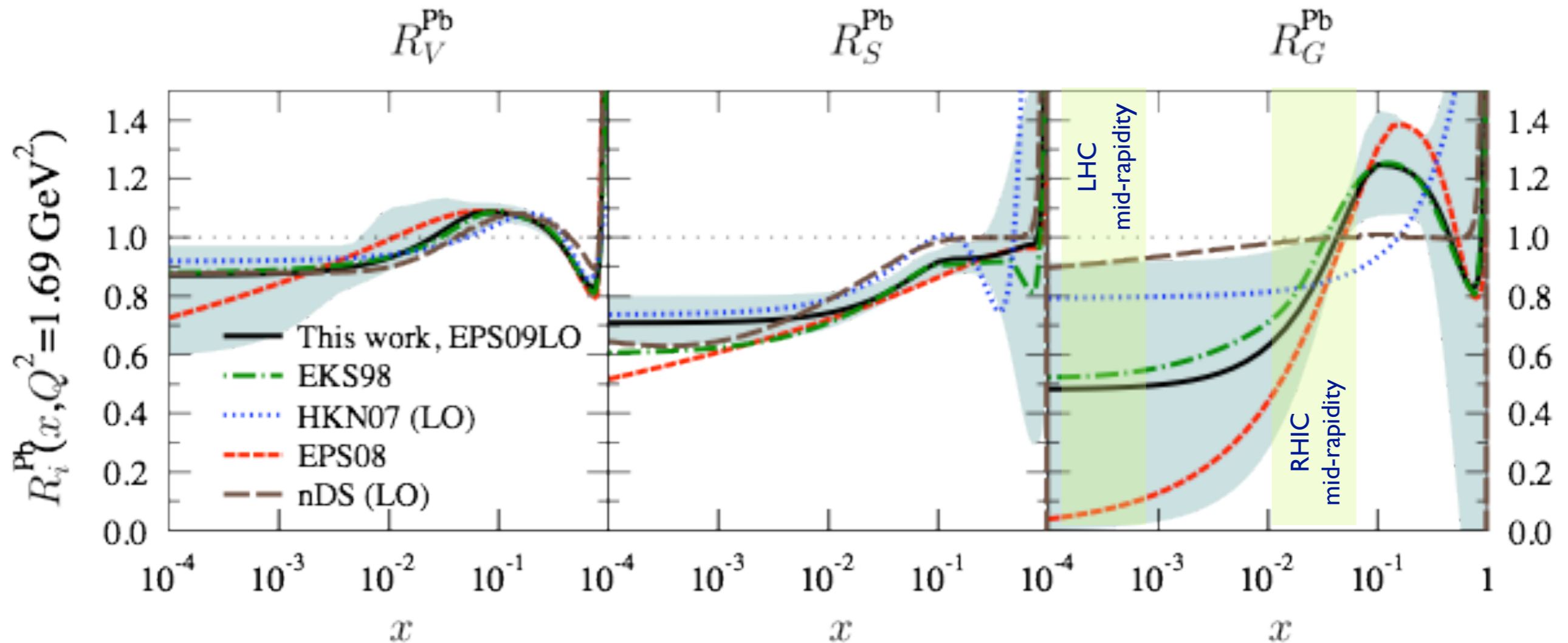


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## Electron Ion Collider:

- $\mathcal{L}(\text{EIC}) > 100 \times \mathcal{L}(\text{HERA})$
- Electrons
- $E_e = 3 - 20 \text{ GeV}$
- polarised
- Polarised  $p$

# How well are gluons understood in nuclei?



The distribution of valence and sea quarks are relatively well known in nuclei - theories agree well

Large discrepancies exist in the gluon distributions from models for mid-rapidity LHC and forward RHIC rapidities !!



# xDVMP MC Generator

- A MC generator for exclusive diffractive vector meson production
  - ➔ Thomas Ullrich's implementation of the b-Sat/b-CGC model for e+p and e+A
- Exclusive diffractive vector meson production is one of the most promising ways to study saturation in ep/eA
  - ➔ Naive:  $\sigma \sim G(x, Q^2)^2$
- Issues:
  - ➔ Experimentally difficult
    - ▶ rapidity gap, breakup,  $\int L dt$  needed ?
    - ▶ reconstruction of  $t$
    - ▶ detector requirements (resolution, acceptance)
    - ▶ sensitivity to physics (saturation)?
    - ▶ need to study in ep and eA

# Requirements for a new generator

- Simple, i.e. easy to use, manipulate and modify
  - ➔ single purpose:  $e p \rightarrow e' p' V$
  - ➔ write only the necessary core
  - ➔ reuse what is available (and accessible)
- Based on a model that is known to describe data well
  - ➔ Dipole model (works well at Hera)
- Extendable to eA
  - ➔ Dipole model does that
- Modern
  - ➔ C++, integrates with ROOT and other tools
- Output should follow standards as much as possible
- Useful for detector/acceptance studies as well as physics studies (e.g., sensitivity to  $xG(x, Q^2)$  etc. )

# Dipole Model (I)

Cross-section for production of final state VM:

$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} \left( \mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep} \right)^2 = \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \left( \frac{d\sigma_{qq}}{d^2\mathbf{b}} \right)^2 \right|^2$$

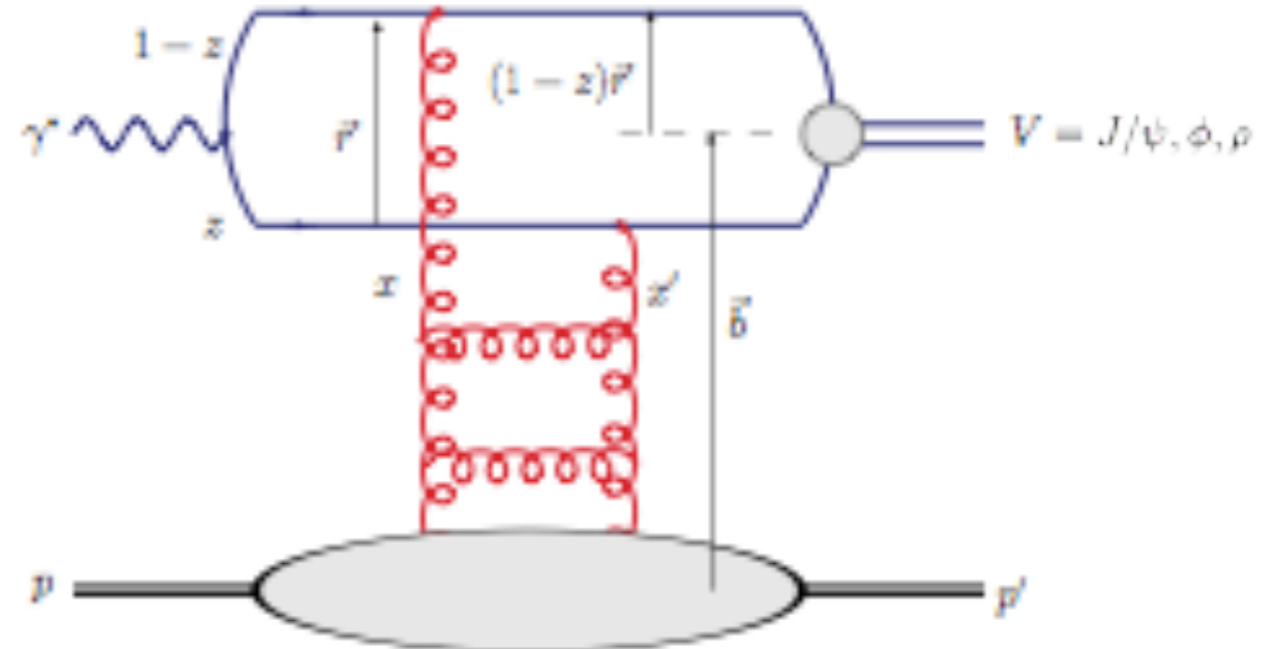
Amplitude

Overlap between photon and VM wave function

Dipole Cross-Section

Many dipole models on the market:

- Use : [H. Kowalski, L. Motyka, G. Watt, Phys. Rev. D74, 074016](#)
- Describes Hera data well
- has b-dependence
- Michael & TU have experience with it
- Henri is around to ask
- can be “easily” modified to do eA (via b-dependence)



# Dipole Model (II)

Cross-section for production of final state VM:

$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} \left| \mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep} \right|^2 = \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \left( \frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \right)^2 \right|^2$$

Overlap between  
photon and VM  
wave function

Dipole  
Cross-Section

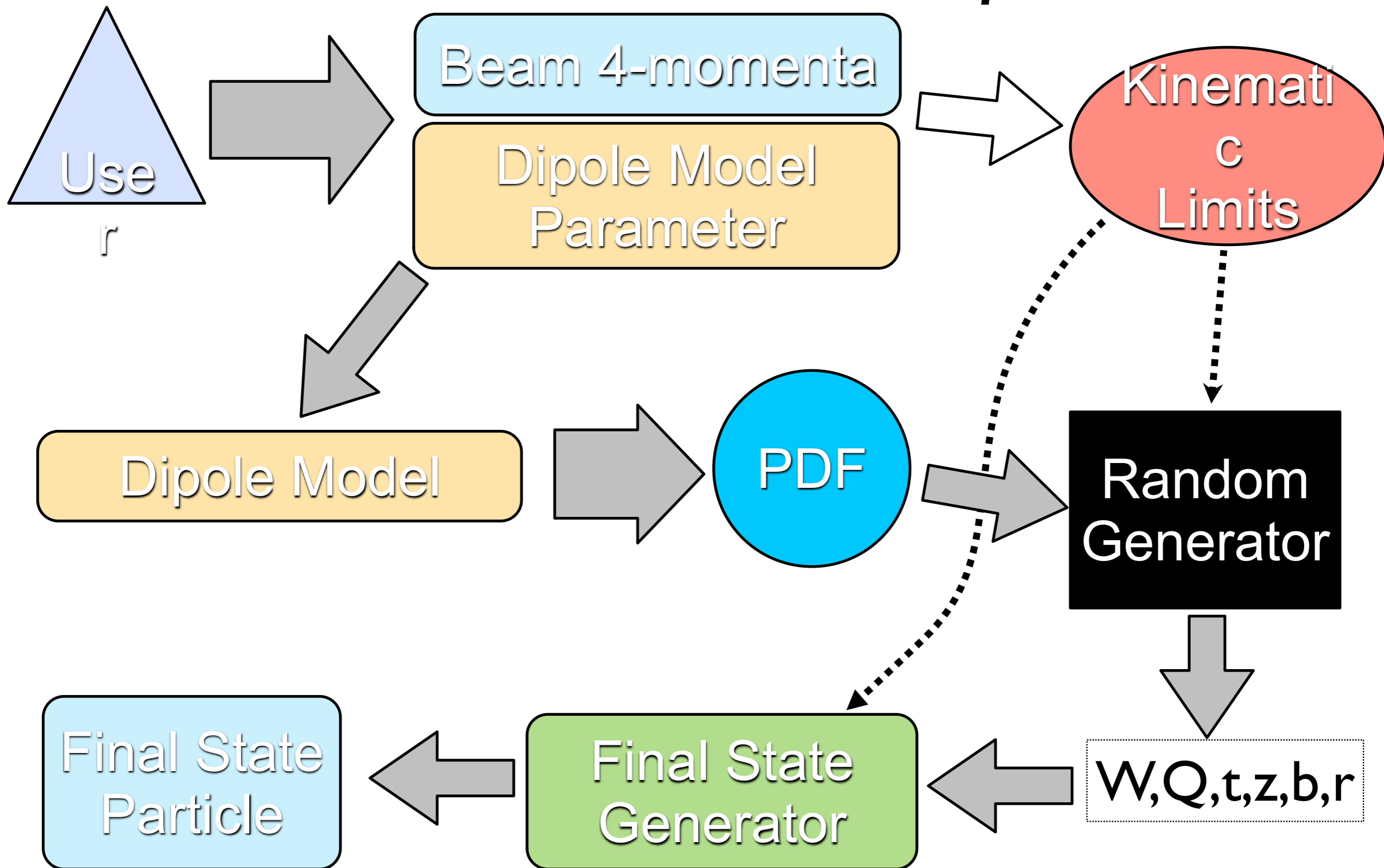
## Wave function:

- Boosted Gaussian
  - ➔ Forshaw, Sandapen, Shaw
- GausLC
  - ➔ Dosch, Gousset, Kulzinger, Pirner, Teaney, Kowalski
- Parameters tuned for HERA are available
- any improved wave function can be easily plugged in

## Dipole Cross-Section:

- b-Sat
  - ➔ uses DGLAP evolution from initial G(x, Q)
  - ➔ can be adapted for A (b-dependence)
- b-CGC
- Parameters tuned for HERA are available

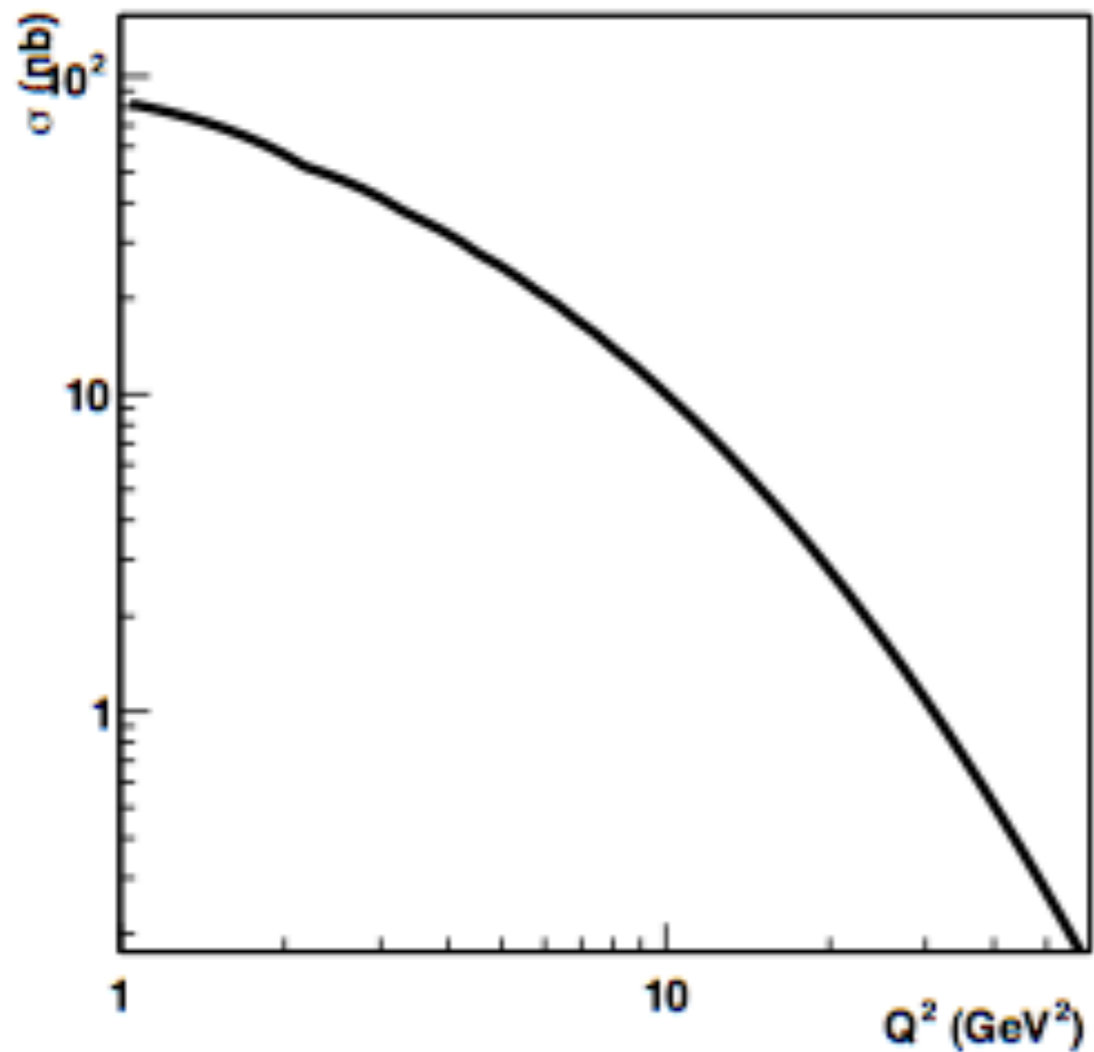
# Basic scheme behind *xdvmpGenerator*



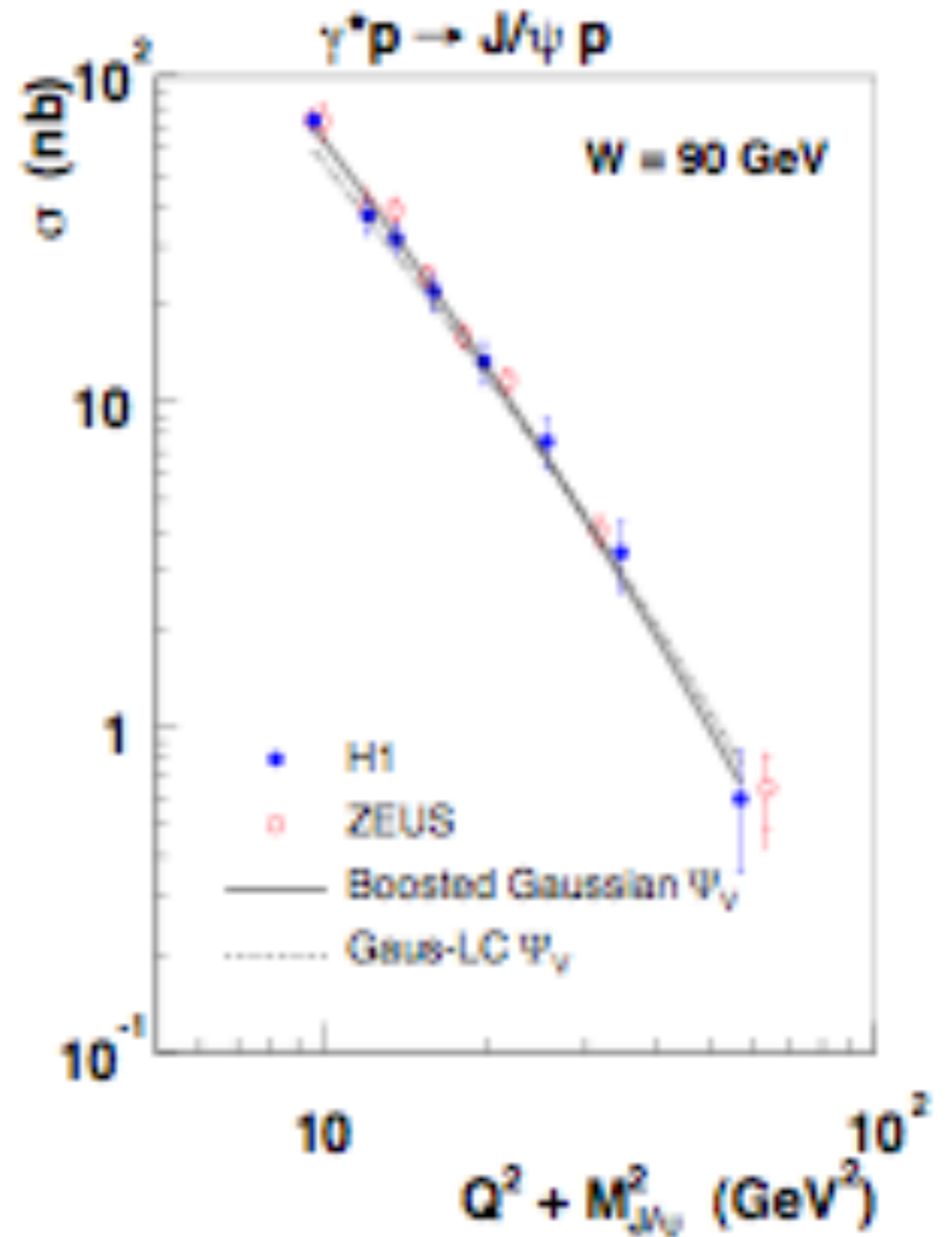
# Implementation

- Follow Pythia8 philosophy
  - ➔ main program to be provided by user
  - ➔ *xdvmpGenerator* is a class with simple methods
    - ▶ *init()*, *generateEvent()*, *printEventRecord()*, ...
    - ▶ event record in plain structure (*xdvmpEvent*)
    - ▶ setup through runcard (txt file) or programmatically
  - ➔ *xdvmpGenerator* uses many other classes and functions
    - ▶ class *xdvmpDipoleModel* (dipole model implementation)
      - *alphaStrong.cpp* (fcts to calculate  $\alpha_s$  - adapted from MRST, rewritten in C++)
      - *laguerre.c*, *dglap.c* (for DGLAP from F. Gelis)
    - ▶ class *xdvmpFinalStateGenerator* (generate final state particles from  $x, Q^2, s, t$ )
    - ▶ class *xdvmpSettings* (handle parameter & runcard parsing)
  - ➔ Total ~ 4200 lines of code only (requires only GSL, ROOT libs)

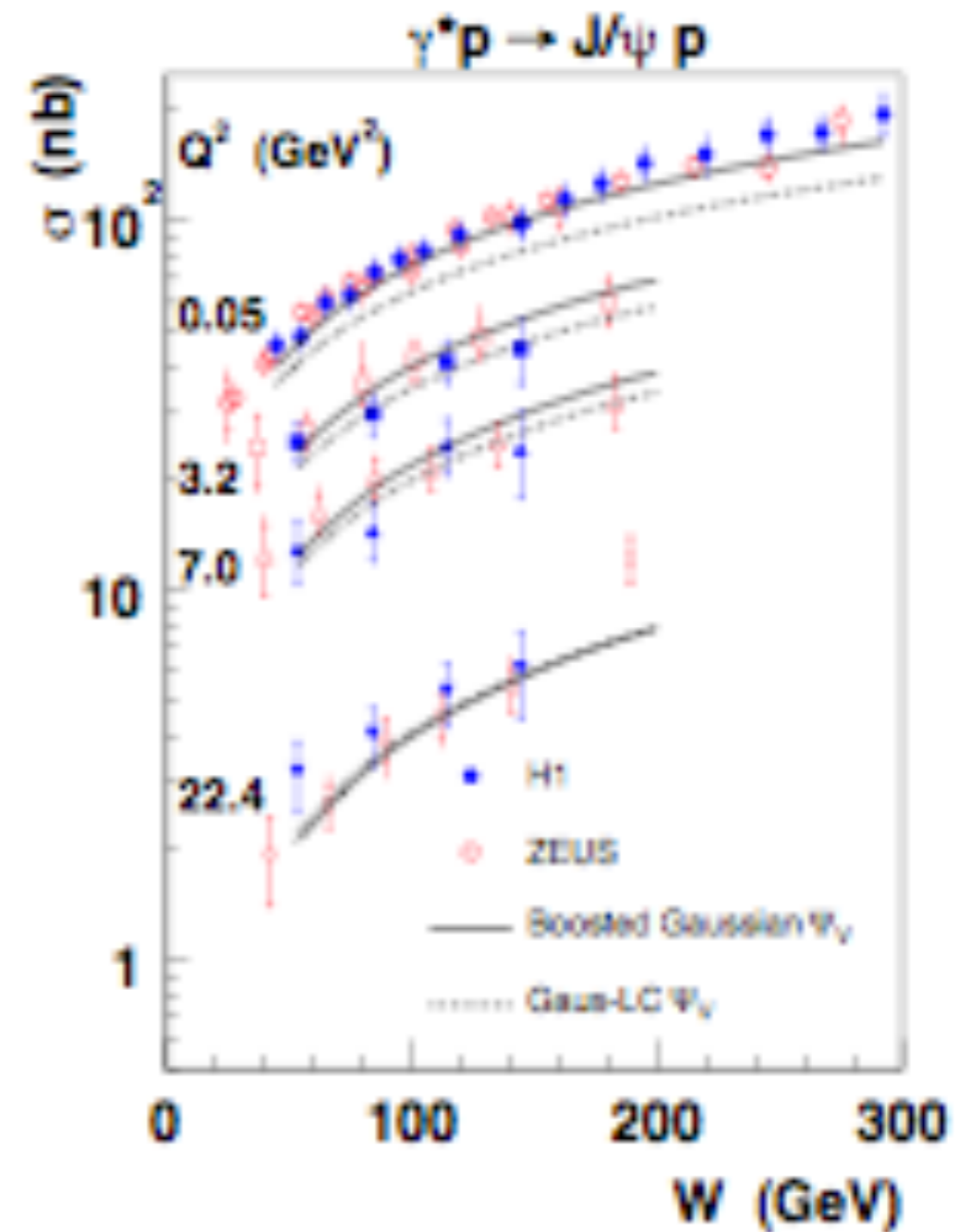
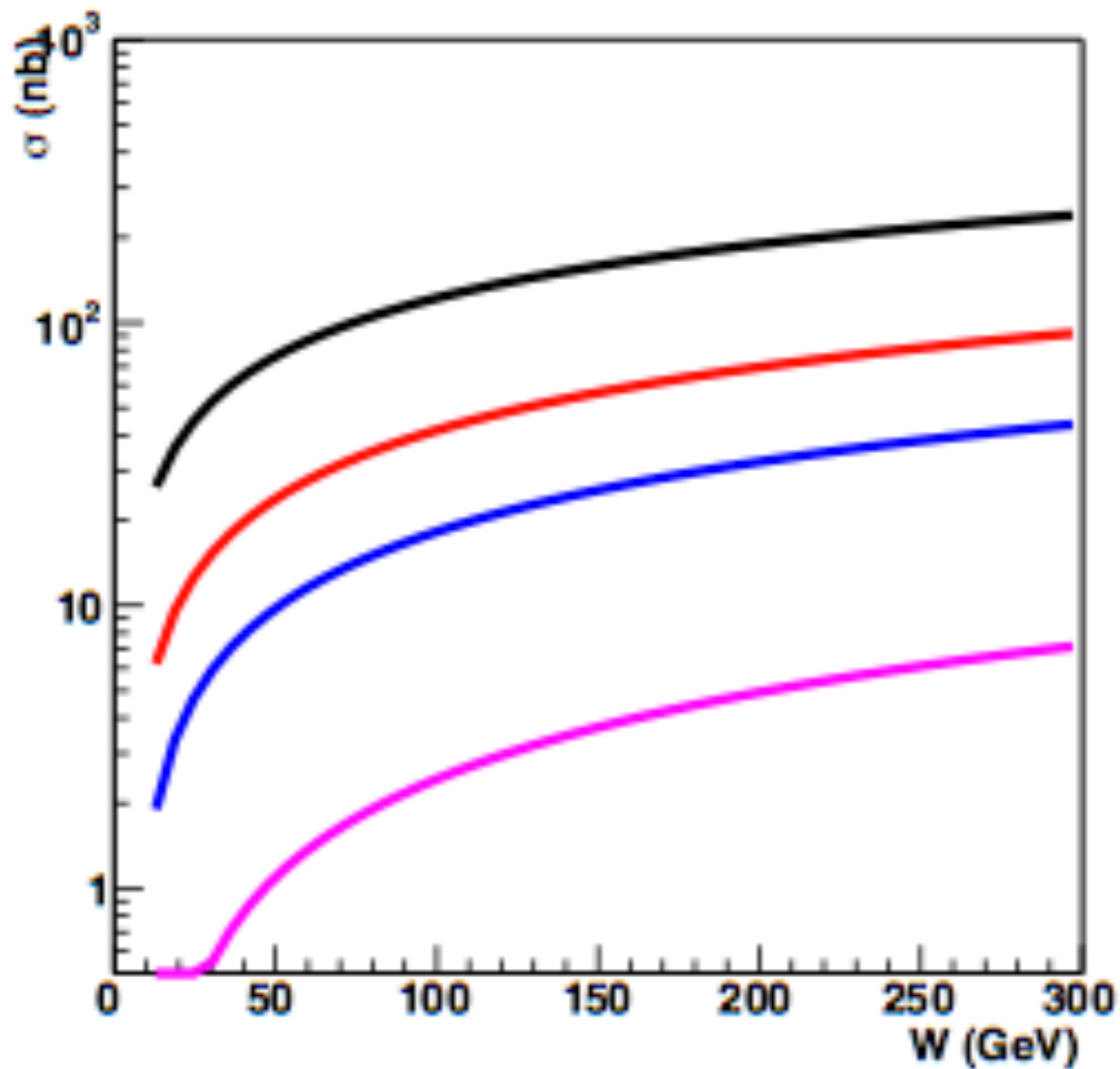
# Dipole Model Test (I)



$W = 90$  GeV



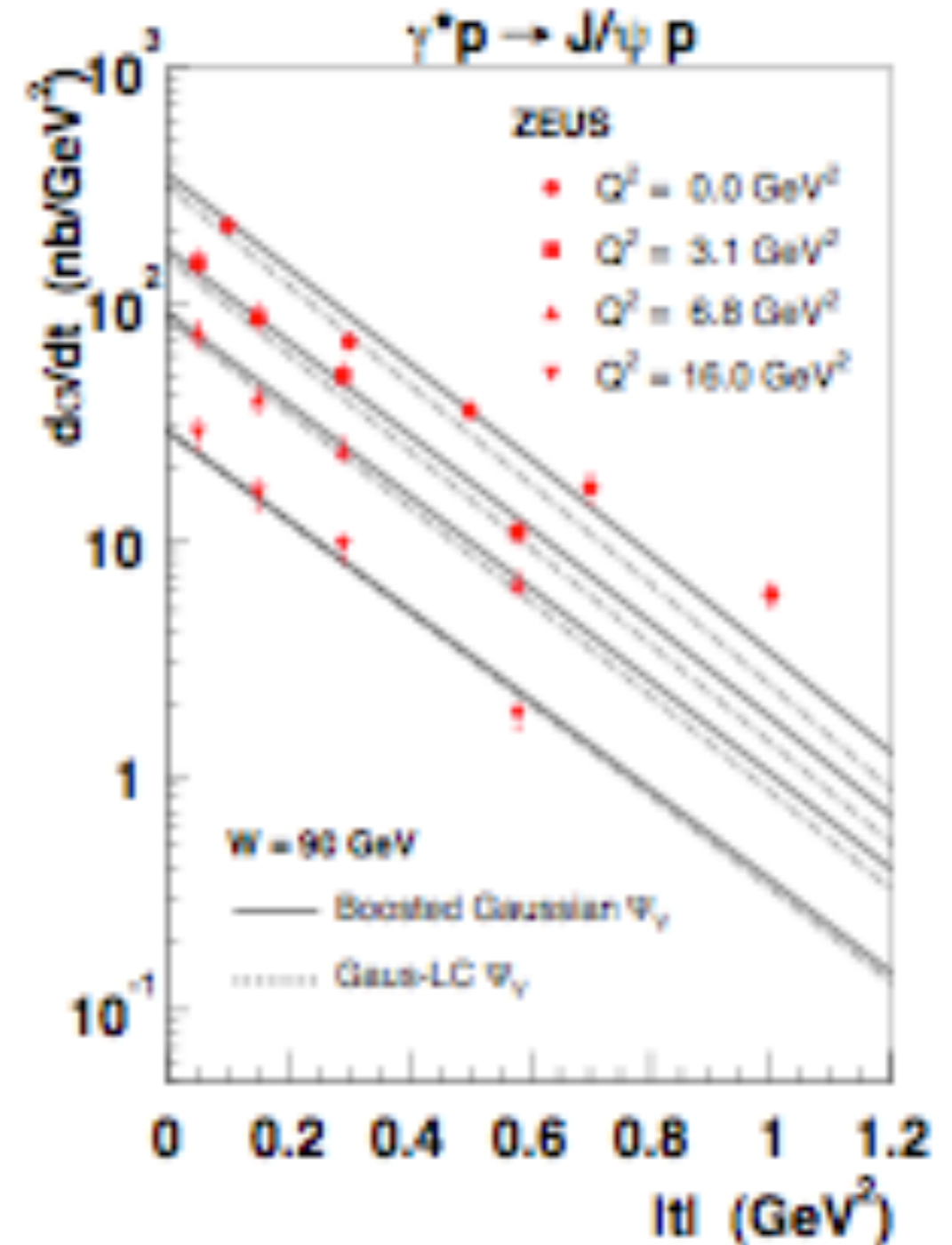
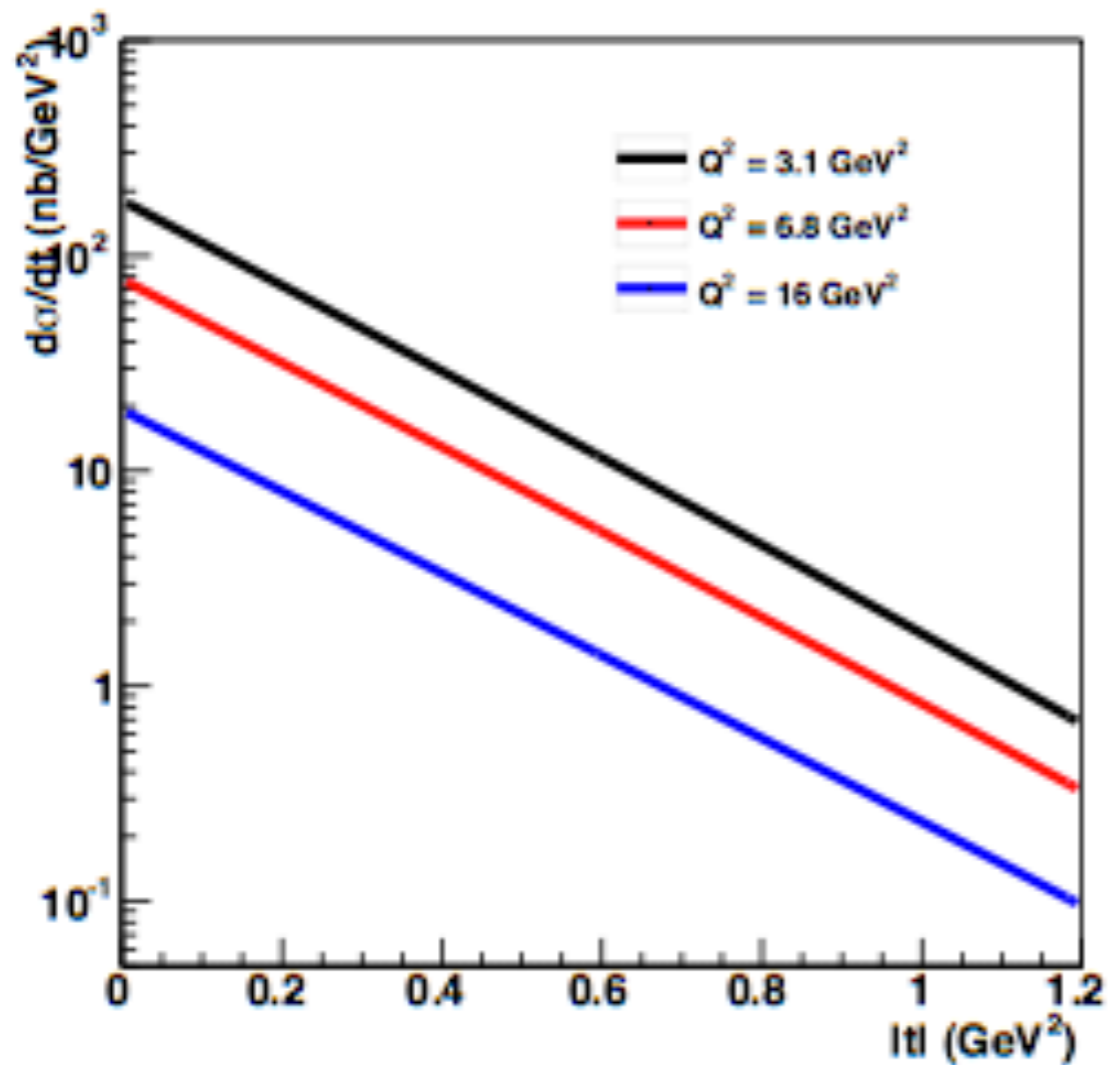
# Dipole Model Test (II)



$Q^2 = 0.5, 3.2, 7.0, 22.4 \text{ GeV}^2$



# Dipole Model Test (III)



# xDVMP status



## xdvmp Documentation

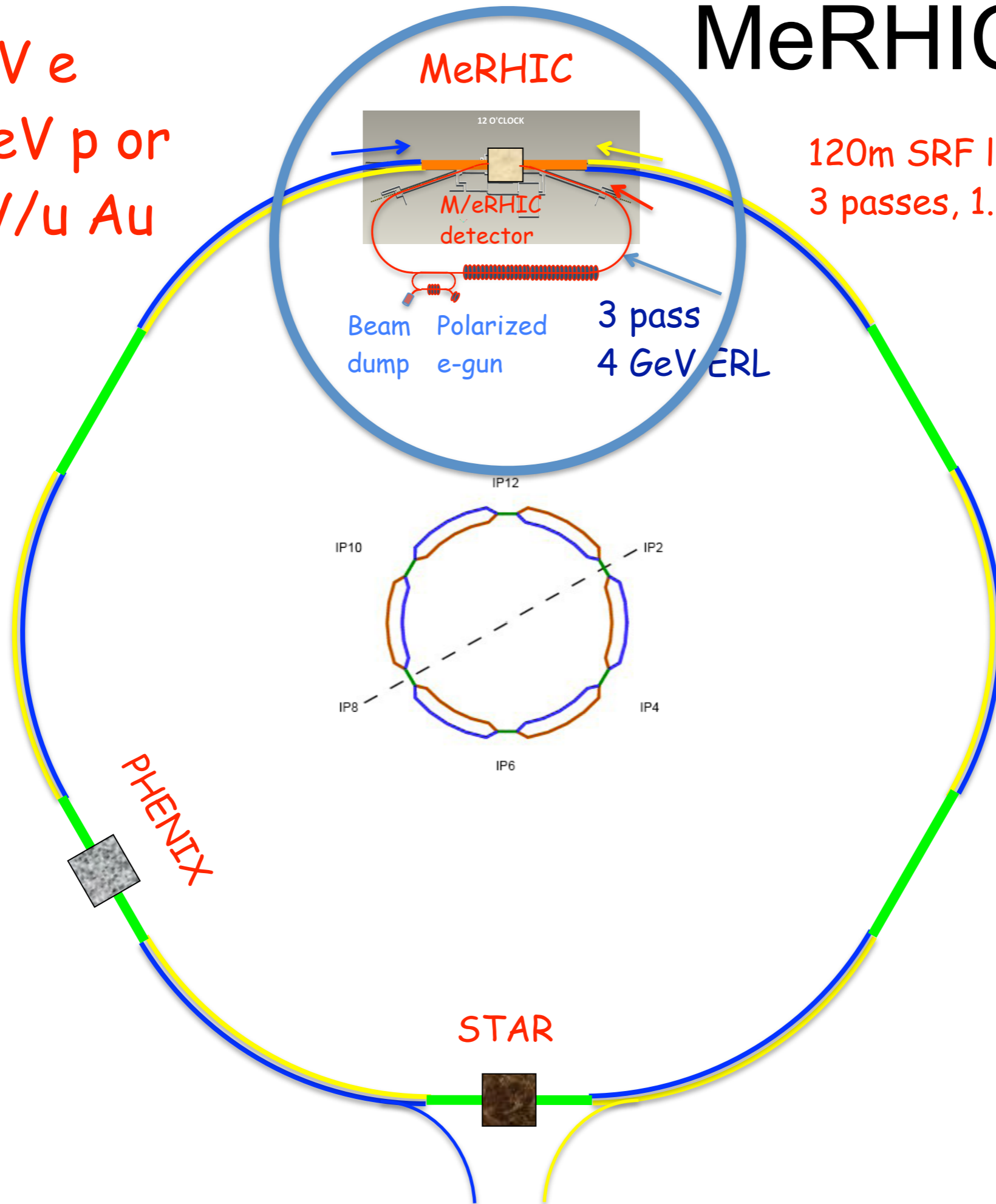
Getting started	xdvmp Basics	API Reference
<ul style="list-style-type: none"><li>• <a href="#">Overview</a></li><li>• <a href="#">Downloading</a></li><li>• <a href="#">Installing xdvmp</a></li></ul>	<ul style="list-style-type: none"><li>• <a href="#">Event Generator</a></li><li>• <a href="#">Example program: xdvmpMain</a></li></ul>	<ul style="list-style-type: none"><li>• <a href="#">Overview</a></li><li>• <a href="#">class xdvmpGenerator</a></li><li>• <a href="#">class xdvmpSettings</a></li><li>• <a href="#">class xdvmpDipoleModel</a></li><li>• <a href="#">class xdvmpFinalStateGenerator</a></li><li>• <a href="#">class xdvmpEvent (Event Record)</a></li><li>• <a href="#">Runcard Reference</a></li></ul>
The Physics Behind the Model	What's New?	Troubleshooting
<ul style="list-style-type: none"><li>• <a href="#">The Dipole Model</a></li><li>• <a href="#">Generation of final state particles</a></li><li>• <a href="#">References &amp; Credits</a></li></ul>		<ul style="list-style-type: none"><li>• <a href="#">Known problems</a></li><li>• <a href="#">To-do list</a></li></ul>

Last Update: April 6, 20

Some final testing required before it is released into the wild ....

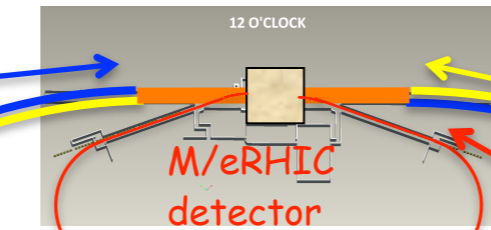
# MeRHIC at BNL

4 GeV e  
x 250 GeV p or  
100 GeV/u Au



MeRHIC

120m SRF linac  
3 passes, 1.3 GeV/pass



Beam dump  
Polarized e-gun  
3 pass  
4 GeV ERL

IP12

IP10

IP2

IP8

IP4

IP6

PHENIX

STAR

# Detector requirements from physics

- e+p physics

- ➔ Need the same detector for inclusive ( $ep \rightarrow e'X$ ), semi-inclusive ( $ep \rightarrow e'X + \text{hadrons}$ ) and exclusive ( $ep \rightarrow e'p+\pi$ ) reactions

- ▶ Need to have a large acceptance (*both* mid- and forward-rapidity)

- ▶ Crucial to have particle identification

- e,  $\pi$ , K, p, n over wide momentum range and scattering angles

- excellent secondary vertex resolution (charm)

- ▶ small systematic uncertainty for e/p polarisation measurements

- ▶ small systematic uncertainty for luminosity measurements

- e+A physics

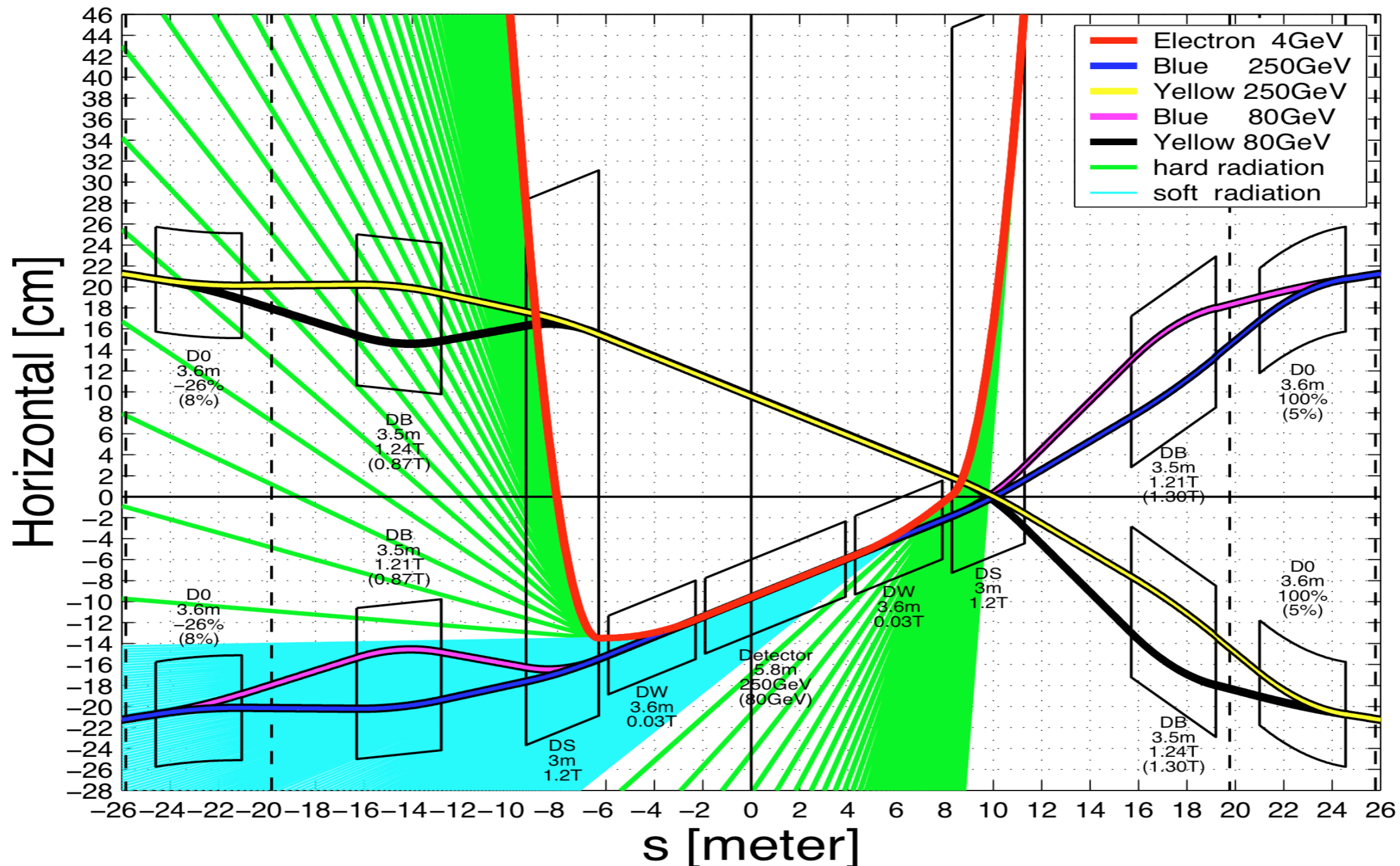
- ➔ most requirements similar to e+p guidelines

- ➔ additional complication arises from the need to tag the struck nucleus in exclusive and diffractive reactions

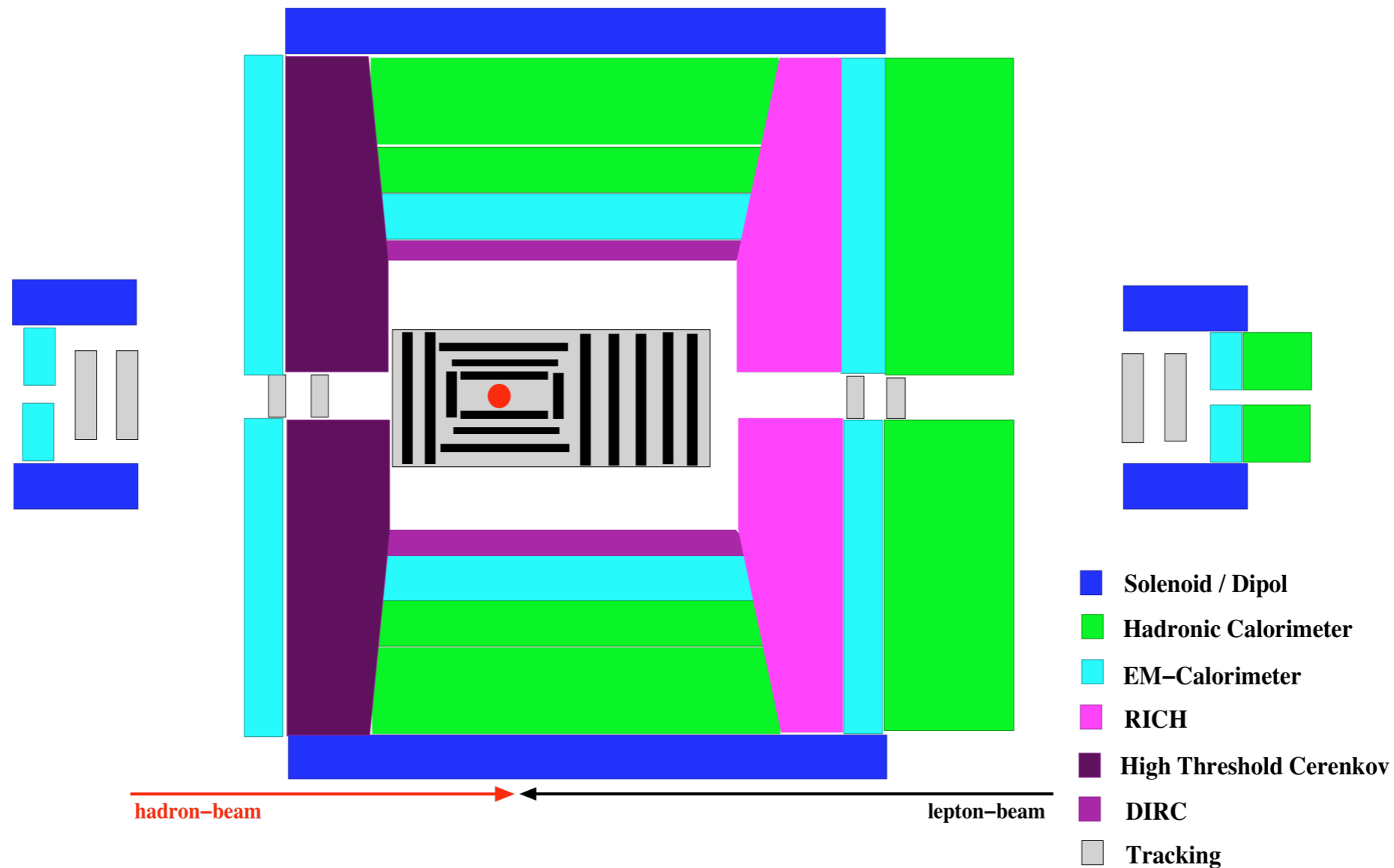
- Also, important to have the same detector for all energies

# Latest IR Design for MeRHIC at IP2

- No DX magnet
- No synchrotron shielding included
- Height of beam from floor ~ 6 feet
- Allows p and A decay product tagging

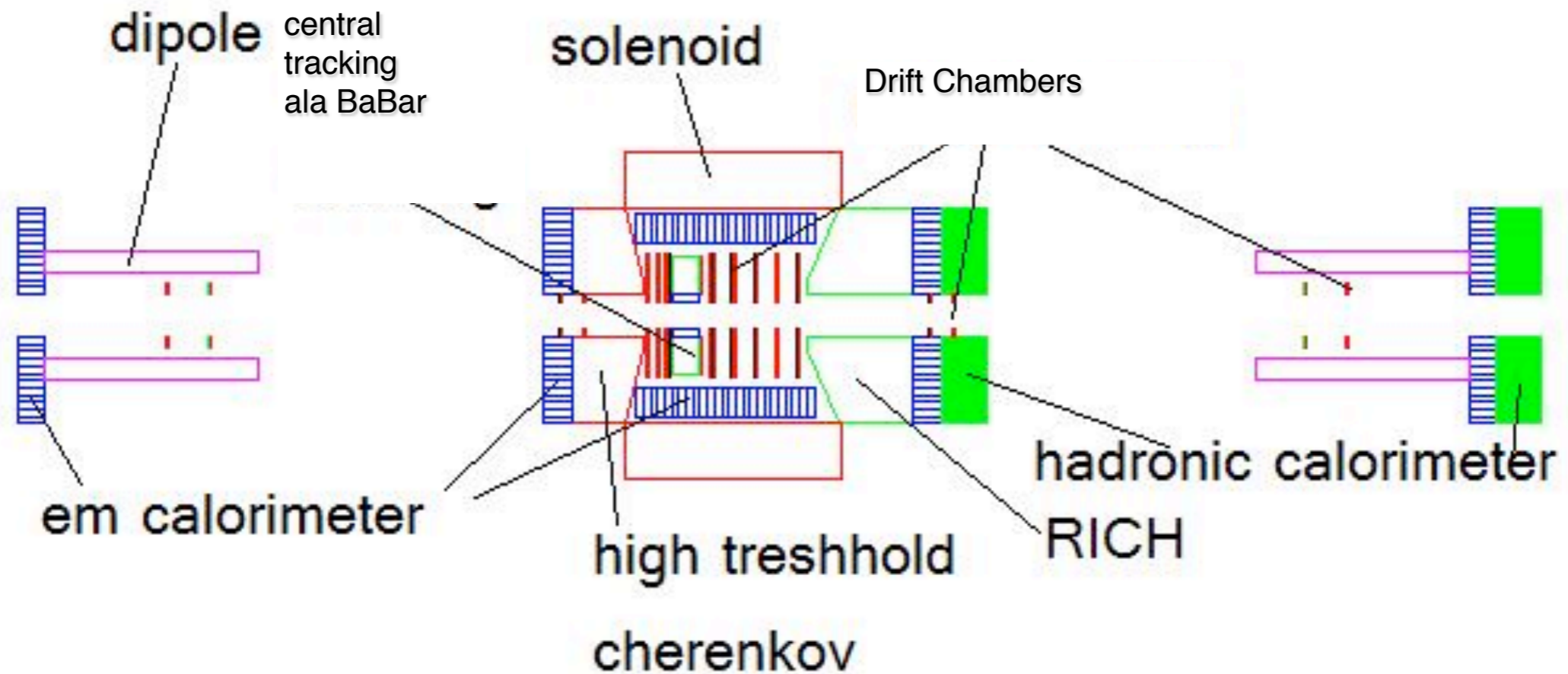


# First attempt at detector design



- Dipoles need to have good forward momentum resolution
  - ➔ Solenoid has no magnetic field for  $r \rightarrow 0$
- RICH, DIRC for hadron pid
- High threshold Cherenkov  $\rightarrow$  fast trigger for scattered lepton
- Radiation length very critical  $\rightarrow$  low lepton energies

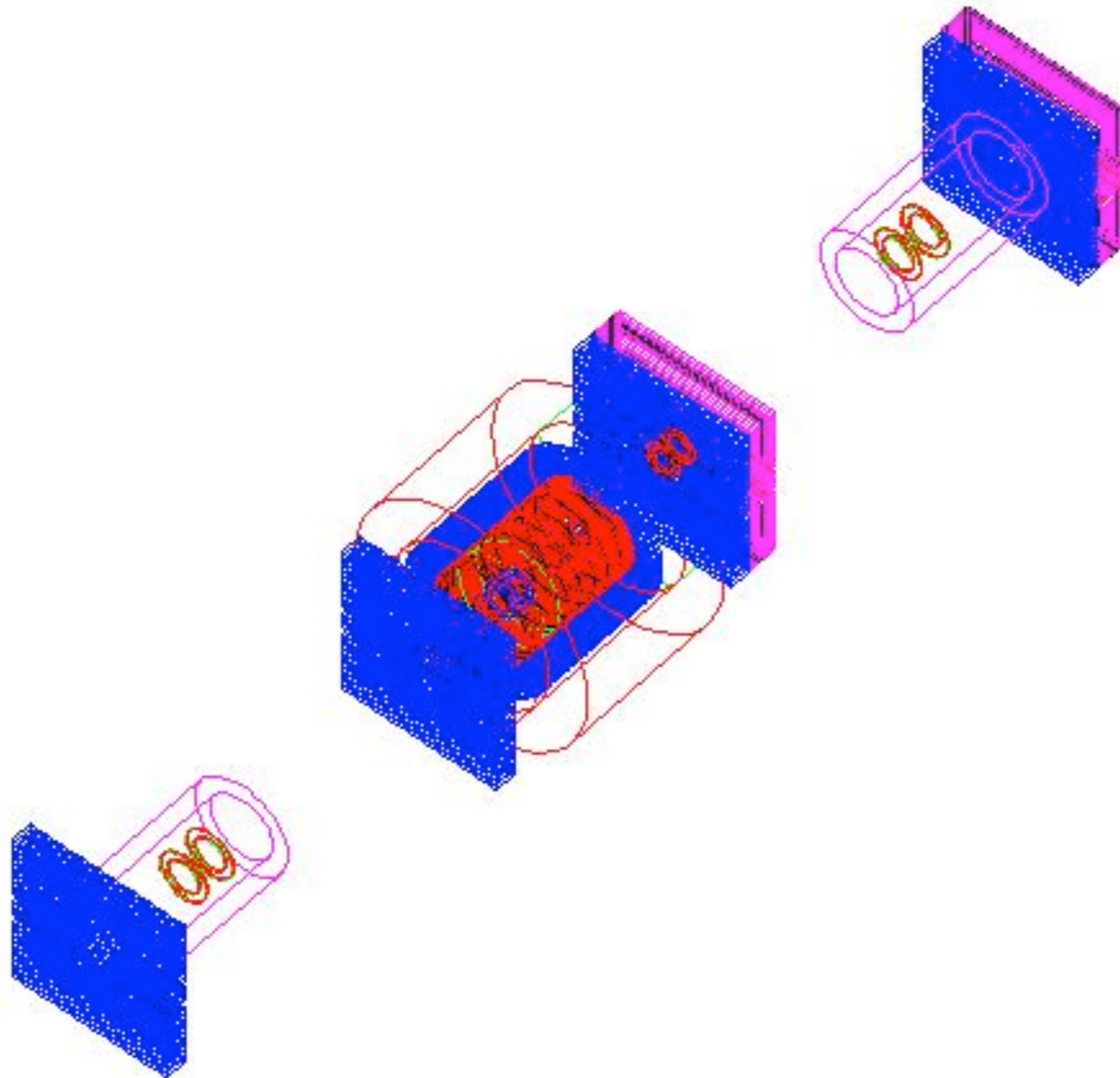
# MeRHIC Detector in Geant 3



DIRC is present but not seen  
due to position of cut

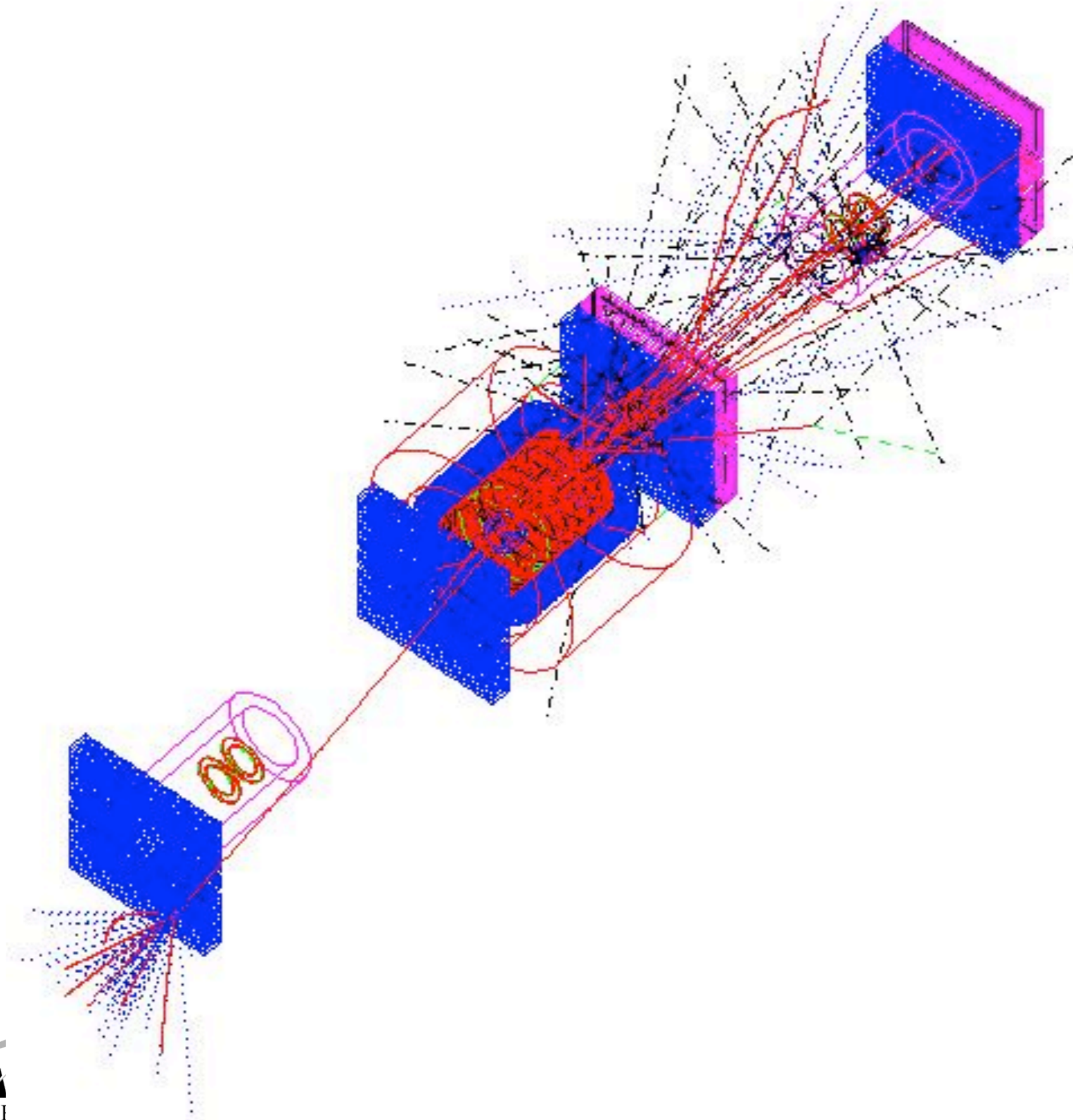
- Note - no hadronic barrel calorimeter due to height restrictions at IP2

# MeRHIC detector in Geant 3

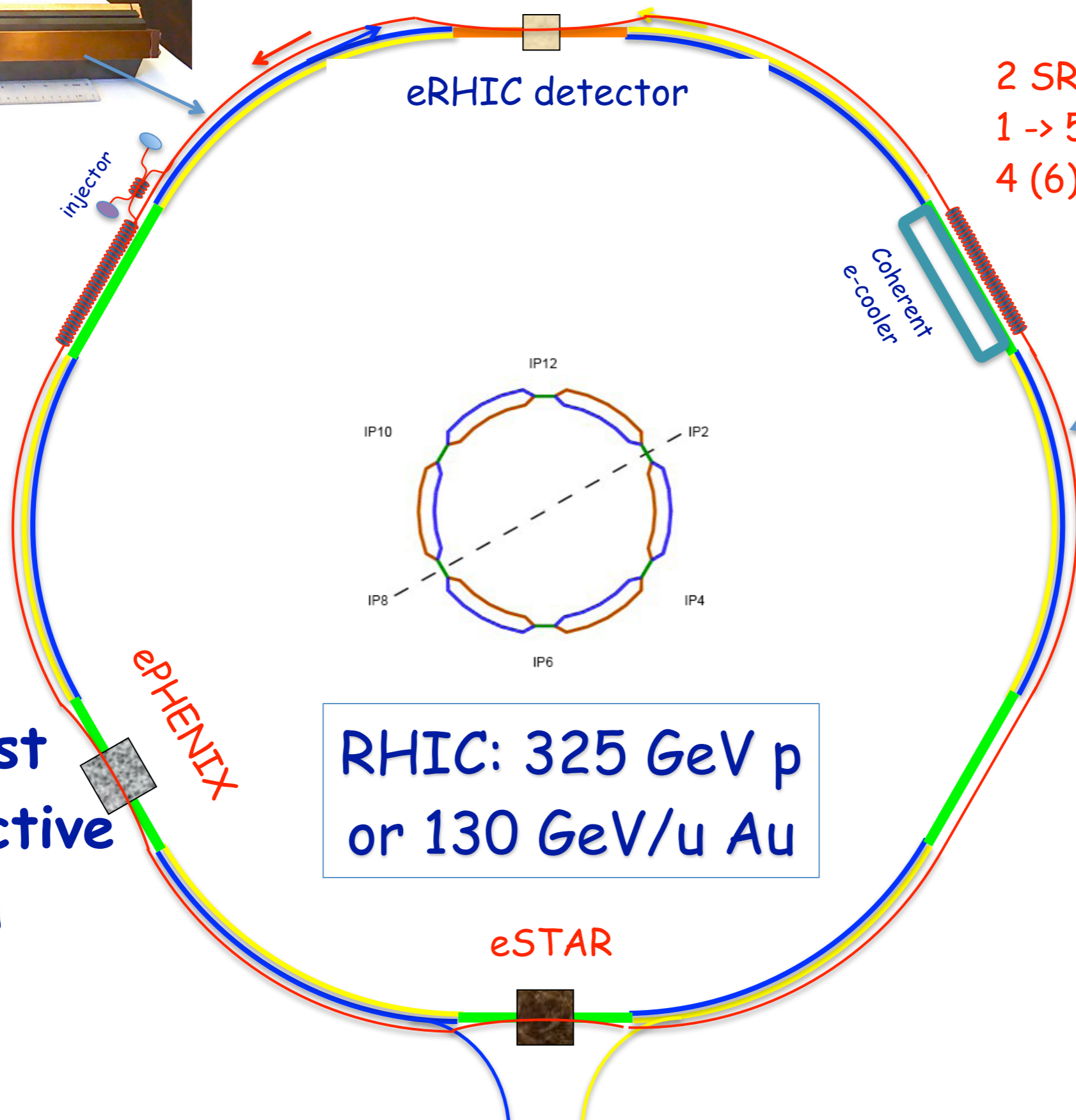
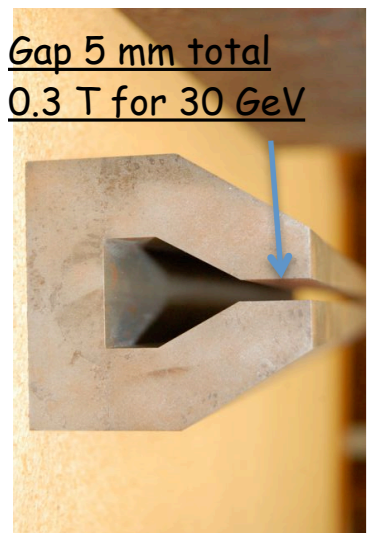




# MeRHIC detector in Geant 3



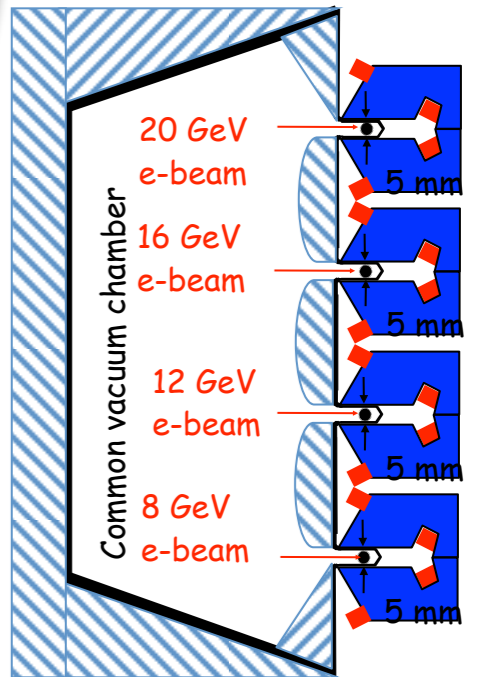
# Staging all-in tunnel eRHIC: energy of electron beam is increasing from 5 GeV to 30 GeV by building-up the linacs



2 SRF linac  
1 -> 5 GeV per pass  
4 (6) passes

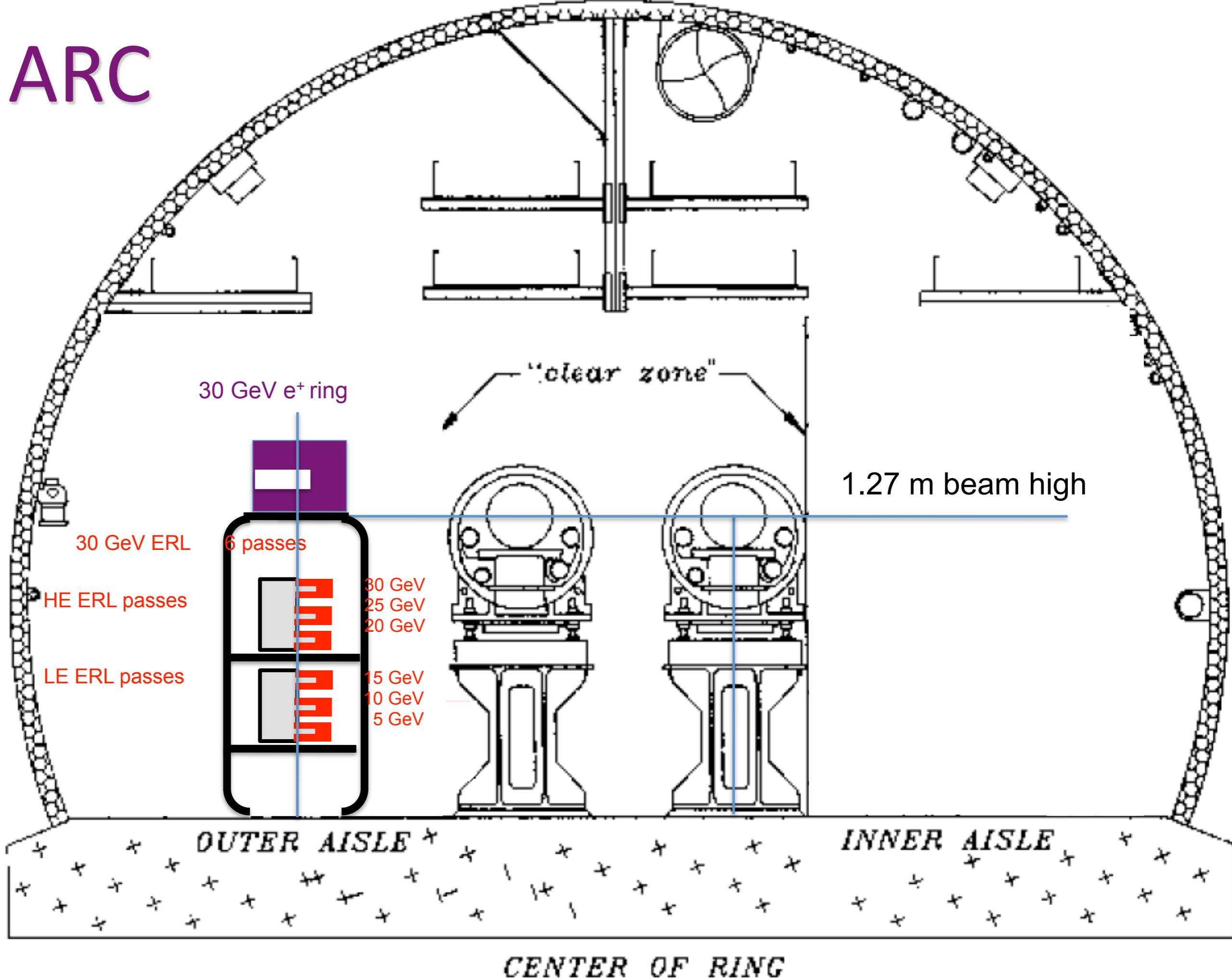
4 to 6 vertically separated recirculating passes. # of passes will be chosen to optimize eRHIC cost

RHIC: 325 GeV p  
or 130 GeV/u Au



The most cost effective design

# ARC



# Incorporating eSTAR and ePHENIX

- **Without changing DX-D0 both the energy and luminosity will be low in electron-hadron collisions**
- **Parallel operation of hadron-hadron and electron-hadron collisions does not allow cooling of hadron beam, hence 10-fold lower luminosity for e-p and e-A**
- **Sequential operation of RHIC as a hadron collider and as an electron-hadron collider allows to have both full energy and full luminosities in all modes of operation, including coherent electron cooling**
- **CeC would provide 10-fold increases in e-p and e-A luminosities and 6-fold increase in polarized p-p luminosity**
- **We have designs of two IR: low-x ( $L \sim 3 \cdot 10^{33}$ ) and high-lumi ( $L \sim 2 \cdot 10^{34}$ )**
- **We suggest using crossing angle and crab-cavities to have identical energy-independent geometry of IRs and no synchrotron radiation in detectors**

# STAR: A Correlation Machine

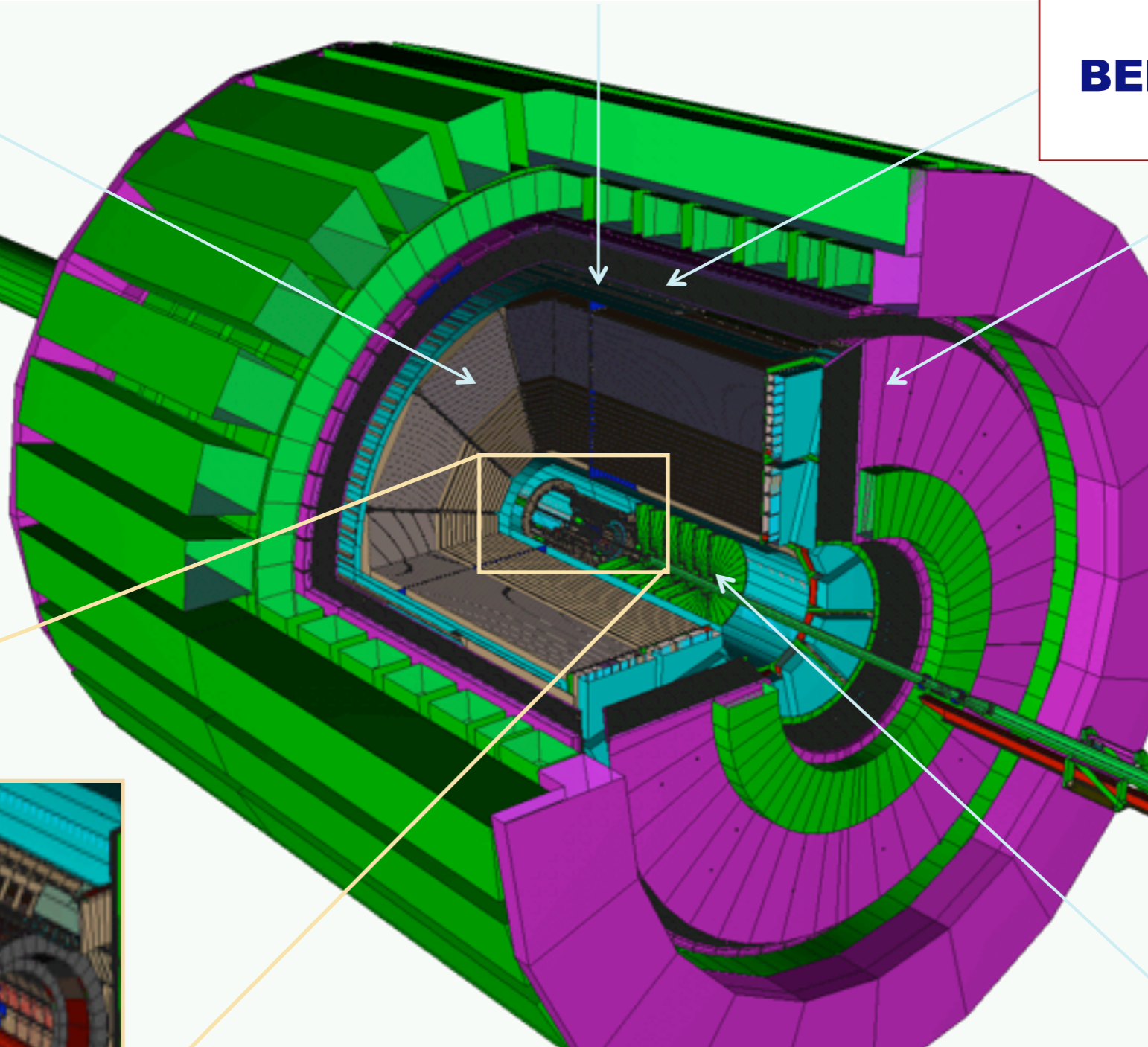
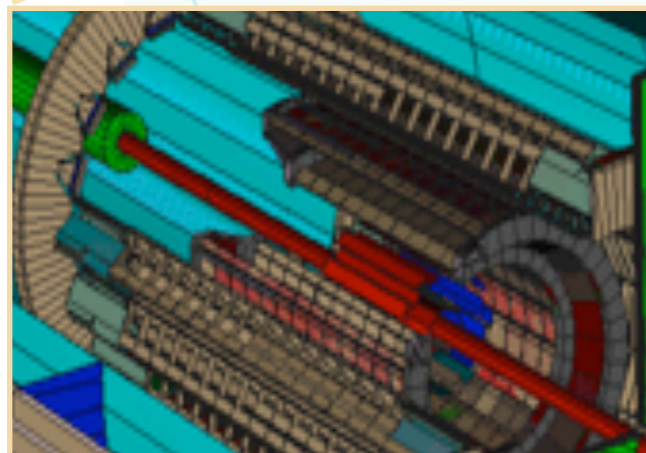
**Tracking: TPC**

**Particle ID: TOF**

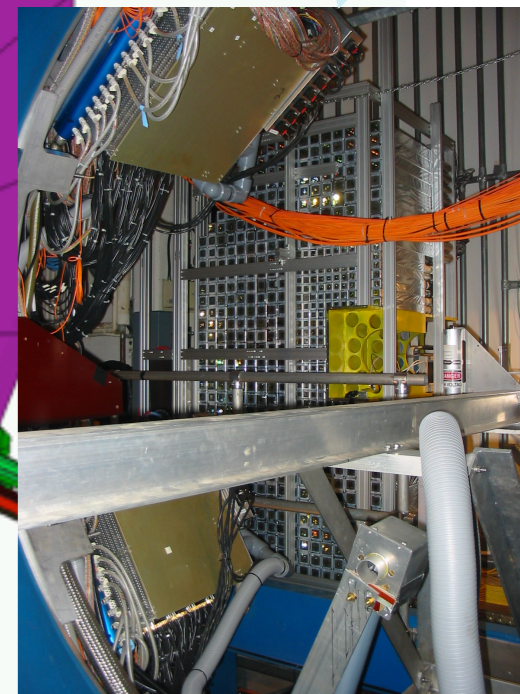
**Electromagnetic  
Calorimetry:  
BEMC+EEMC+FMS  
( $-1 \leq \eta \leq 4$ )**

**Upgrades:  
Muon Tracking  
Detector  
HLT**

**Heavy Flavor  
Tracker (2013)**



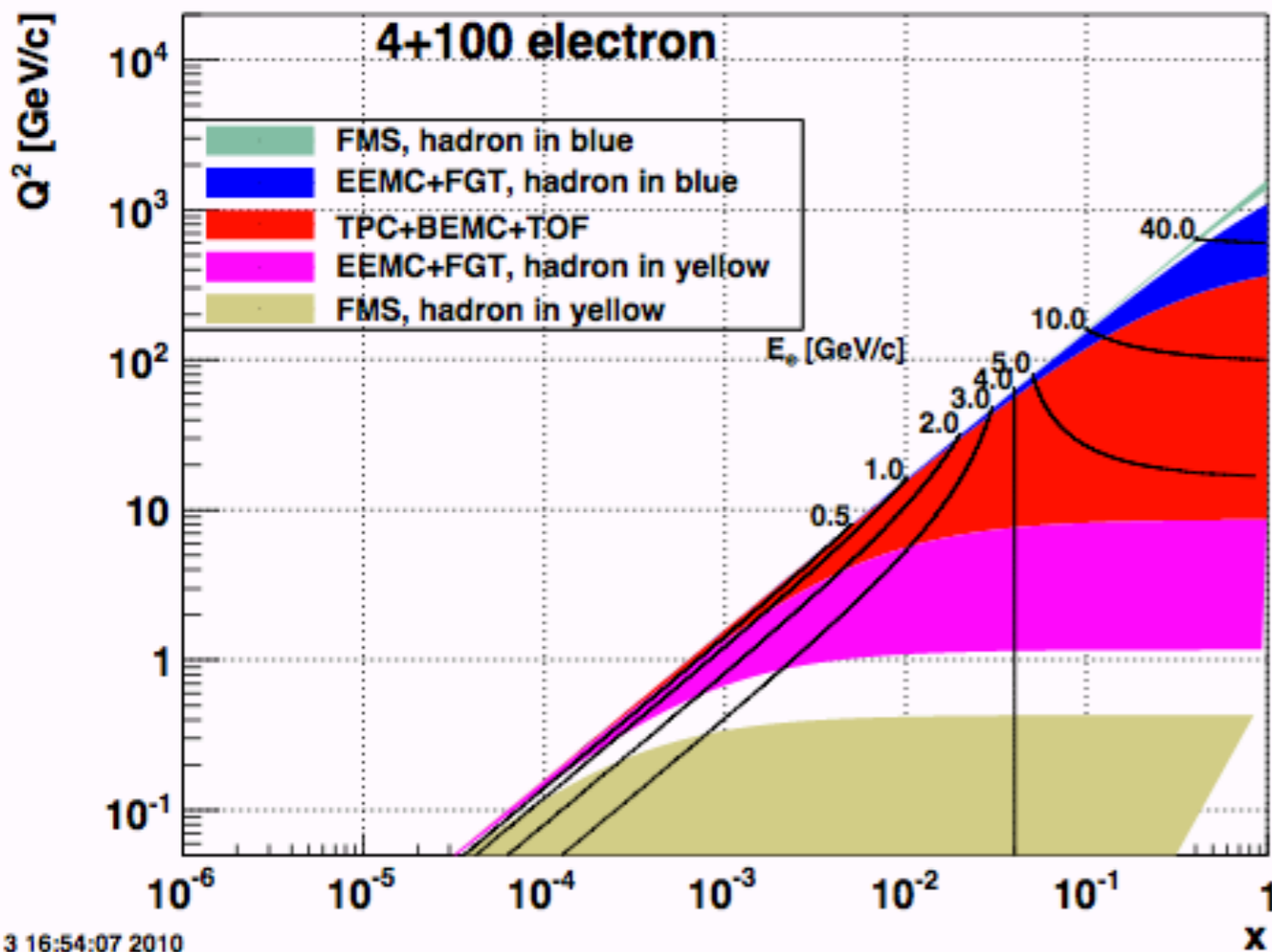
*Full azimuthal particle identification  
over a broad range in pseudorapidity*



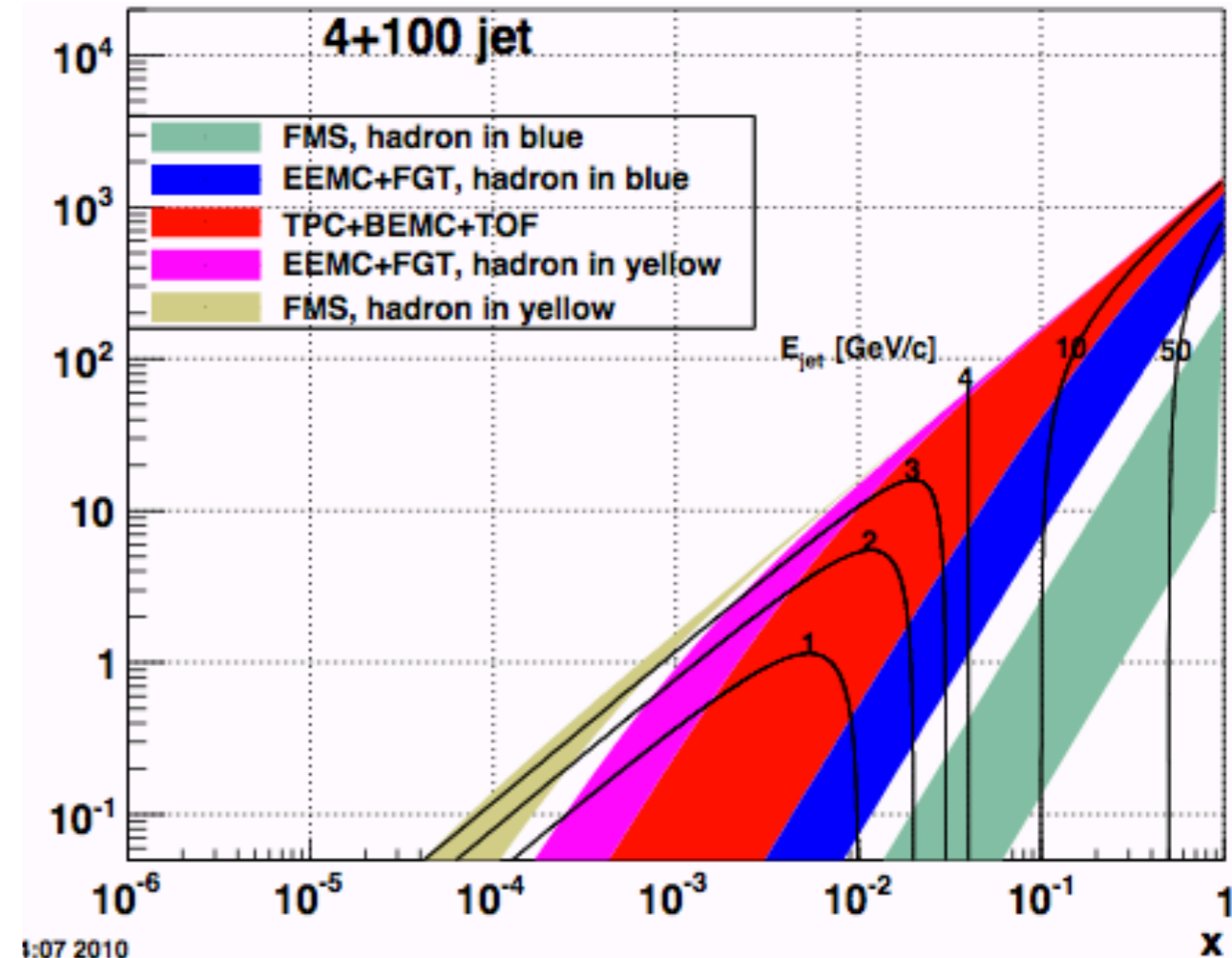
**Forward Gem  
Tracker  
(2011)**

# Kinematics at 4+100

Scattered electron



Scattered jet



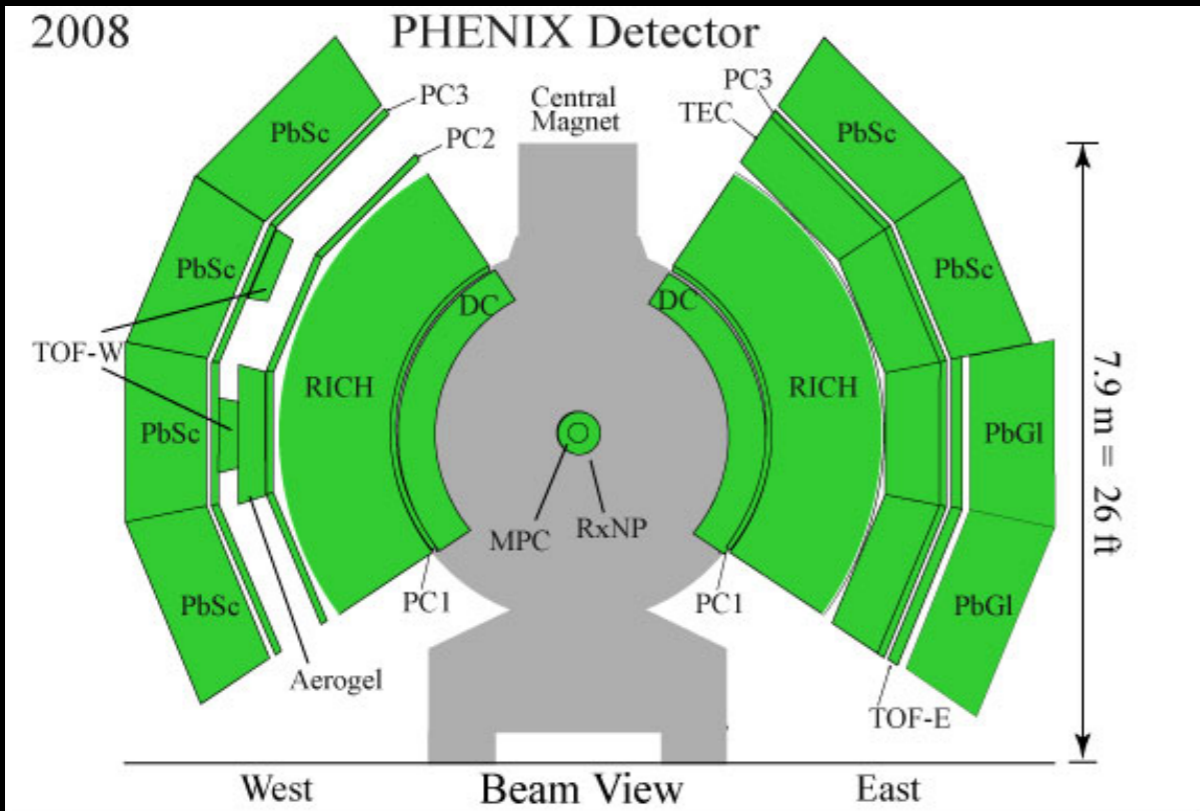
4+100 open kinematics: scatters the electron and jet to mid-rapidity

Forward region (FMS): Electron either  $Q^2 < 1$  GeV, or very high  $x$  and  $Q^2$

Jet either very soft or very hard

Note: current thinking has hadron in the blue beam: optimized for high  $x$  and  $Q^2$

# Current PHENIX Detector at RHIC



MPC

$$3.1 < |\eta| < 3.9$$

$$2.5^\circ < \Theta < 5.2^\circ$$

Muon Arms

$$1.2 < |\eta| < 2.4$$

South:

$$12^\circ < \Theta < 37^\circ$$

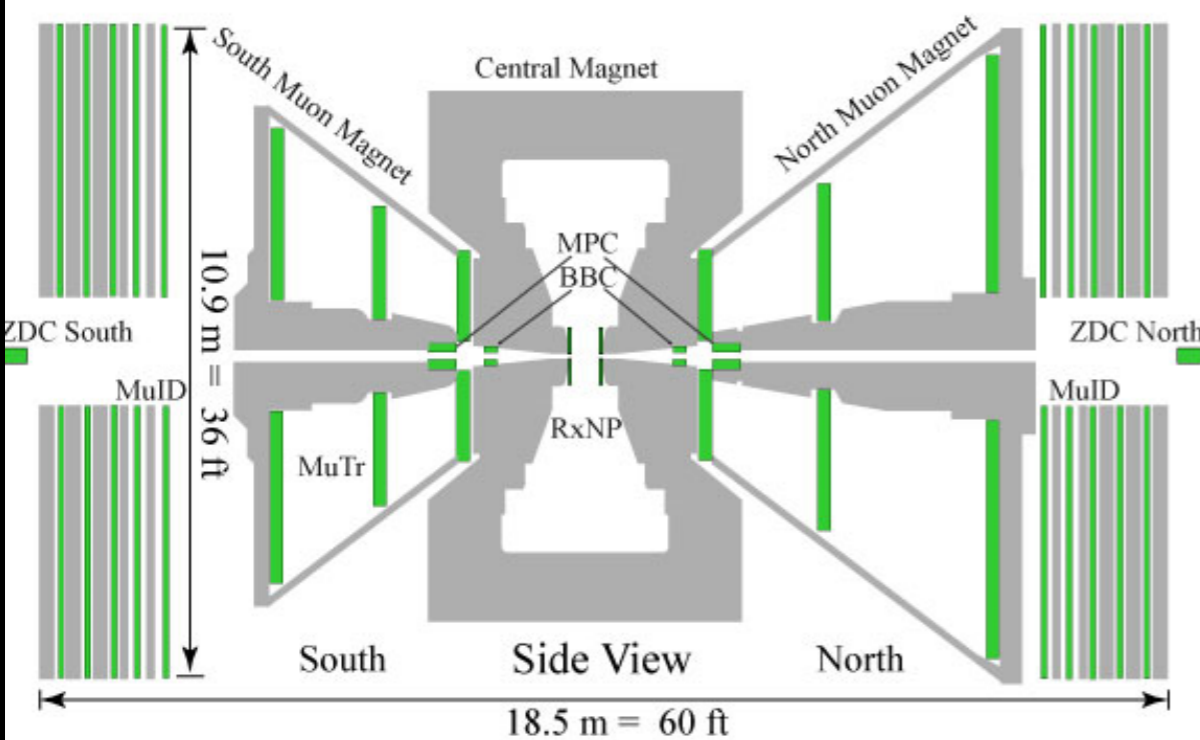
North:

$$10^\circ < \Theta < 37^\circ$$

Central Arms

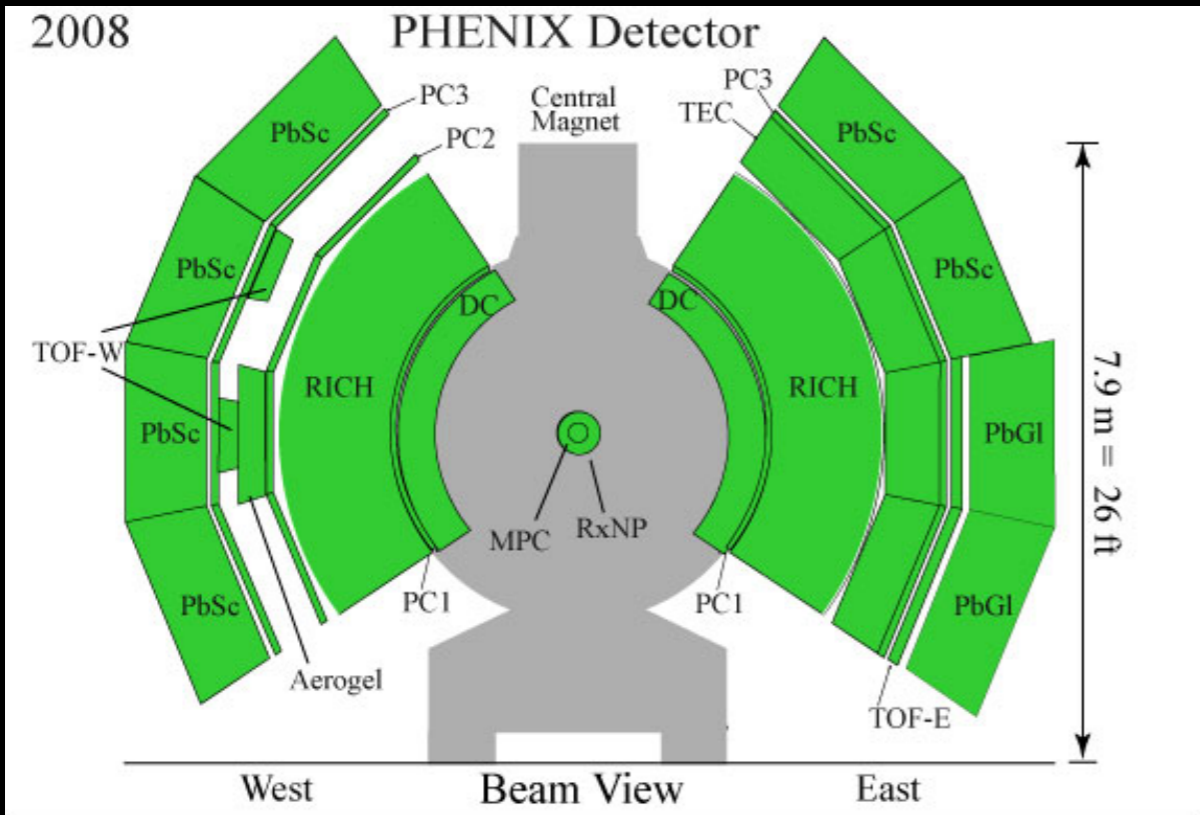
$$|\eta| < 0.35$$

$$60^\circ < \Theta < 110^\circ$$



electrons will not make it  
to the south muon arm  
→ to much material

# Current PHENIX Detector at RHIC



MPC

$$3.1 < |\eta| < 3.9$$

$$2.5^\circ < \Theta < 5.2^\circ$$

Muon Arms

$$1.2 < |\eta| < 2.4$$

South:

$$12^\circ < \Theta < 37^\circ$$

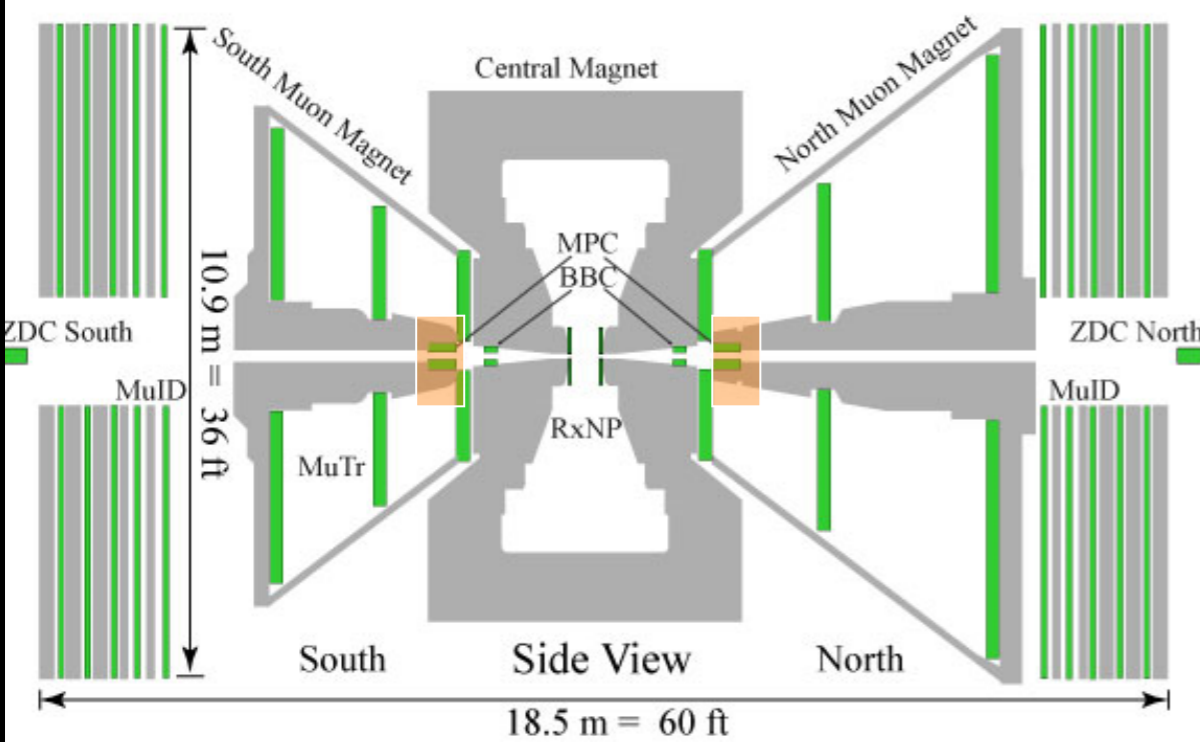
North:

$$10^\circ < \Theta < 37^\circ$$

Central Arms

$$|\eta| < 0.35$$

$$60^\circ < \Theta < 110^\circ$$



electrons will not make it  
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→ to much material



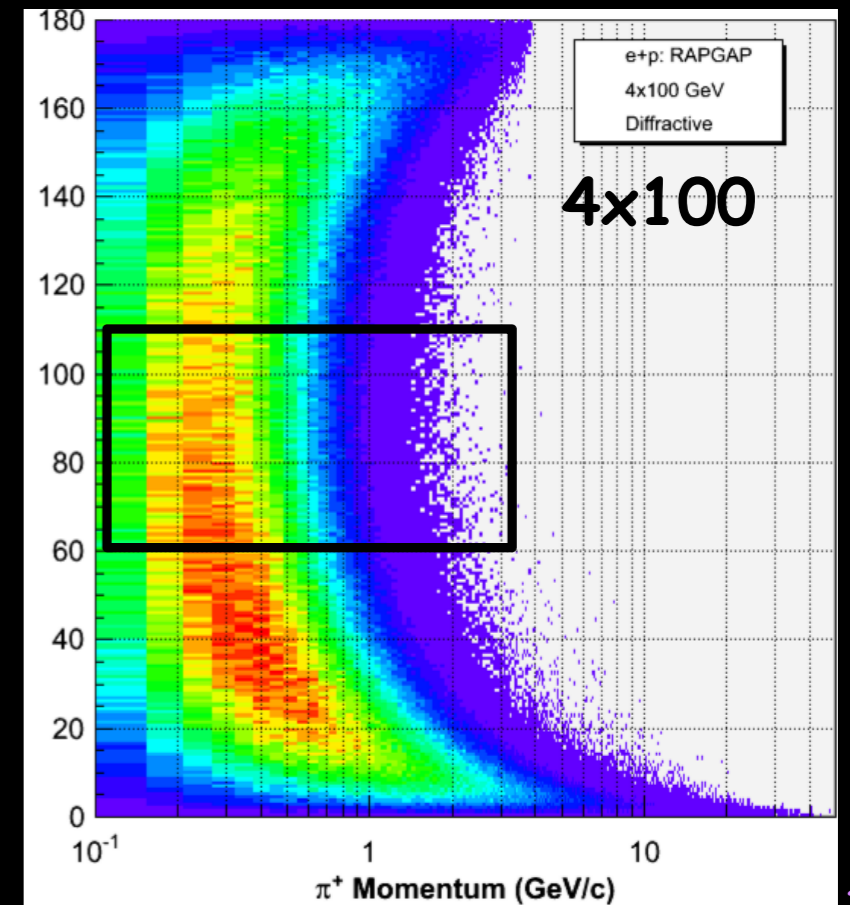
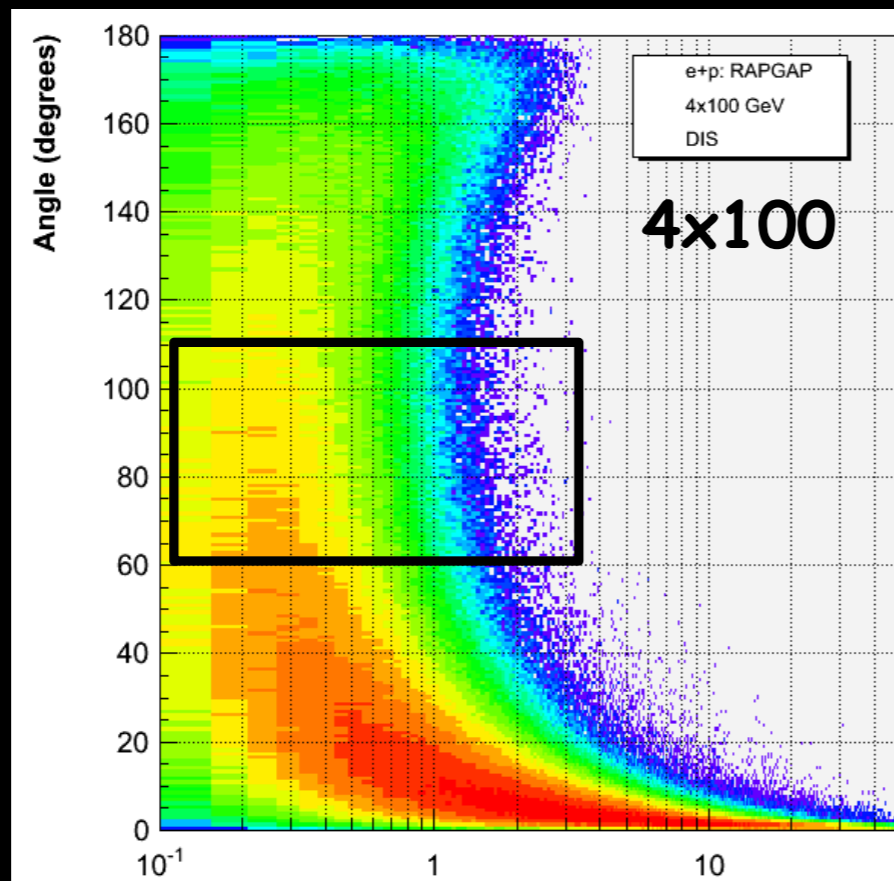
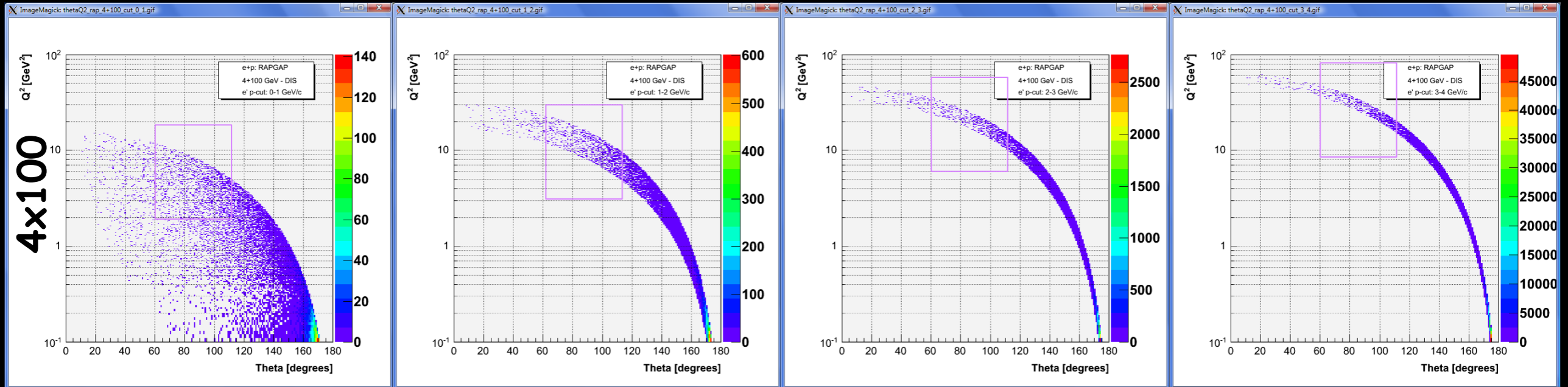
# What will the current Phenix see

$p_e$ : 0-1 GeV

$p_e$ : 1-2 GeV

$p_e$ : 2-3 GeV

$p_e$ : 3-4 GeV



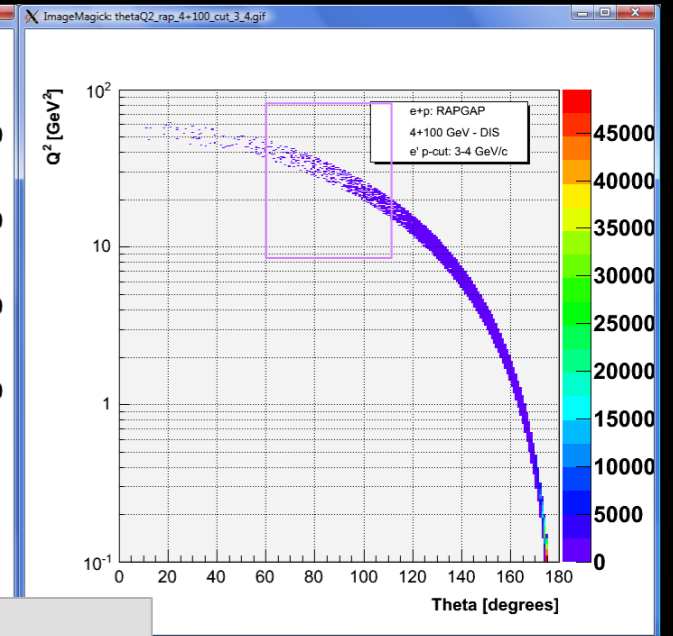
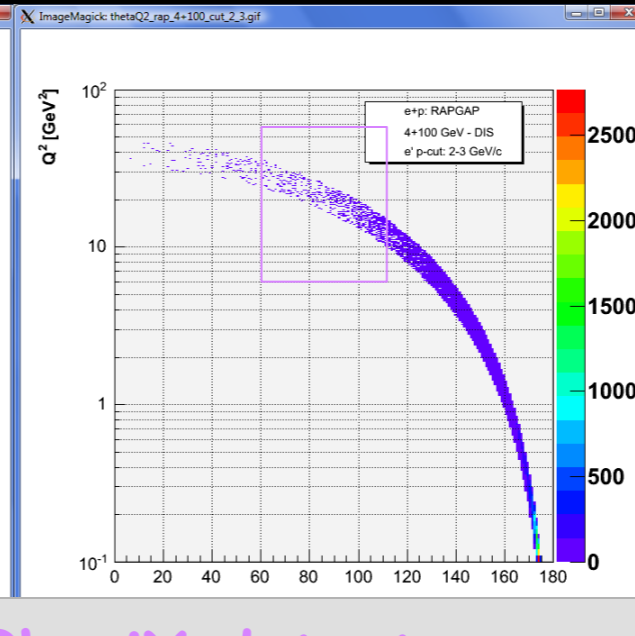
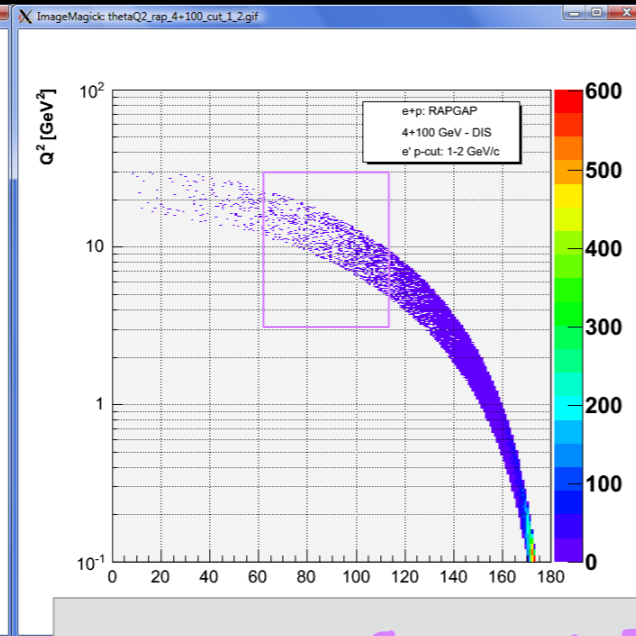
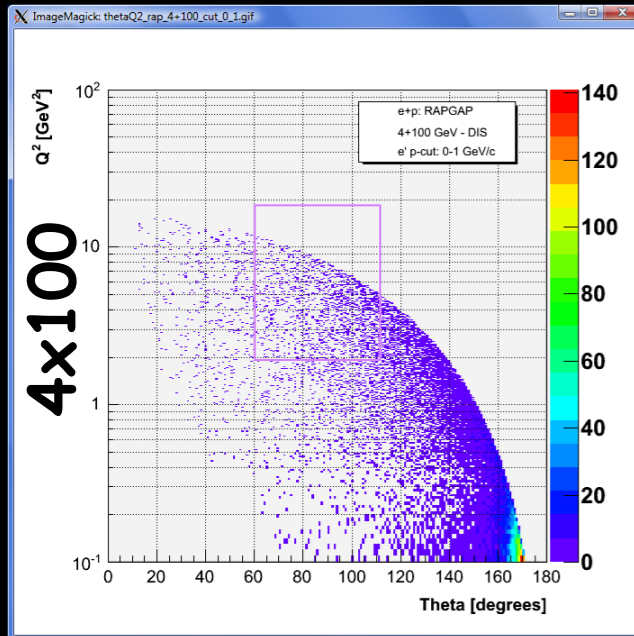
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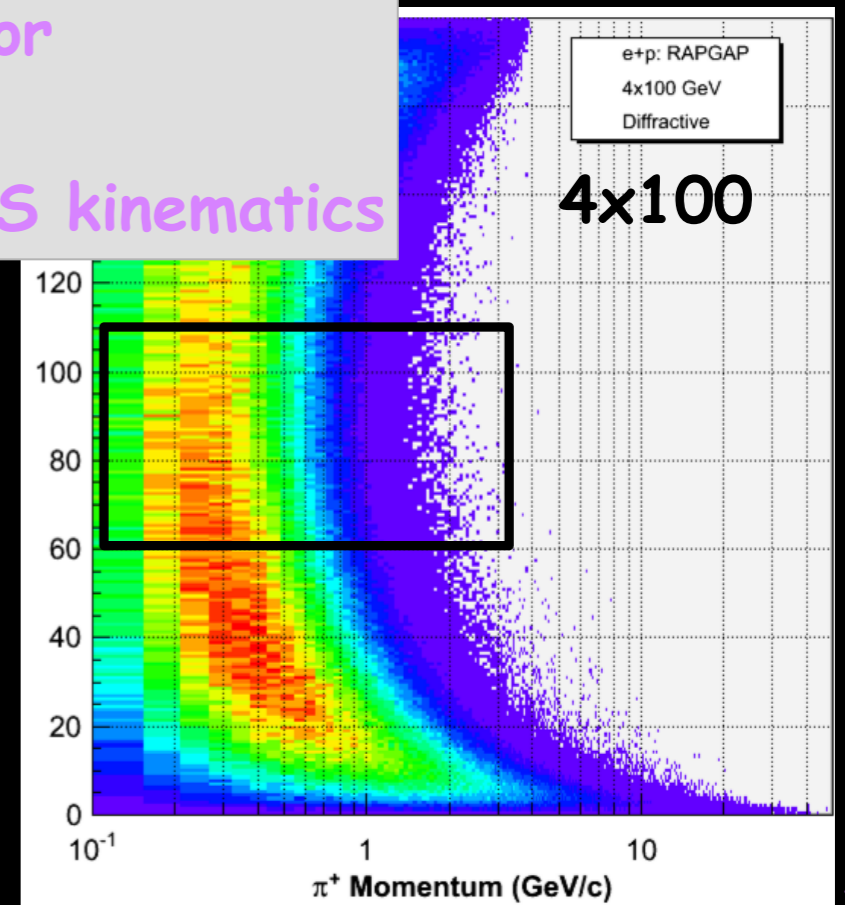
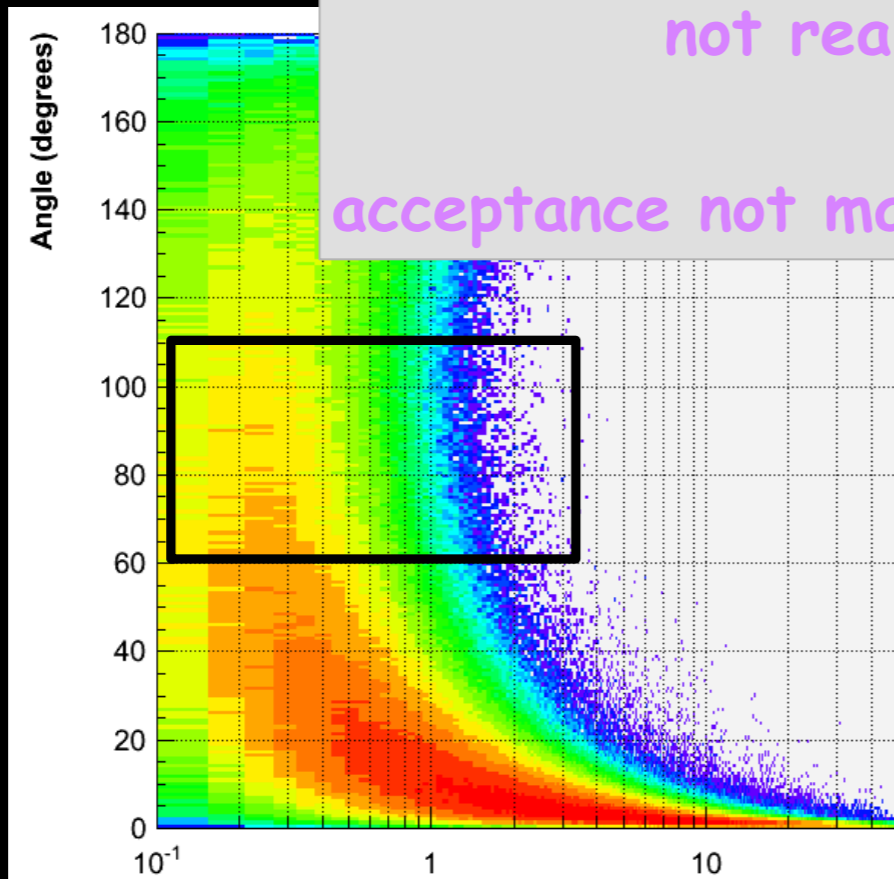
$p_e$ : 1-2 GeV

$p_e$ : 2-3 GeV

$p_e$ : 3-4 GeV



Current PhenIX detector  
not really useable for  
DIS  
acceptance not matched to DIS kinematics



# How should a ePhenIX look like

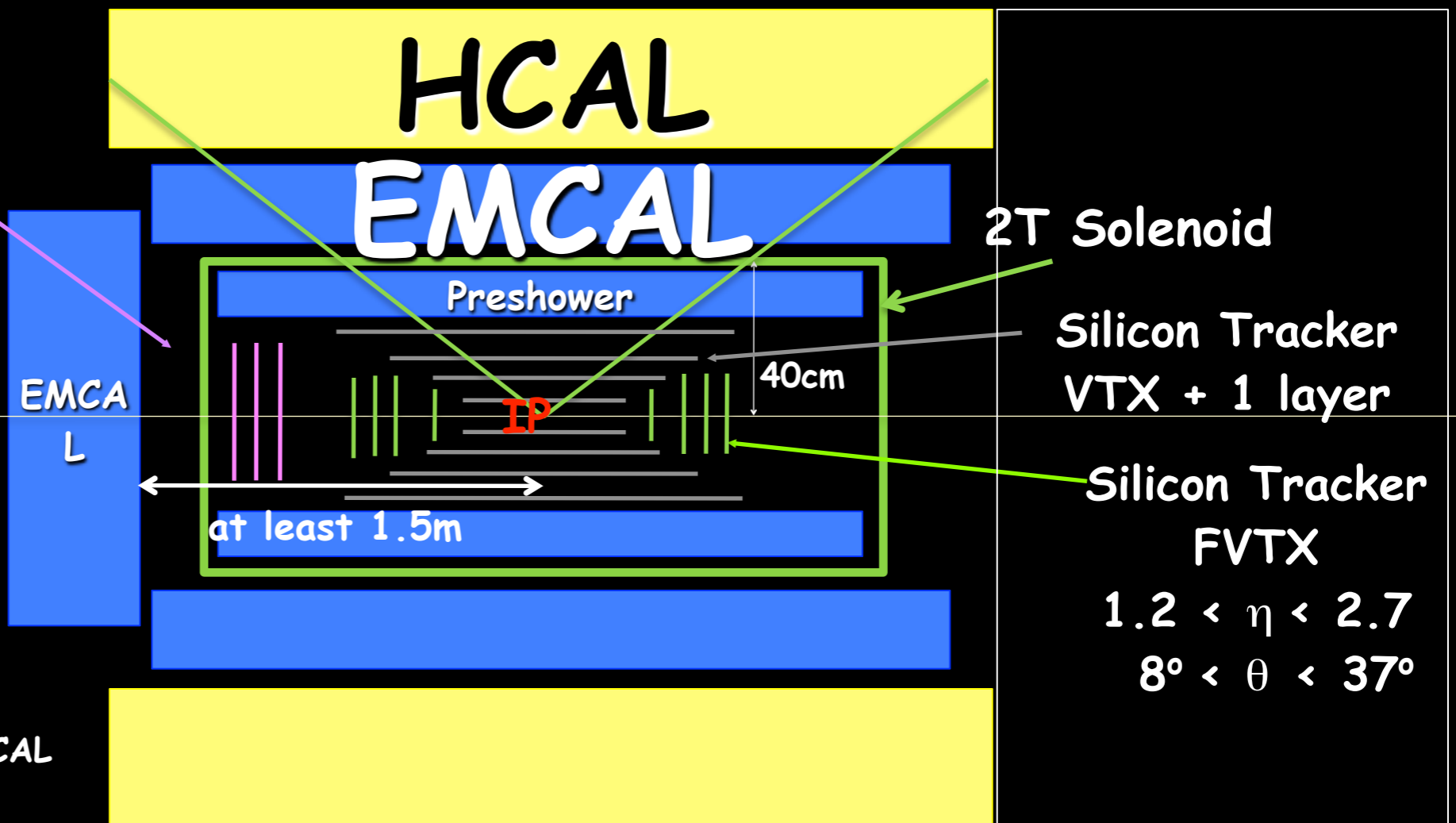
- Coverage in  $|\eta| = < 3 \rightarrow 0.1 < Q^2 < 100$  ( $5^\circ - 175^\circ$ )
  - ◆ need an open geometry detector
  - ◆ planes for next decadal plan
    - replace current central detector with a new one covering  $|\eta| = < 1$
    - replace South muon arm by a endcap spectrometer able to do DY at  $|\eta| > 2.5$ , preferable  $3 < |\eta| < 4$

might need a RICH for HI physics or PID

$5^\circ$  @ 2m  
17.4 cm  $\delta y$

HCAL  
AL

could be ILC-type HCAL with  $\mu$ -ID



# Summary and Outlook

- Lots of MC generators at BNL (anyone can use)
  - ➔ spin: gmc\_trans, PEPSI; low-x: PYTHIA, RAPGAP; e+p, e+A: xDVMP
- xDVMP is a promising tool to look at exclusive diffractive vector-meson production in a saturated picture
  - ➔ currently works for e+p collisions, needs work to implement in e+A collisions
    - ▶ relatively straight forward
  - ➔ need to develop a more general e+A generator
    - ▶ Yasushi Nara just completed 1 month at BNL, Henri Kowalksi currently at BNL for 3 months, Tobias Toll is a new post-doctoral hire about to start
- Work underway in implementing detector designs in GEANT to study with the generated events
  - ➔ Looking at the possible use of eSTAR and ePHENIX concepts
    - ▶ eSTAR looks promising and the STAR geometry is in the same format as what we are using for our other studies

**BACKUP SLIDES**

Accelerator

# MeRHIC parameters for e-p collisions

© V.Ptitsyn

	not cooled		With cooling	
	p	e	p	e
Energy, GeV	250	4	250	4
Number of bunches	111		111	
Bunch intensity, $10^{11}$	2.0	0.31	2.0	0.31
Bunch charge/current, nC/mA	32/320	5/50	32/320	5/50
Normalized emittance, $1e-6$ m, 95% for p / rms for e	15	73	1.5	7.3
rms emittance, nm	9.4	9.4	0.94	0.94
beta*, cm	50	50	50	50
rms bunch length, cm	20	0.2	5	0.2
beam-beam for p /disruption for e	$1.5e-3$	3.1	0.015	7.7
Peak Luminosity, $1e32, \text{ cm}^{-2}\text{s}^{-1}$	<b>0.93</b>		<b>9.3</b>	

**Luminosity for light and heavy ions  
is the same as for e-p if measured per nucleon!**

# Luminosity in eRHIC

	eRHIC IR1		eRHIC IR2	
	p / A	e	p / A	e
Energy (max), GeV	325/130	20	325/130	20
Number of bunches	166	74 nsec	166	74 nsec
Bunch intensity (u) , $10^{11}$	2.0	0.24	2.0	0.24
Bunch charge, nC	32	4	32	4
Beam current, mA	420	50	420	50
Normalized emittance, $1e-6$ m, 95% for p / rms for e	1.2	25	1.2	25
Polarization, %	70	80	70	80
rms bunch length, cm	4.9	0.2	4.9	0.2
$\beta^*$ , cm	25	25	5	5
Luminosity, $cm^{-2}s^{-1}$	$2.8 \times 10^{33}$		$1.4 \times 10^{34}$	

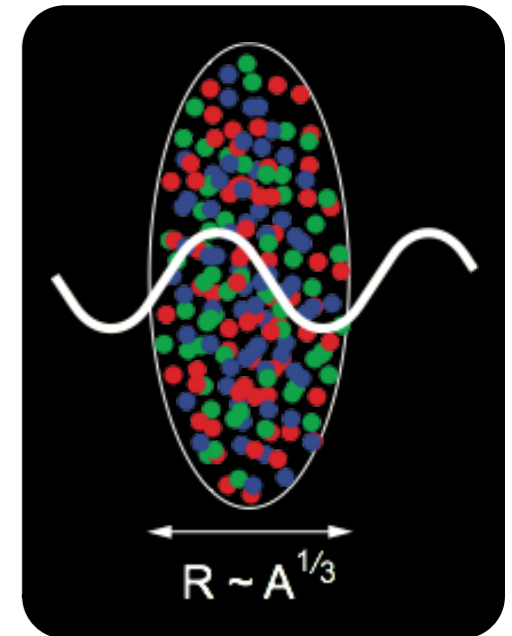
Luminosity for 30 GeV e-beam operation will be at 20% level



Nuclear “Oomph”

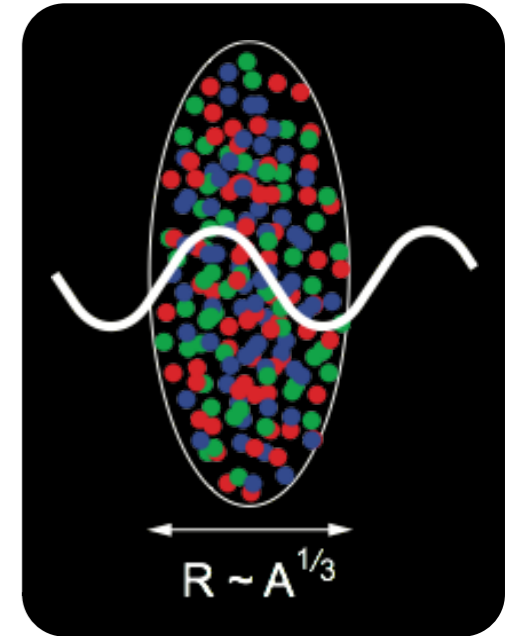
# The Nuclear “Oomph Factor”

- Enhancing Saturation effects:
  - ▶ Probes interact over distances  $L \sim (2m_n\lambda)^{-1}$
  - ▶ For probes where  $L > 2R_A (\sim A^{1/3})$  cannot distinguish between nucleons in front or back of the nucleus.  
**Probe acts coherently with all nucleons!!**



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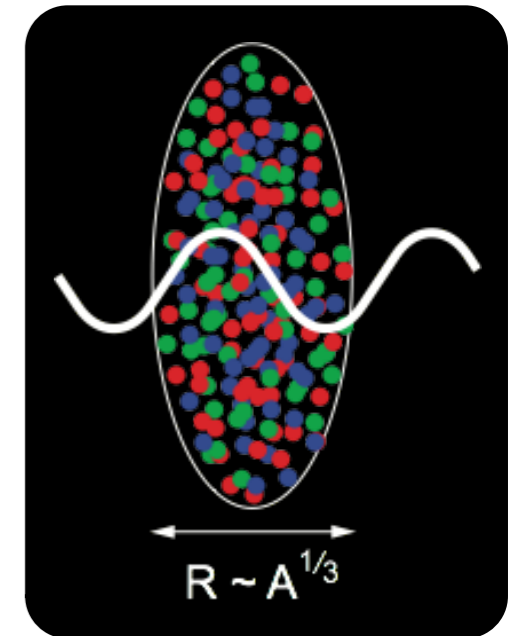
Simple geometric considerations lead to:

**Nuclear “Oomph” Factor:**

$$(Q_s^A)^2 \approx c Q_0^2 \left( \frac{A}{x} \right)^{1/3}$$

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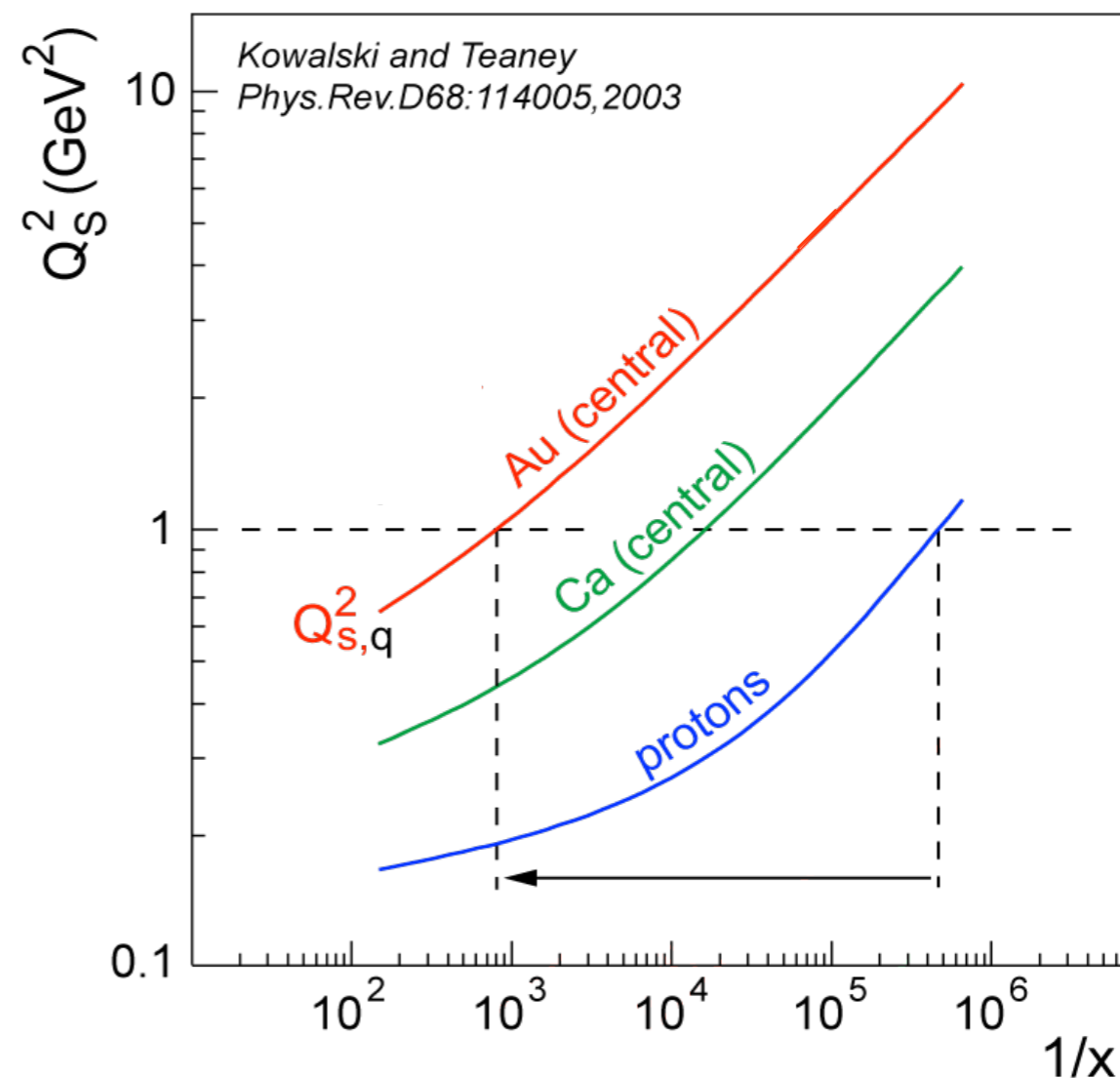
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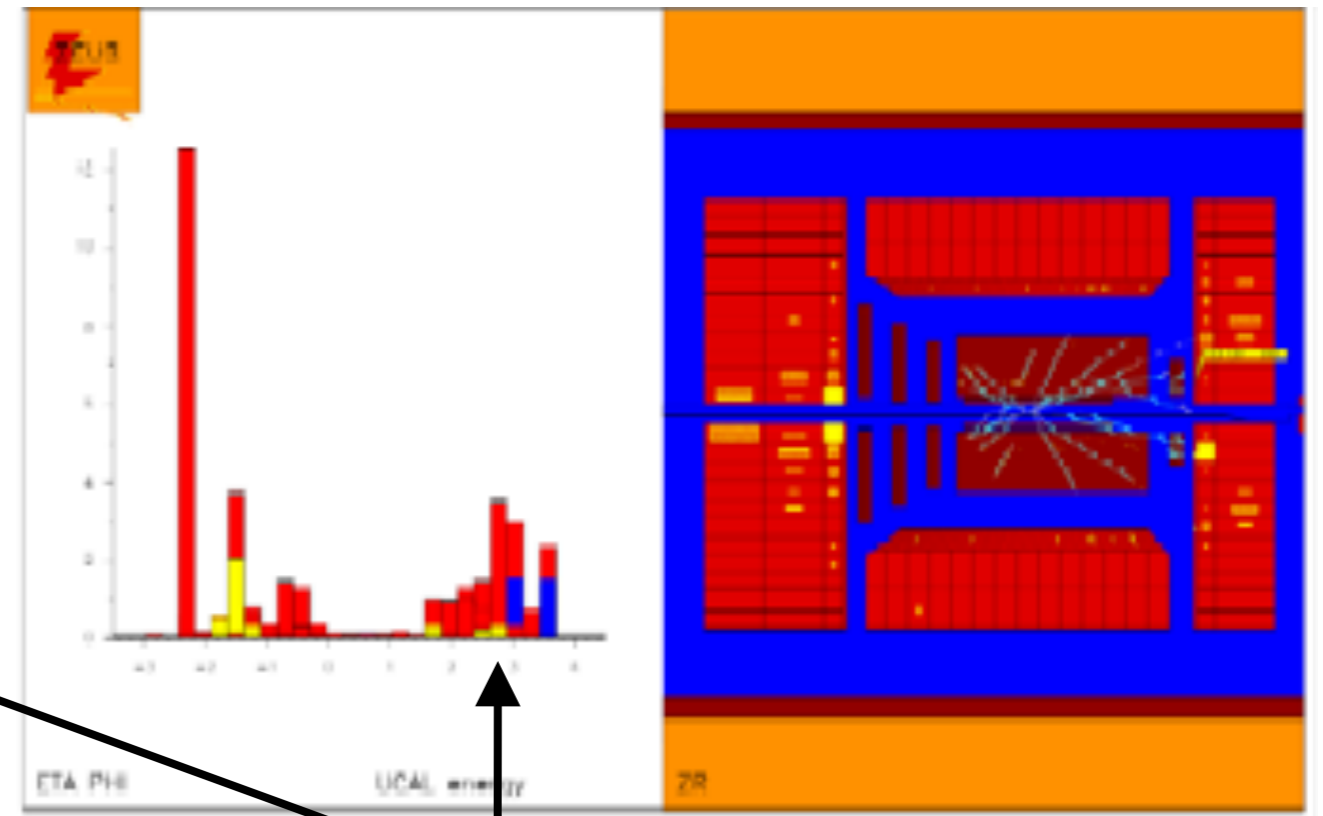
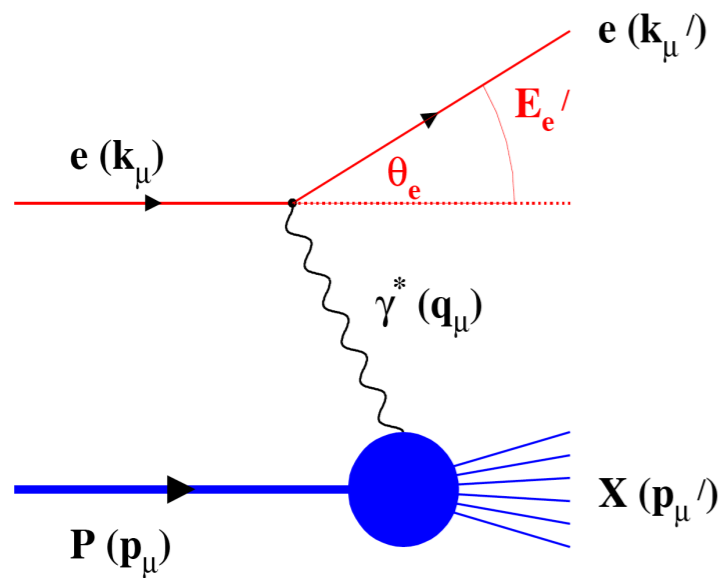
$$(Q_s^A)^2 \approx c Q_0^2 \left( \frac{A}{x} \right)^{1/3}$$



**Diffractive**

# Diffractive Physics in $e+A$

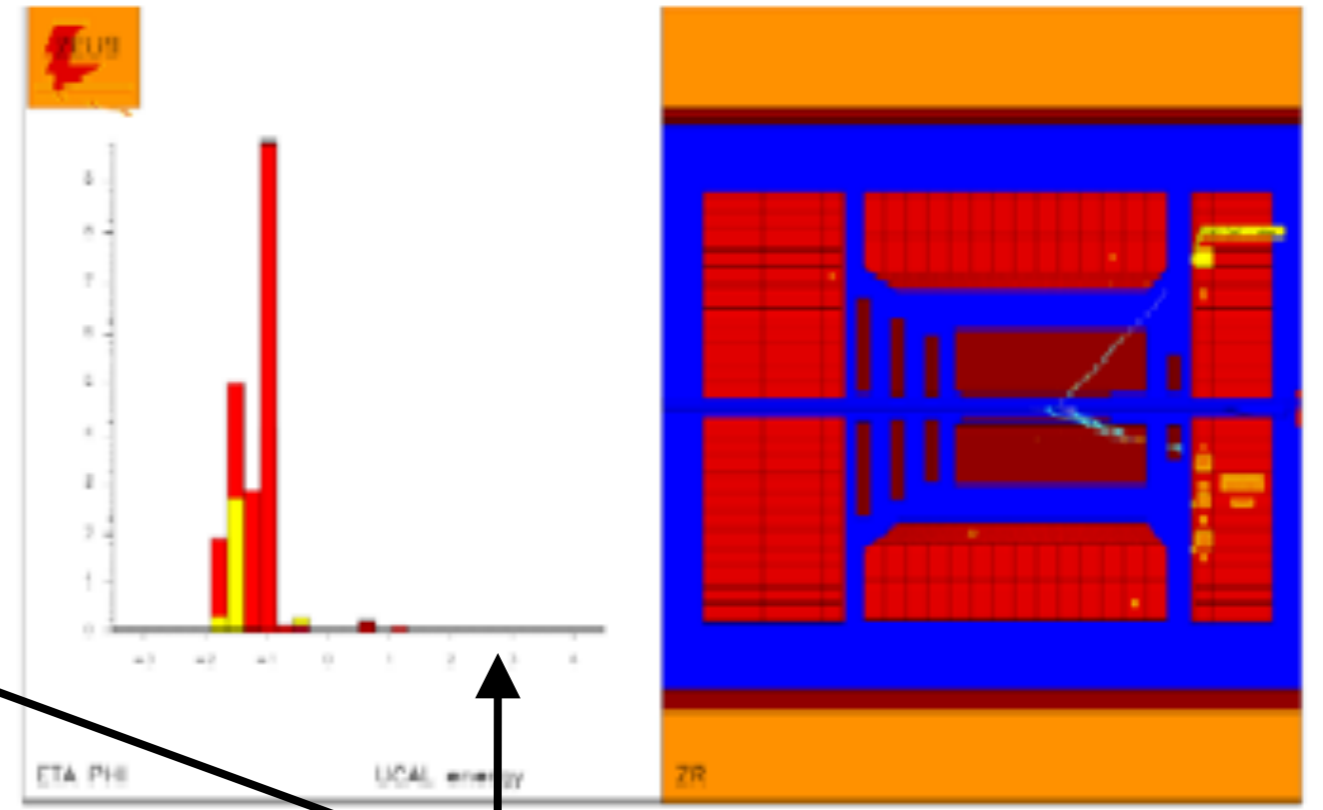
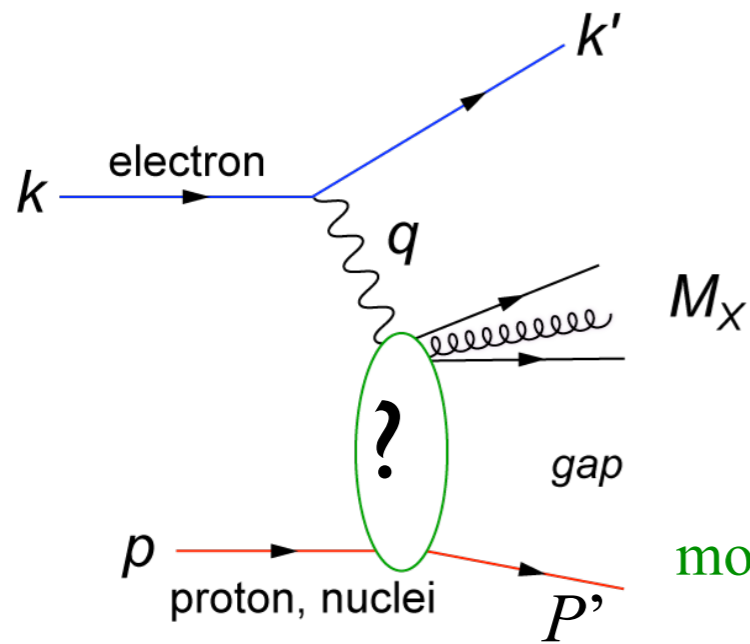
‘Standard DIS event’



Activity in proton direction

# Diffraction Physics in $e+A$

## Diffractive event

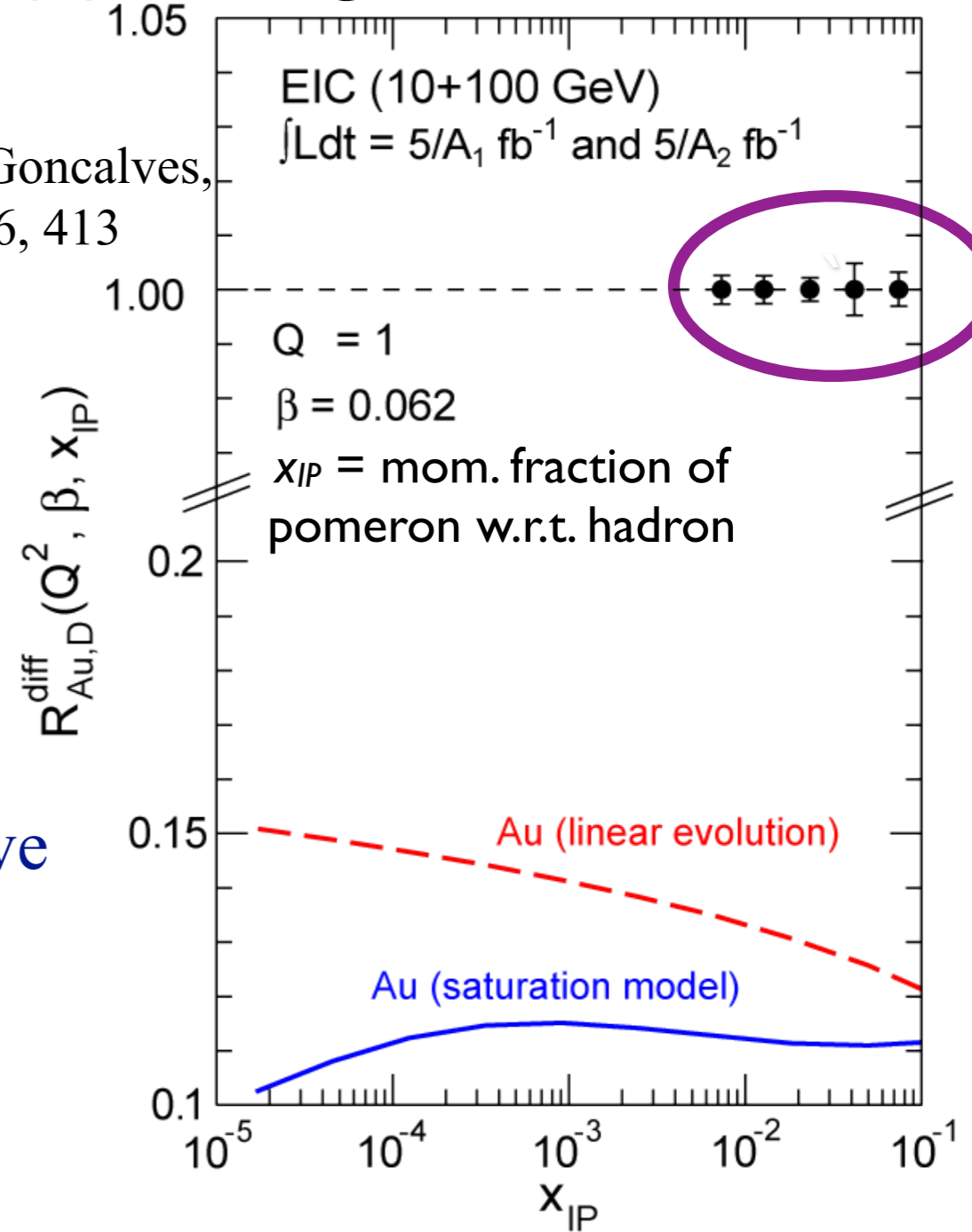
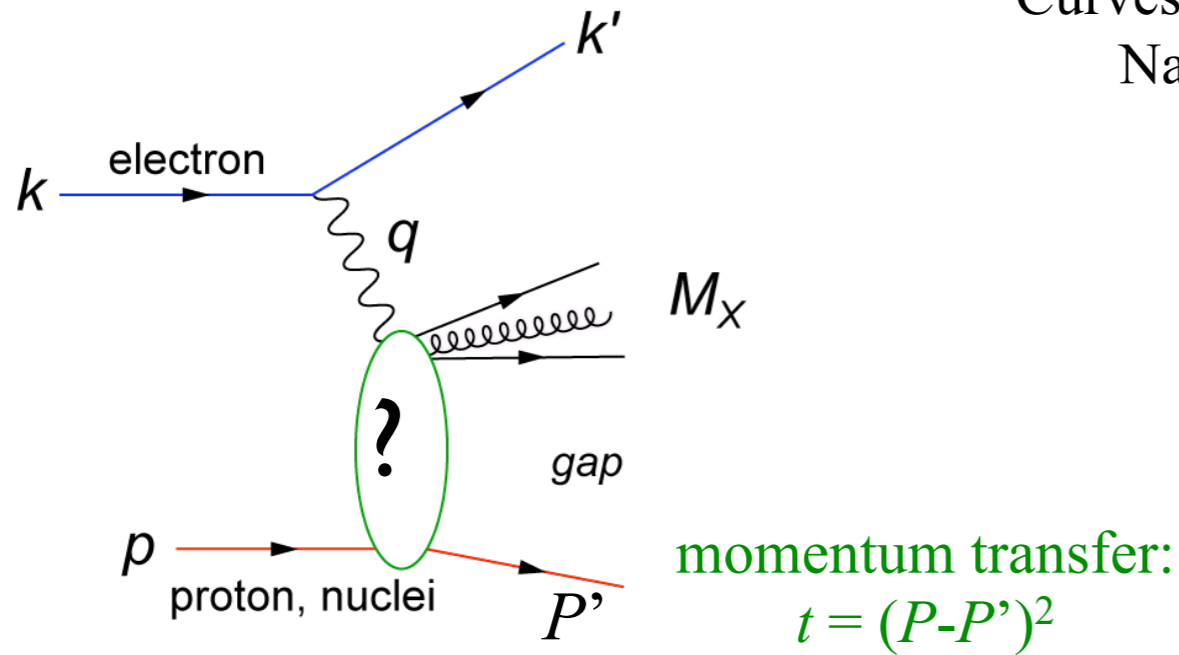


Activity in proton direction

- HERA/ep: 15% of all events are hard diffractive
- Diffractive cross-section  $\sigma_{\text{diff}}/\sigma_{\text{tot}}$  in  $e+A$  ?
- ➔ Predictions: ~25-40%?
- Look inside the “Pomeron”
- ➔ Diffractive structure functions
- ➔ Exclusive Diffractive vector meson production:  $d\sigma/dt \sim [xG(x, Q^2)]^2$  !!

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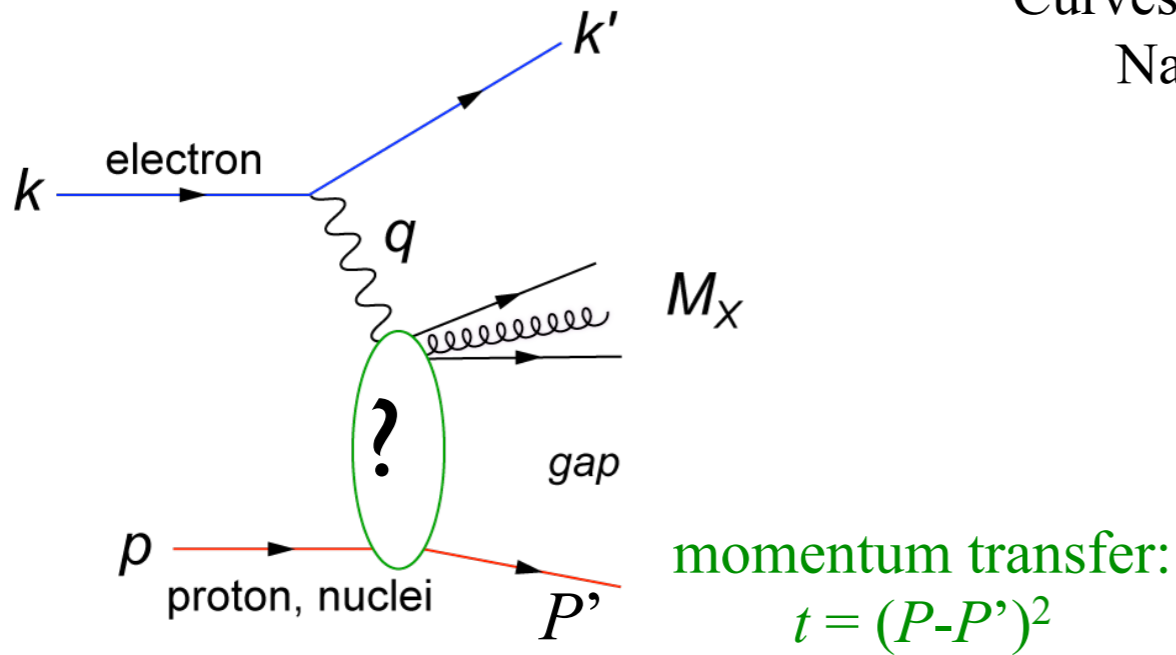
➔ Exclusive Diffractive vector meson production:  $d\sigma/dt \sim [xG(x, Q^2)]^2$  !!

- Distinguish between linear evolution and saturation models

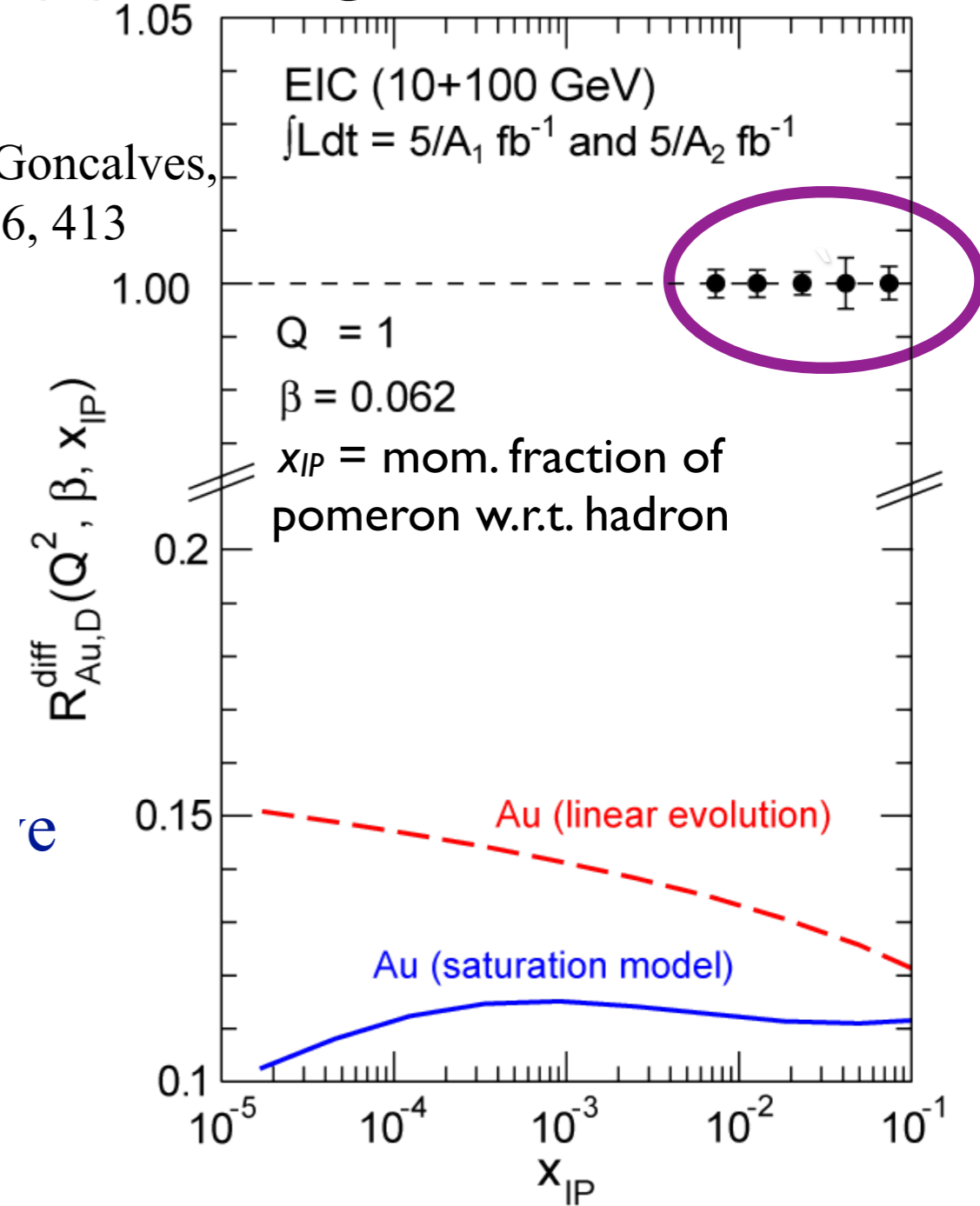
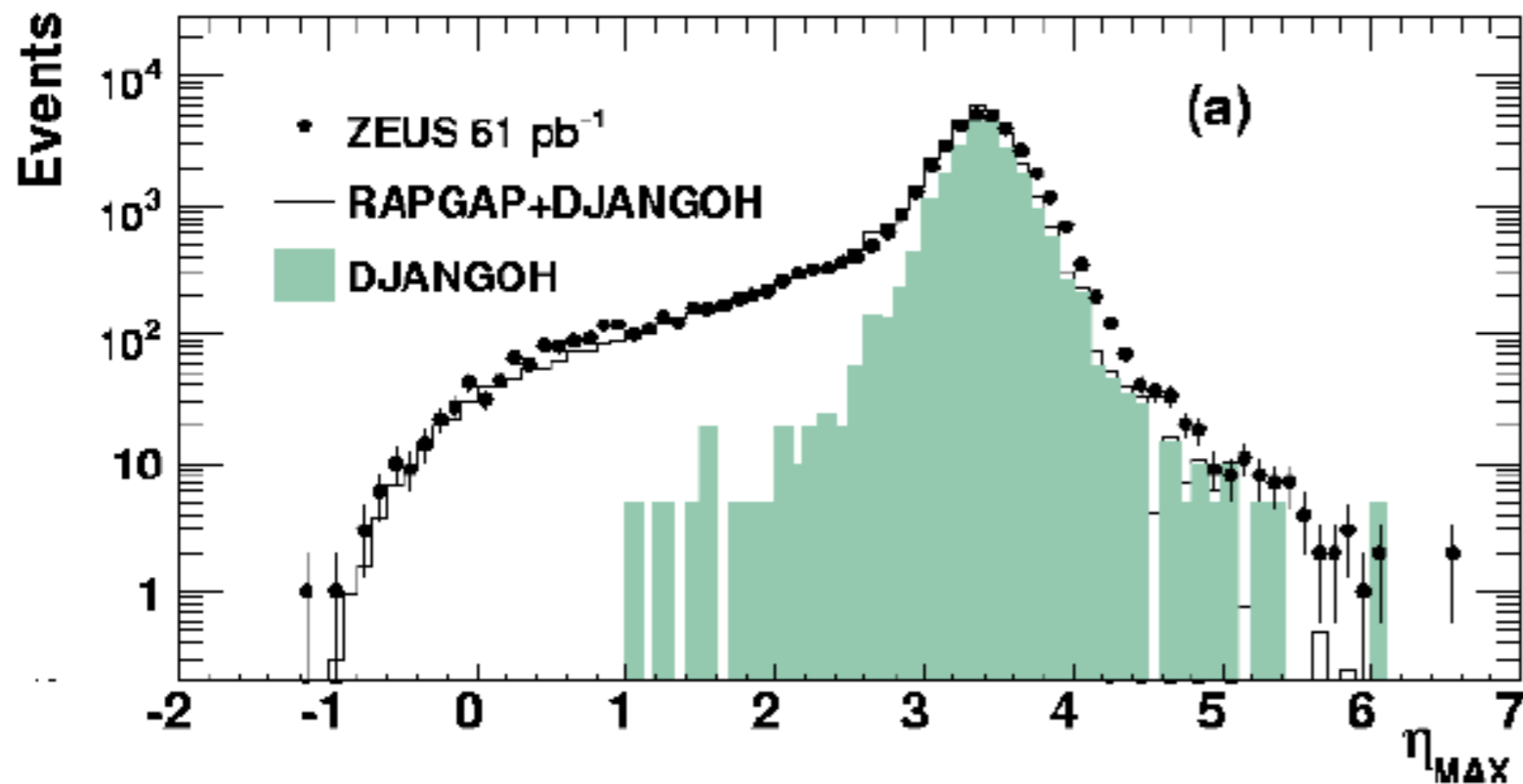


# Diffractive Physics in e+A

## Diffractive event



**ZEUS**

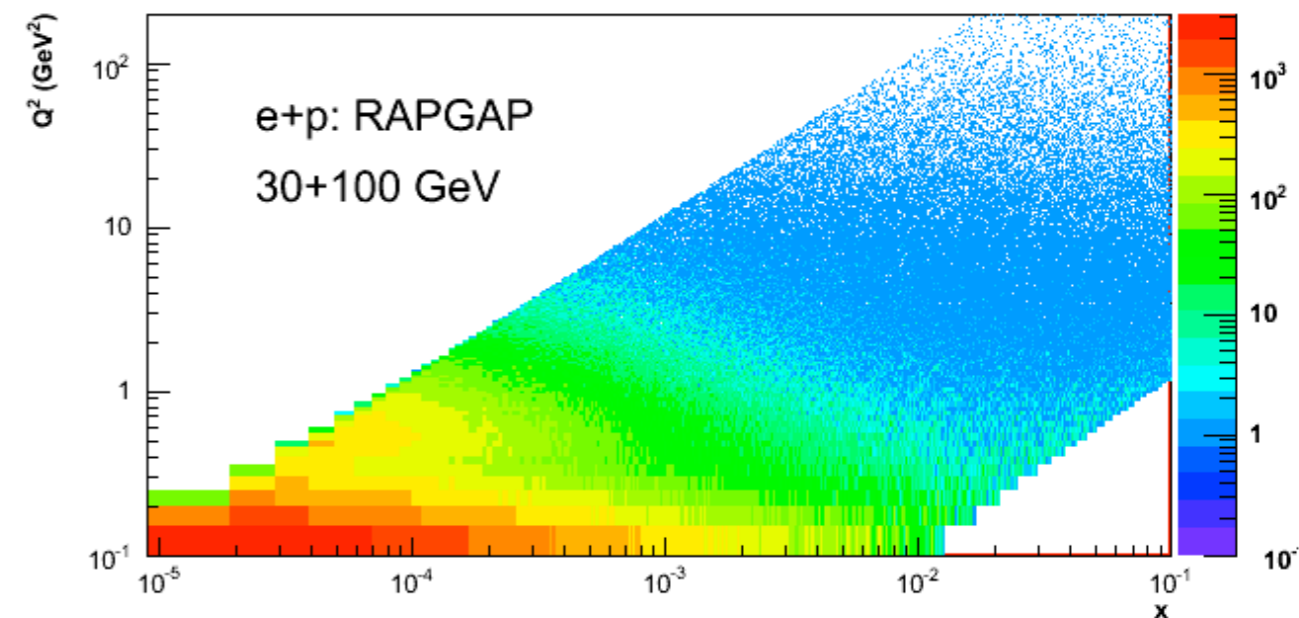
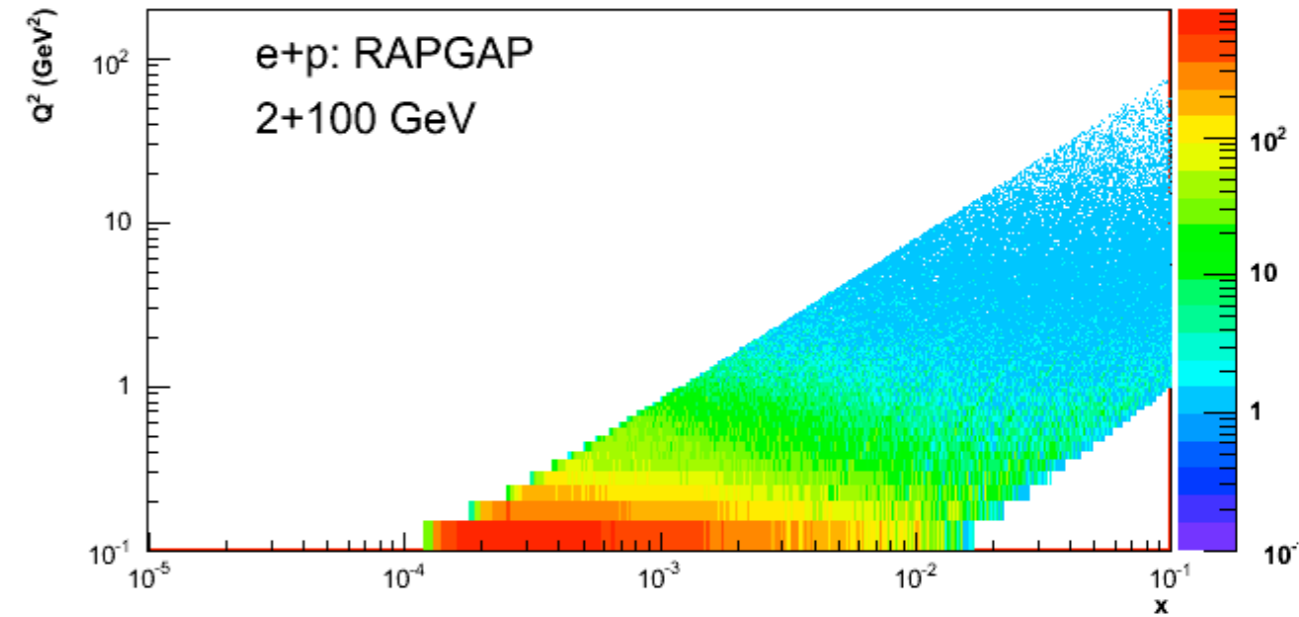


$d\sigma/dt \sim [xG(x, Q^2)]^2 !!$

saturation models

# Diffractive Physics at an EIC

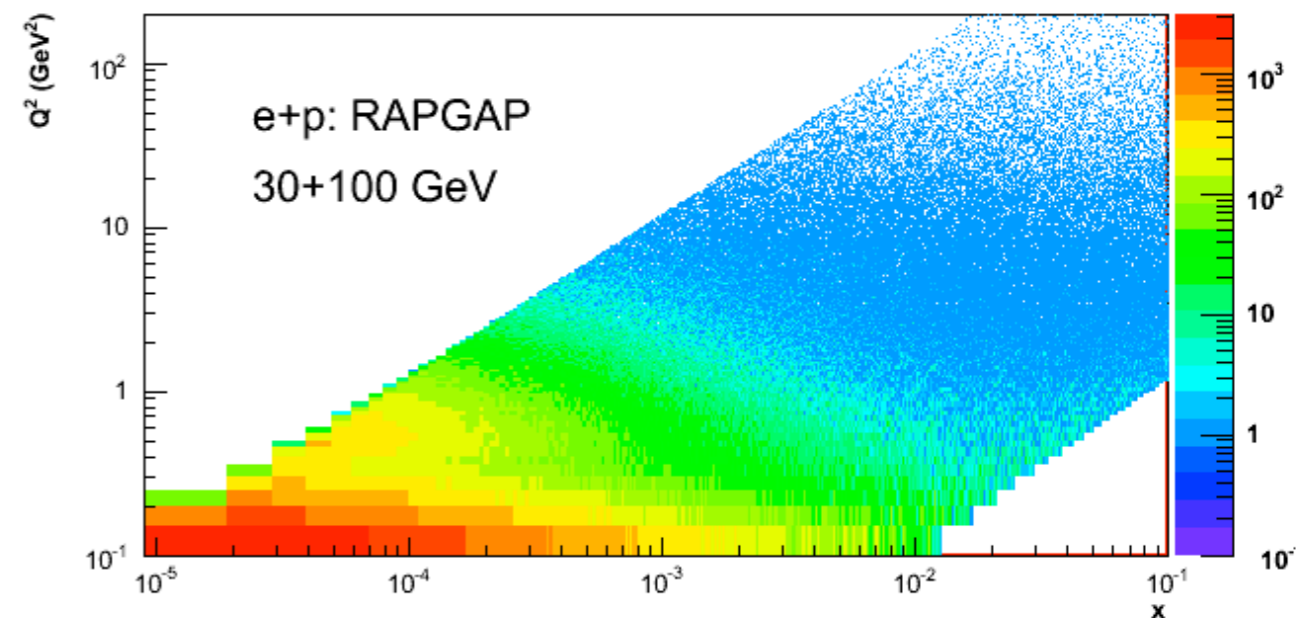
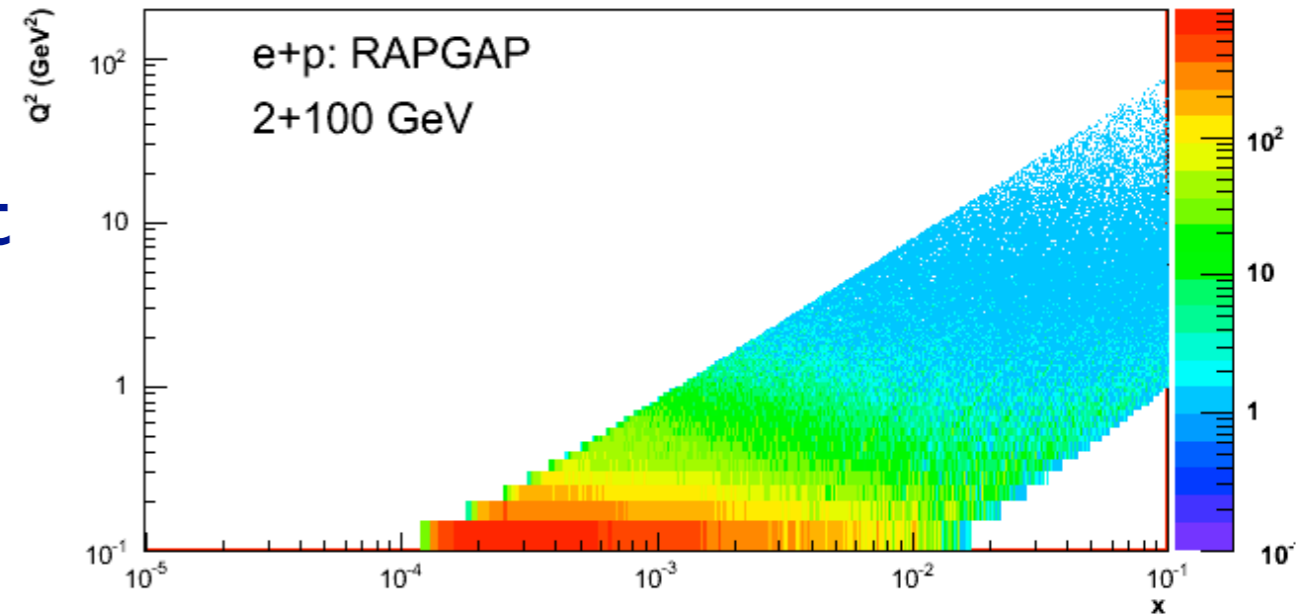
Generated  $10^6$  e+p events using RAPGAP for a variety of proposed EIC energies



# Diffraction Physics at an EIC

- Significant coverage in  $x$ - $Q^2$ 
  - ➔ increases by ~ order of magnitude over EIC energies
- Plotted the distribution of the Most Forward Particle in the event for DIS and Diffractive events
  - ➔ significant gap between two classes of events
- Reproduce well the “ZEUS” plot
- Important - plot the efficiency vs purity
  - ➔ Can place a cut in rapidity for ~90% efficiency and ~90% purity !!

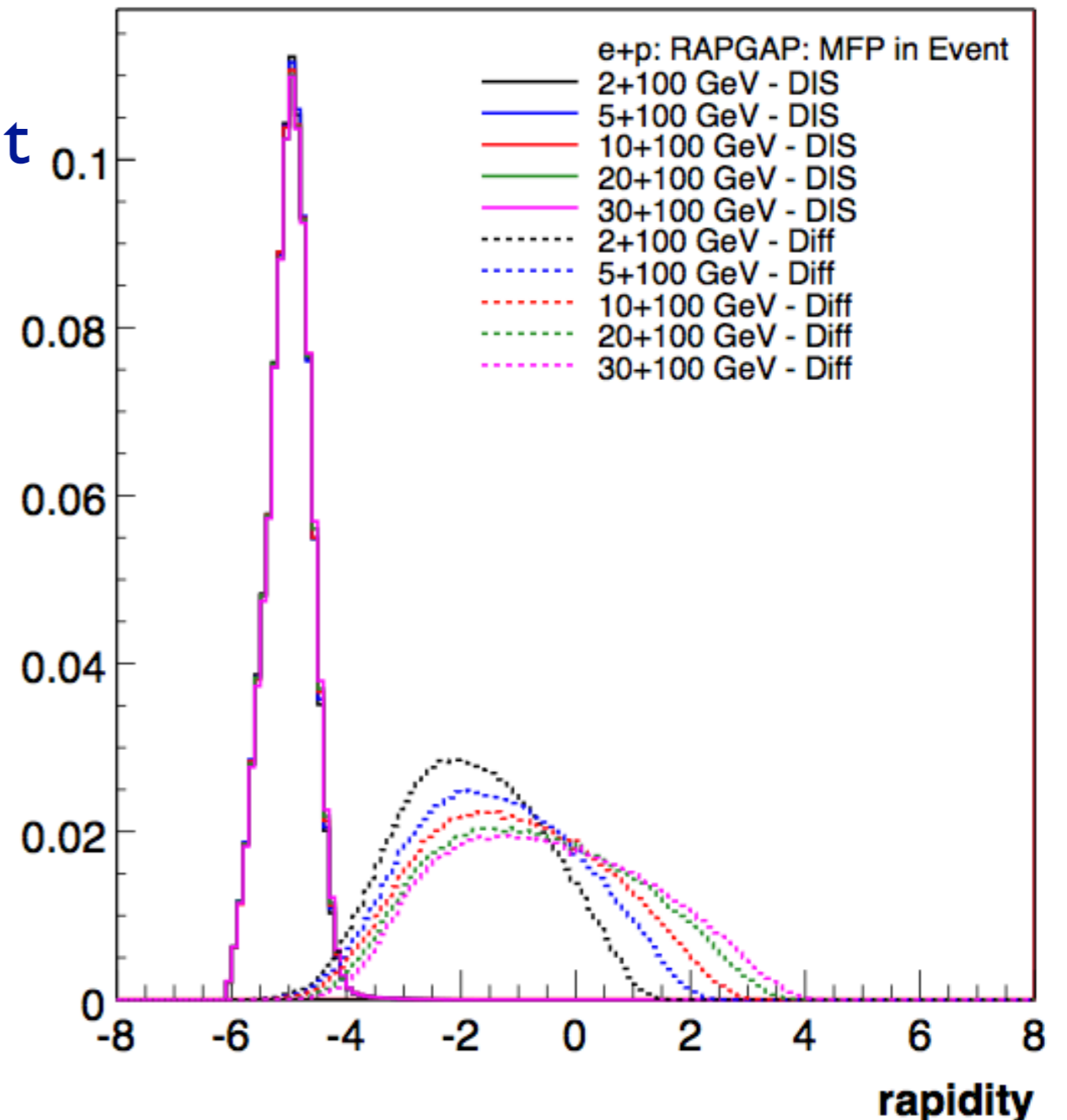
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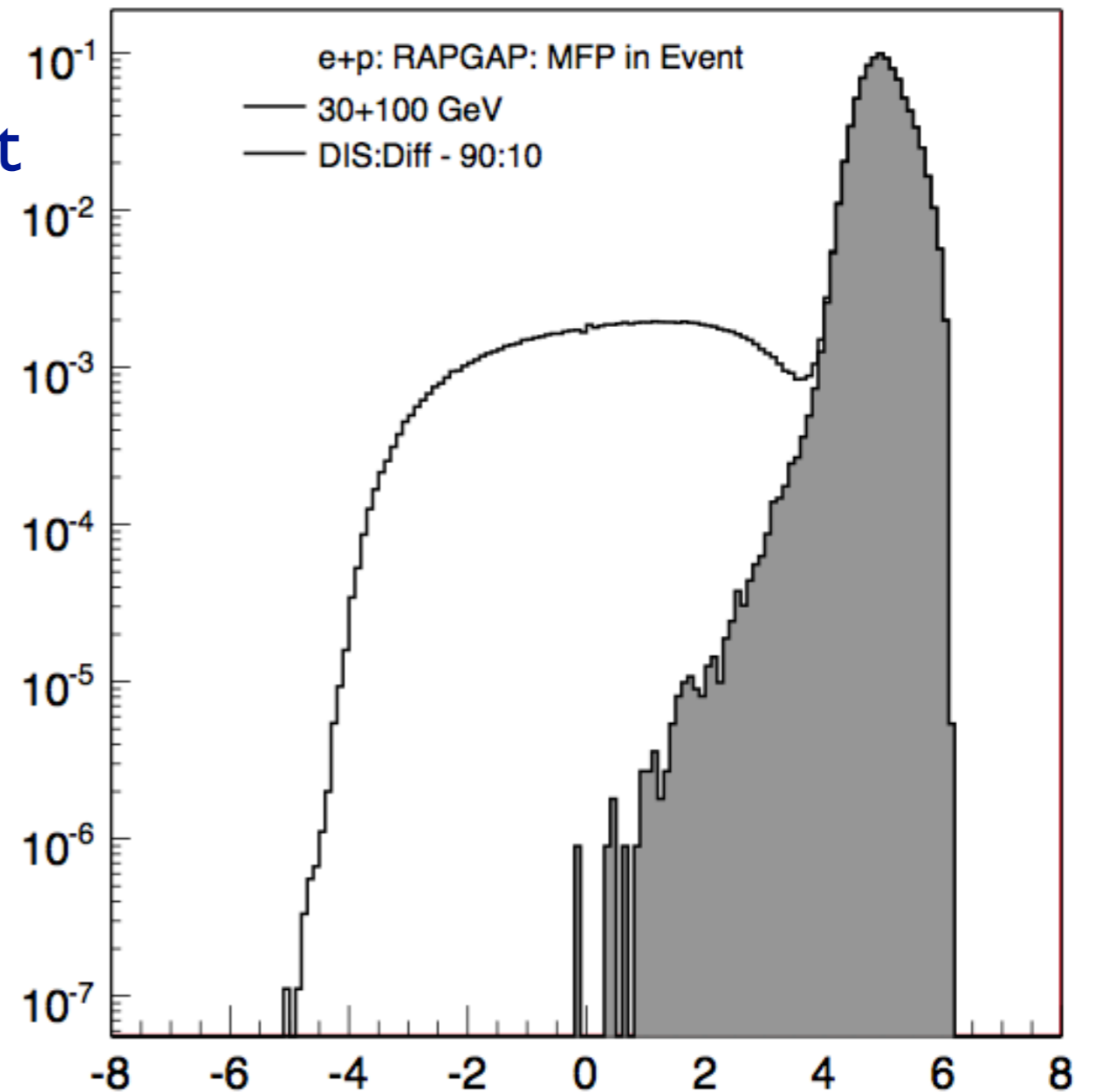
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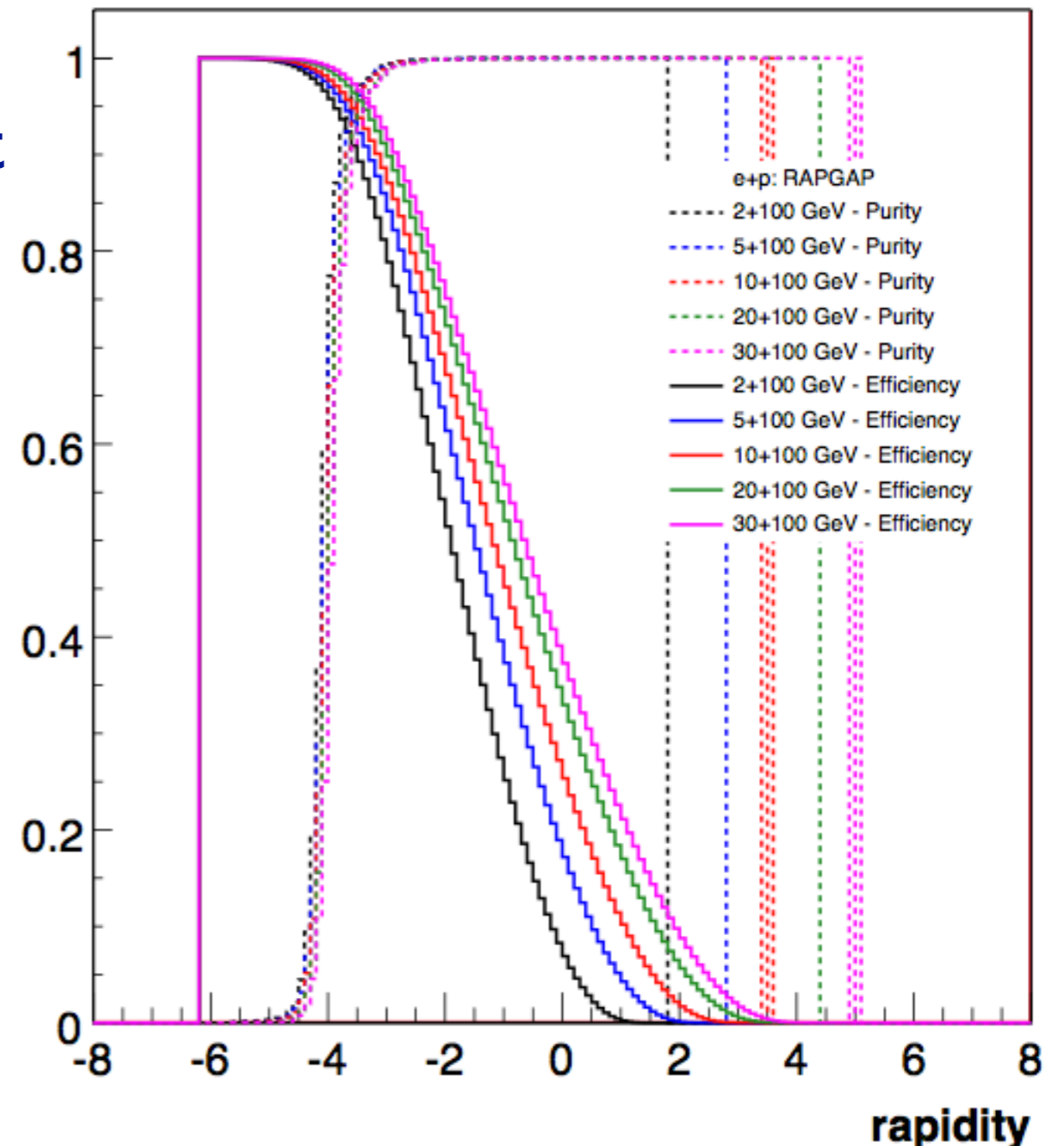
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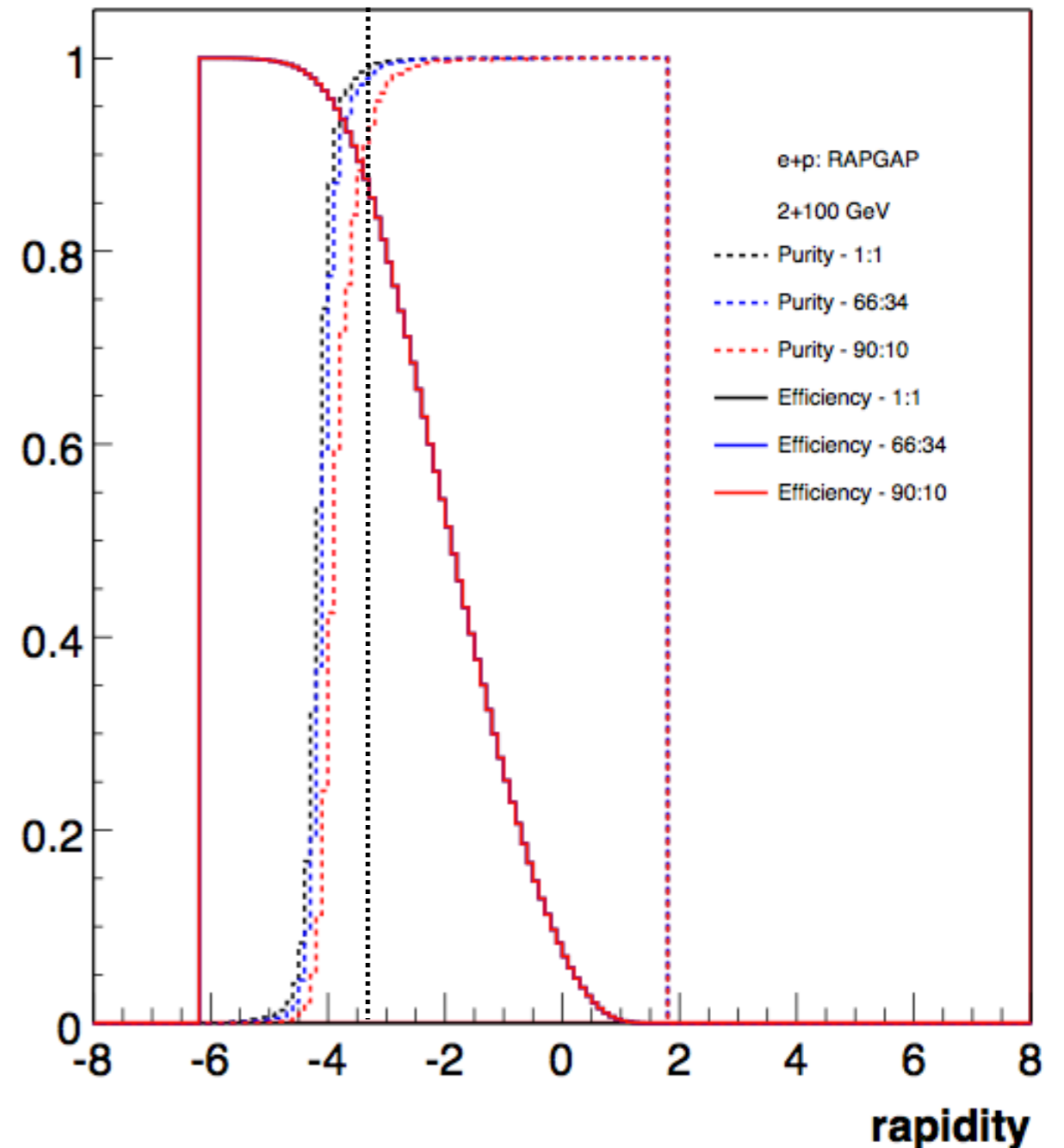
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**Effic:** frac of Diff events out of all Diff events  
**Purity:** frac. Diff events out of all events



# Diffraction Physics at an EIC - Acceptance

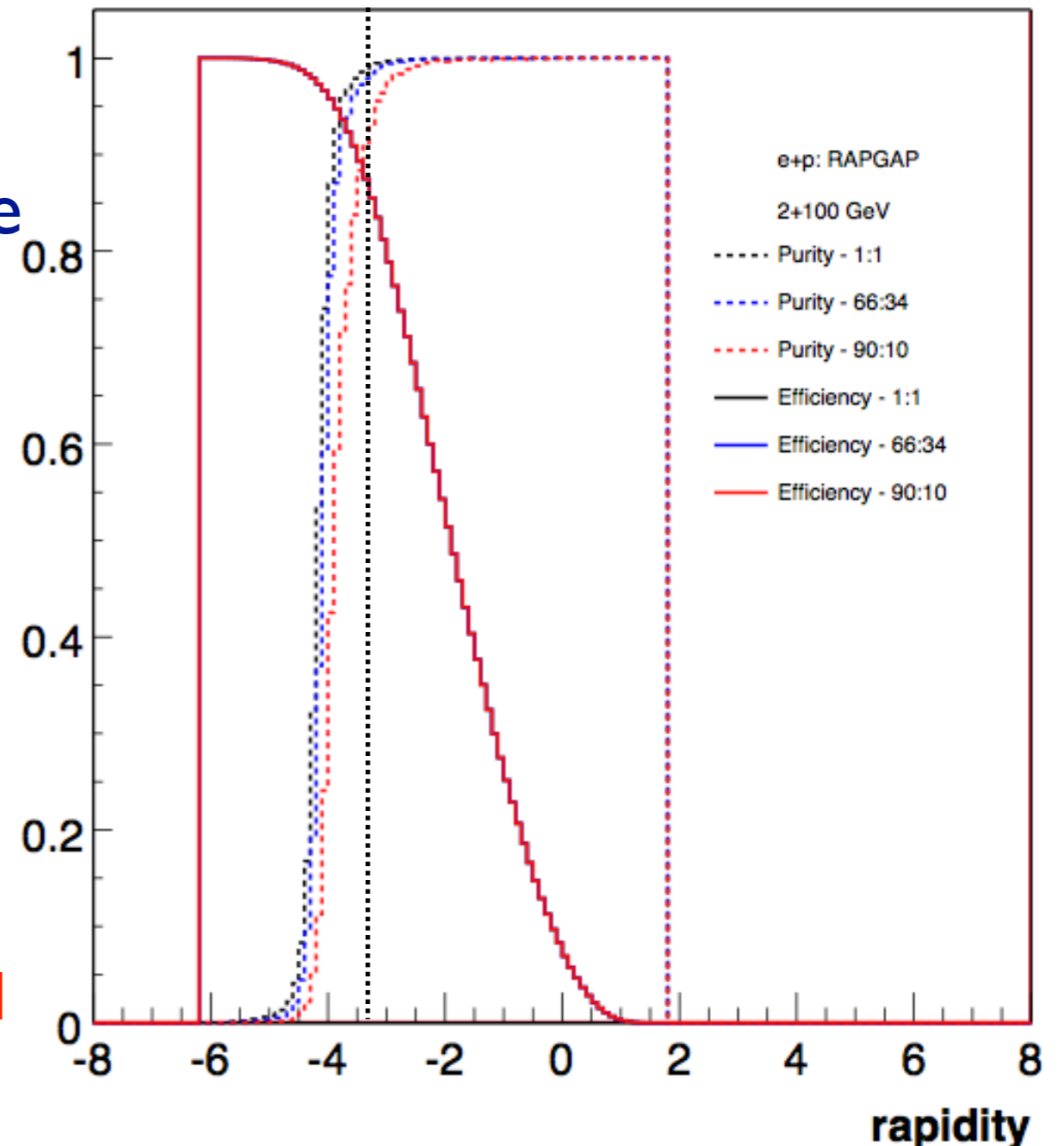
**Effic:** frac of Diff events out of all Diff events  
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# Diffraction Physics at an EIC - Acceptance

- ZEUS had a gap in detector coverage (acceptance) of  $\sim 3$  units.
- Studied this effect in the **MFP** distribution for EIC energies:
- Keeping the 90% Purity level has the following effect:
  - **1 unit cut in rapidity**
    - ➔ Efficiency falls by factor of 2, rapidity moves 2 units to right
  - **2 unit cut in rapidity**
    - ➔ Efficiency falls by a factor of 4, rapidity cut moves farther to right !!
- **When designing a detector, it is essential to be as hermetic as possible !!!**

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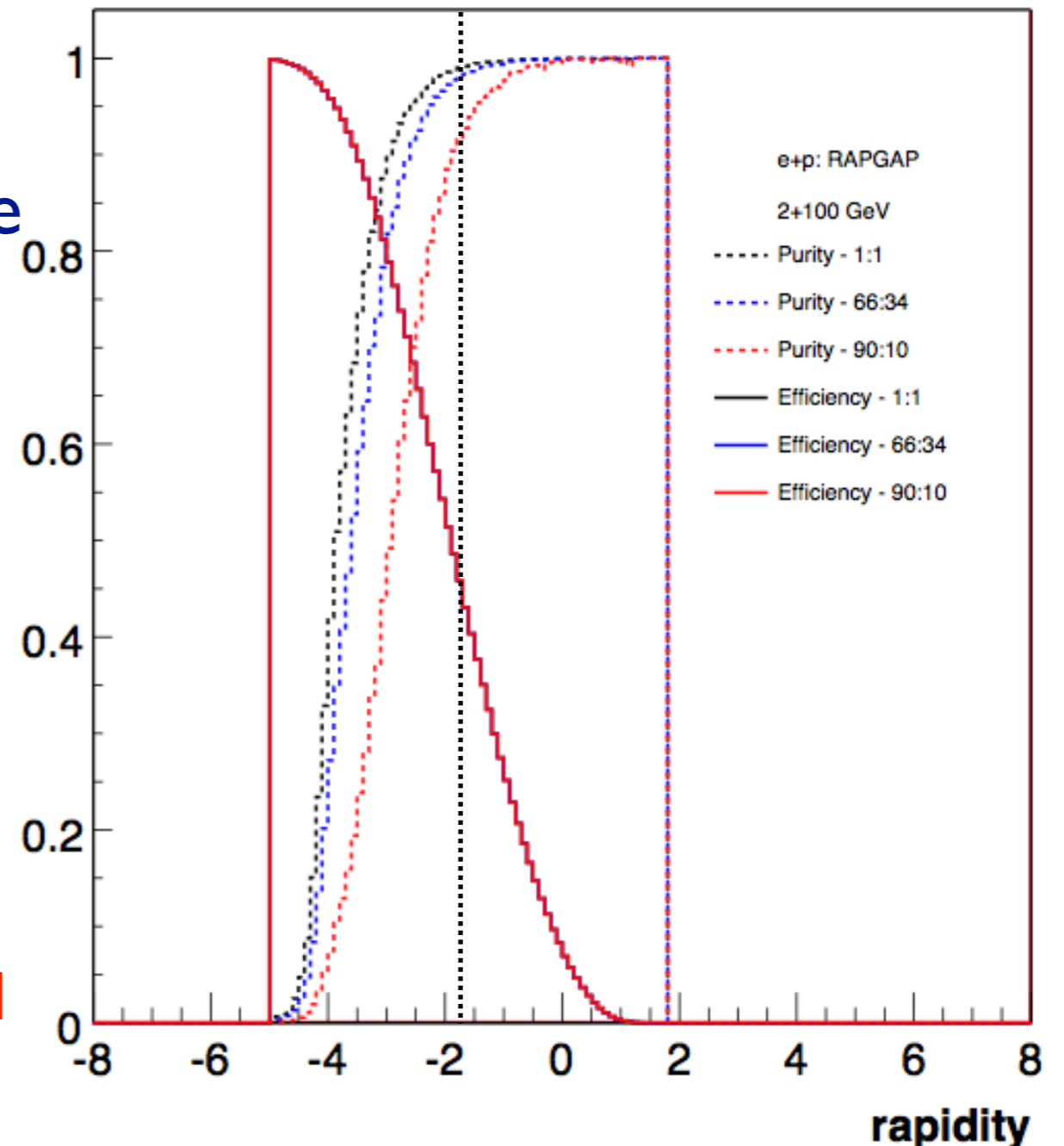




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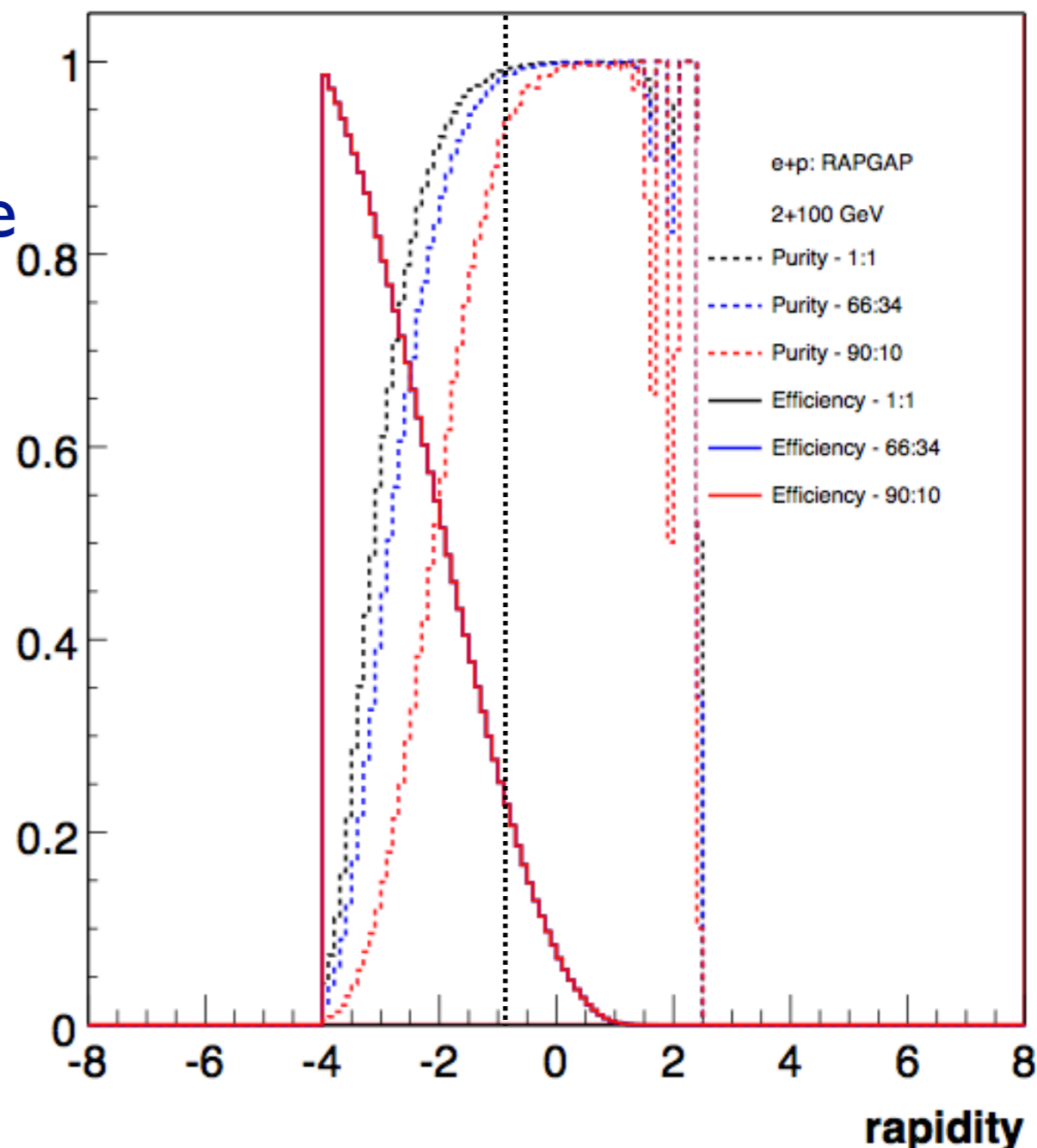
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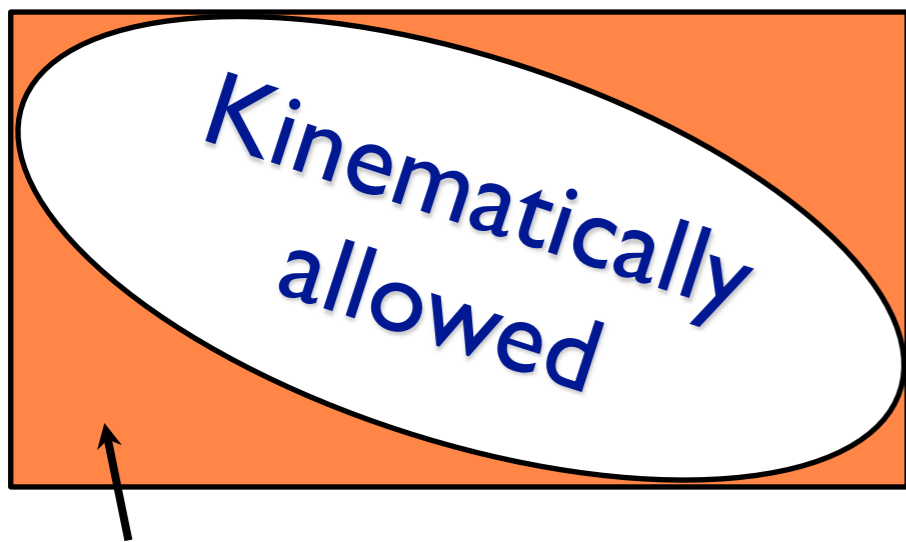
# UNU.RAN Package

Universal Non-Uniform RANdom number generators  
(Math Department University Vienna)

- ➔ provides tools to generate pretty much everything
- ➔ xdvmpGenerator:
  - ▶ Markov chain samplers for continuous multivariate distributions
  - ▶ HITRO: Hit-and-Run Sampler
- ➔ Bare minimum is implemented in Root/MathCore

## • Issues:

Requires uniform limits (domains)



Kinematically not allowed but generated  
Need to discard after generation (tries > events)

Requires to pass mode of pdf  
to UNURAN

- pdf is max at  $|t| = |t|_{\min}, x=x_{\min}, Q=Q_{\min}$
- less obvious for b, z, r

Use MINUIT (TMinuit2)

# Random Generator

- **Big Problem:** generate random numbers according to a given distribution (here 6D PDF)
- **Techniques** (good overview in Pythia6 manual chapter 4):
  - ➔ Inverse transform method (invert cumulative PDF)
    - ▶ must integrate pdf and invert (note we have a DGLAP evolution in the PDF)
  - ➔ Acceptance-rejection method (Von Neumann)
    - ▶ good if pdf is too complex
    - ▶ rather easy in 1-D, nightmare in N-D
  - ➔ and many more
  - ➔ General recommendation in all text books for N-dim: factorize
    - ▶ Problem is we cannot do that since the 6 parameters are heavily intertwined
  - ➔ Largest fraction of code in most simulators is spent on this topic

**UNURAN** to the rescue (<http://statmath.wu.ac.at/unuran/>)

# Example Main Program

```
#include "xdvmpGenerator.h"

int main(int argc, char *argv[])
{
    xdvmpGenerator generator;

    bool ok = generator.init("xdvmpRuncard.txt");

    xdvmpSettings settings = generator.runSettings(); // for convinience

    TFile *hfile = new TFile(settings.rootfile().c_str(), "RECREATE");

    TH1D *histo_r = new TH1D("histo_r", "r distribution", 200, 0., 2.);

    int nPrint = settings.numberOfEvents()/settings.timesToShow();

    unsigned long maxEvents = settings.numberOfEvents();

    generator.printEventHeader(cout);
```

# Example Runcard

```
#=====
# Comments start with a #
# Name and value are separated by a "=":  name = value
#
# The following settings are currently implemented:
# eBeamEnergy:      electron beam energy (GeV)    (default = 10)
# pBeamEnergy:      proton beam energy in (GeV)   (default = 250)
# numberOfEvents:   number of events to generate (default = 10000)
# vectorMeson:      rho | phi | jpsi  (default = rho)
# waveFunction:     GausLC | BoostedGaussian (default = BoostedGaussian)
# dipoleModel:      bSat | bCGC (default = bCGC)
# timesToShow:      # of print-outs to tell how far we are (default=0)
# rootfile:         name of root file for histos etc. (default = "")
# xmin:             min x value (default = 1e-3)
# Q2min:            min Q2 value (GeV^2)  (default = 1.)
#=====
eBeamEnergy = 10
pBeamEnergy = 250
vectorMeson = rho
dipoleModel = bSat
waveFunction = BoostedGaussian
numberOfEvents = 10000
timesToShow = 10;
rootfile = bla.root
Q2min = 1;
xmin = 1e-3;
```

# Example Output (I)

```
#=====##  
xdvmGenerator## An event generator for exclusive diffractive vector  
meson# production using the dipole model.## Code compiled on Jan  
20 2010  
16:50:46#======  
====Run started at Wed Jan 20 23:22:34 2010Runcard is  
'xdvmpRuncard.txt'mXmin = 0.001Electron beam is: 0 0 -10  
10 (0.000510999)Proton beam is: 0 0 249.998 250  
(0.93827)sqrt(s) = 100.004Initializing the xdvmp dipole model:Vector  
meson to generate: rhoDipole model used: bCGCWave function used:  
BoostedGaussian
```

# Example Output (2)

```
Range of kinematic variables (domain) used in generator:t =  
[-4, 0]Q = [1, 100.004]x = [0.001, 0.99]b = [0, 2]z =  
[1e-12, 1]r = [0.001, 2]Finding mode of pdf:mode = (t=0,  
Q=1, x=0.001, b=0.453883, z=0.5, r=0.526119; value of pdf =  
107769)Initializing the random generator:Dimensions used:  
6pdf in log: noNumber of events to process:  
10000xdvmpGenerator is initialized.
```

For bCGC this takes  $< 1$  s

For bSat  $\sim 1$ -2 min (due to DGLAP setup)



# Example Event Record

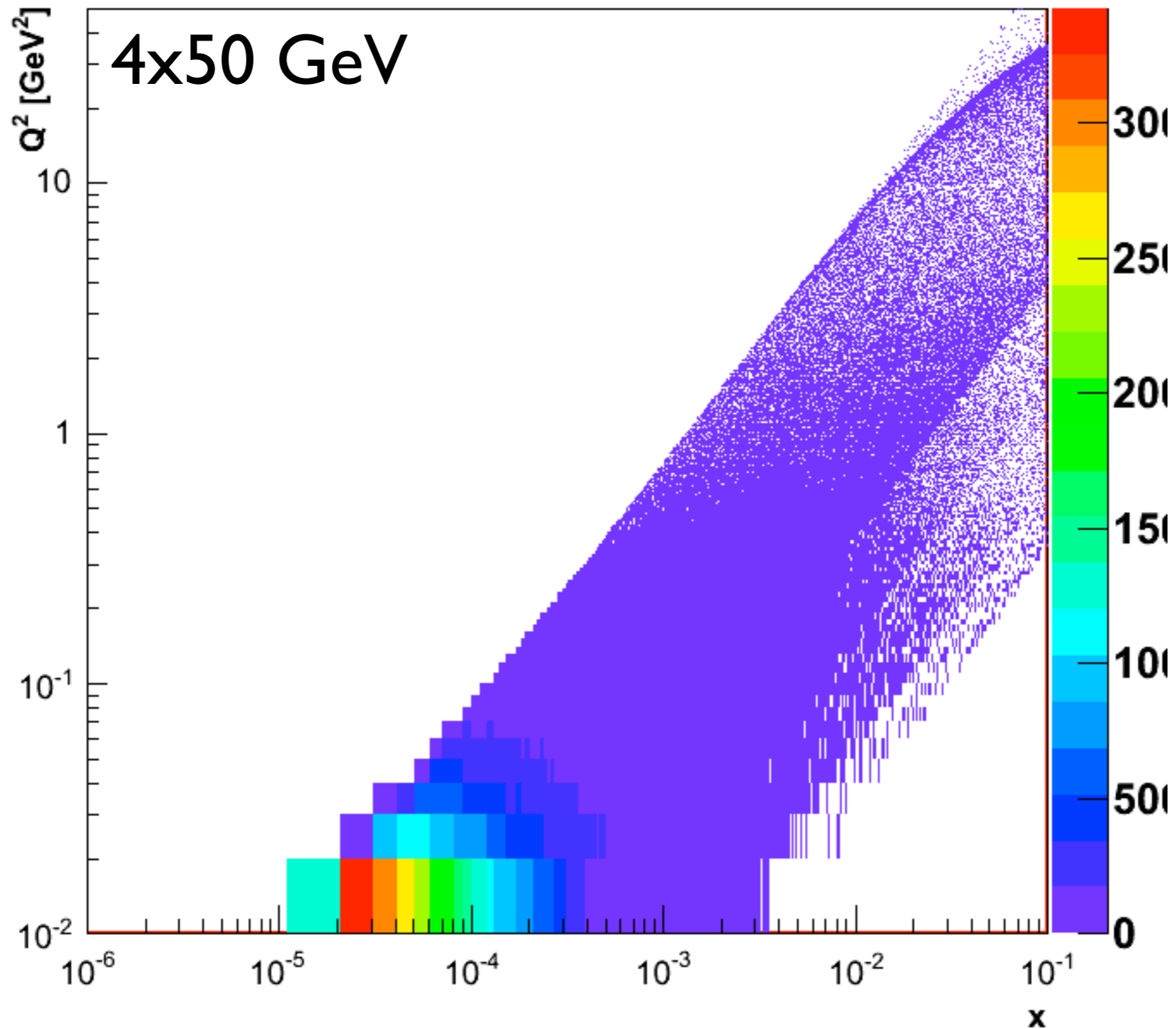
```

xdvmpGen event file=====iEvent, t, Q2, x, y, b, z, r,
s=====i, id, px, py, px, E, m, vx, vy,
vz=====processed 0 events1 -0.171395 2.03611 0.00254752 0.0799258
0.525637 0.380722 0.344587 10000.8=====1 11 0
0 -10 250 10 0.000510999 0 0 0 02 2212 0 0
249.998 250 0.93827 0 0 03 11 -0.00222092 1.36871
-9.14977 9.25157 0.000510999 0 0 04 2212 0.214882 0.352692
248.818 248.82 0.93827 0 0 05 113 -0.212661 -1.7214
0.33036 1.92867 0.776 0 0 0===== End Event Record =====2
-0.171395 2.03611 0.00254752 0.0799258 0.525637 0.380722 0.554715
10000.8=====1 11 0 0 -10 10
0.000510999 0 0 0 02 2212 0 0 249.998 250
0.93827 0 0 0 03 11 1.34006 -0.278549 -9.14977 9.25157
0.000510999 0 0 0 04 2212 0.390437 -0.134496 248.769 248.771
0.93827 0 0 0 05 113 -1.7305 0.413045 0.379414 1.97772
0.776 0 0 0 0===== End Event Record =====

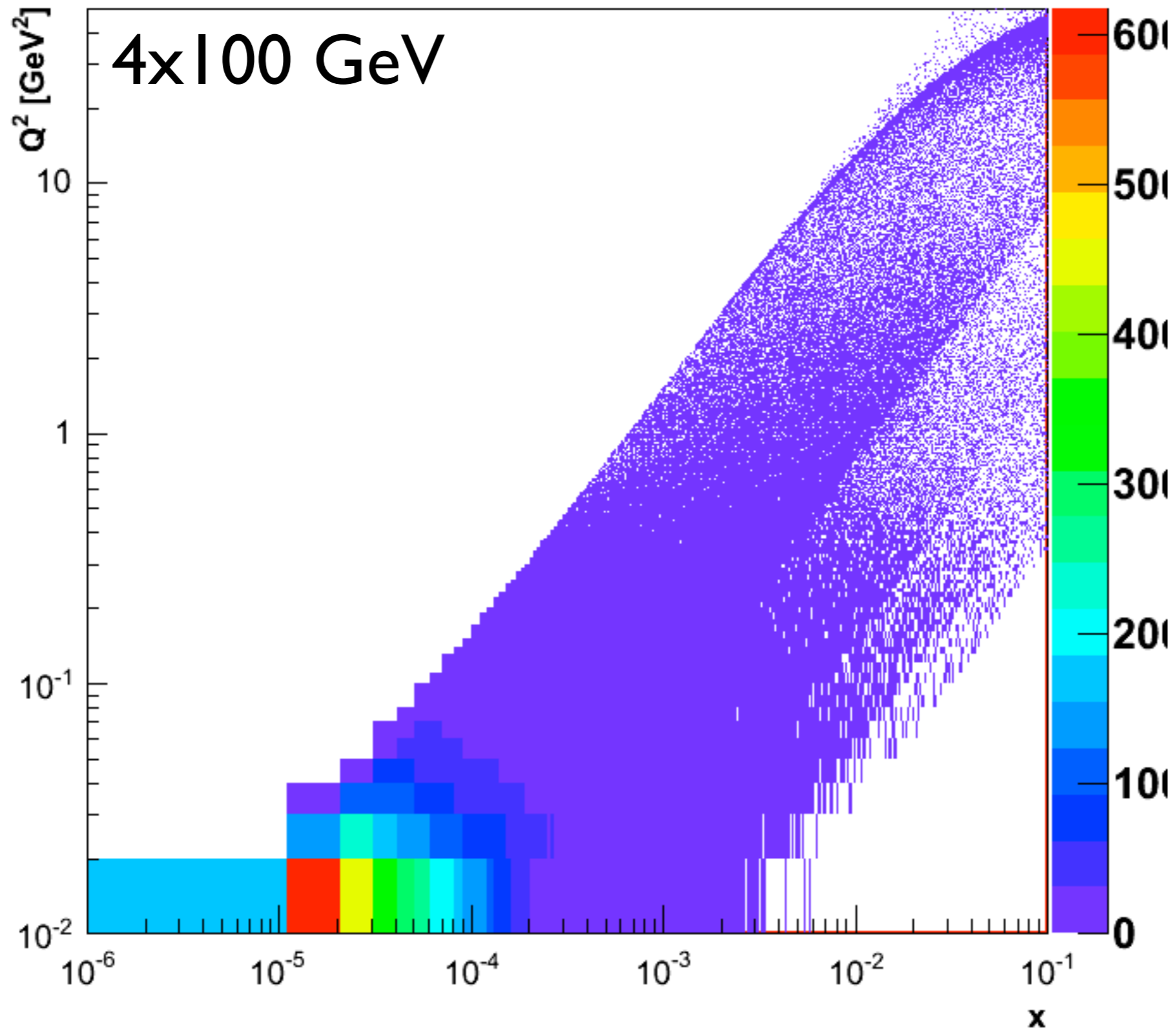
```

- Note the VM does not decay (GEANT can do this if needed)
- VM have zero width (should probably change that)
- The event record can be directly written into a ROOT Tree or any other format, the print-out shown here is optional
- Time to generate **IM events** ~ 4 min on Thomas' 3y old MacBook Pro

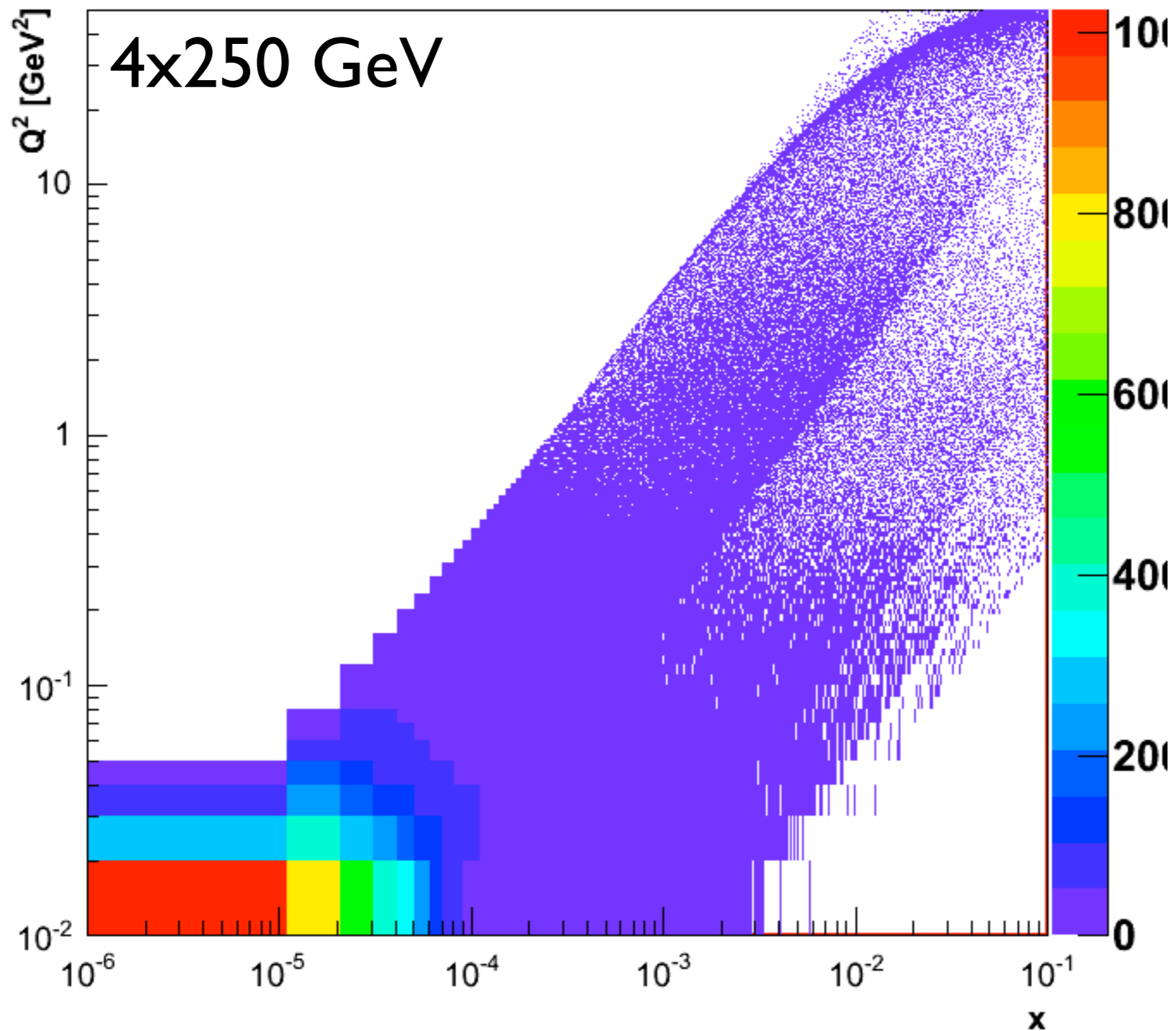
# $x$ - $Q^2$ acceptance vs energy



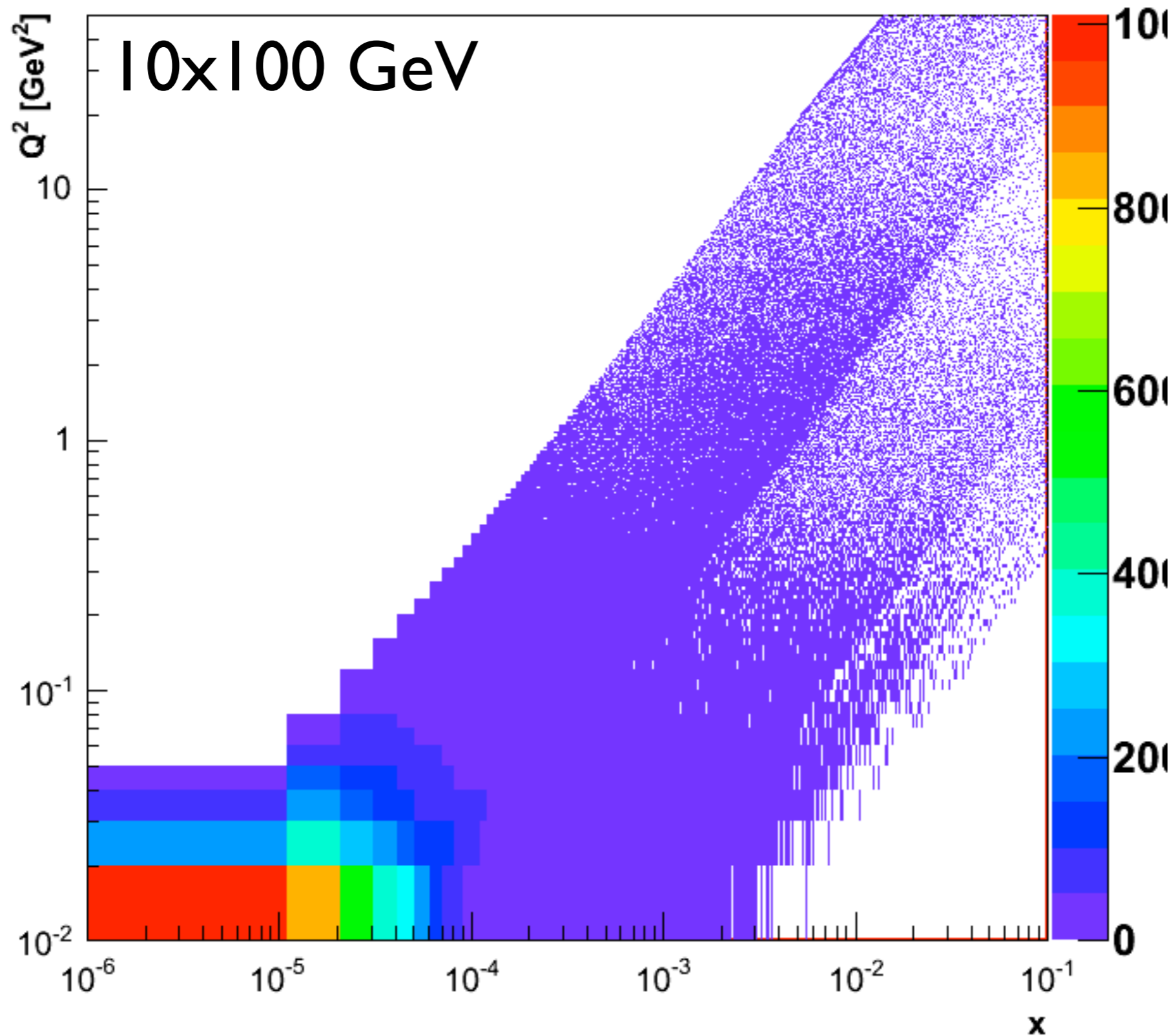
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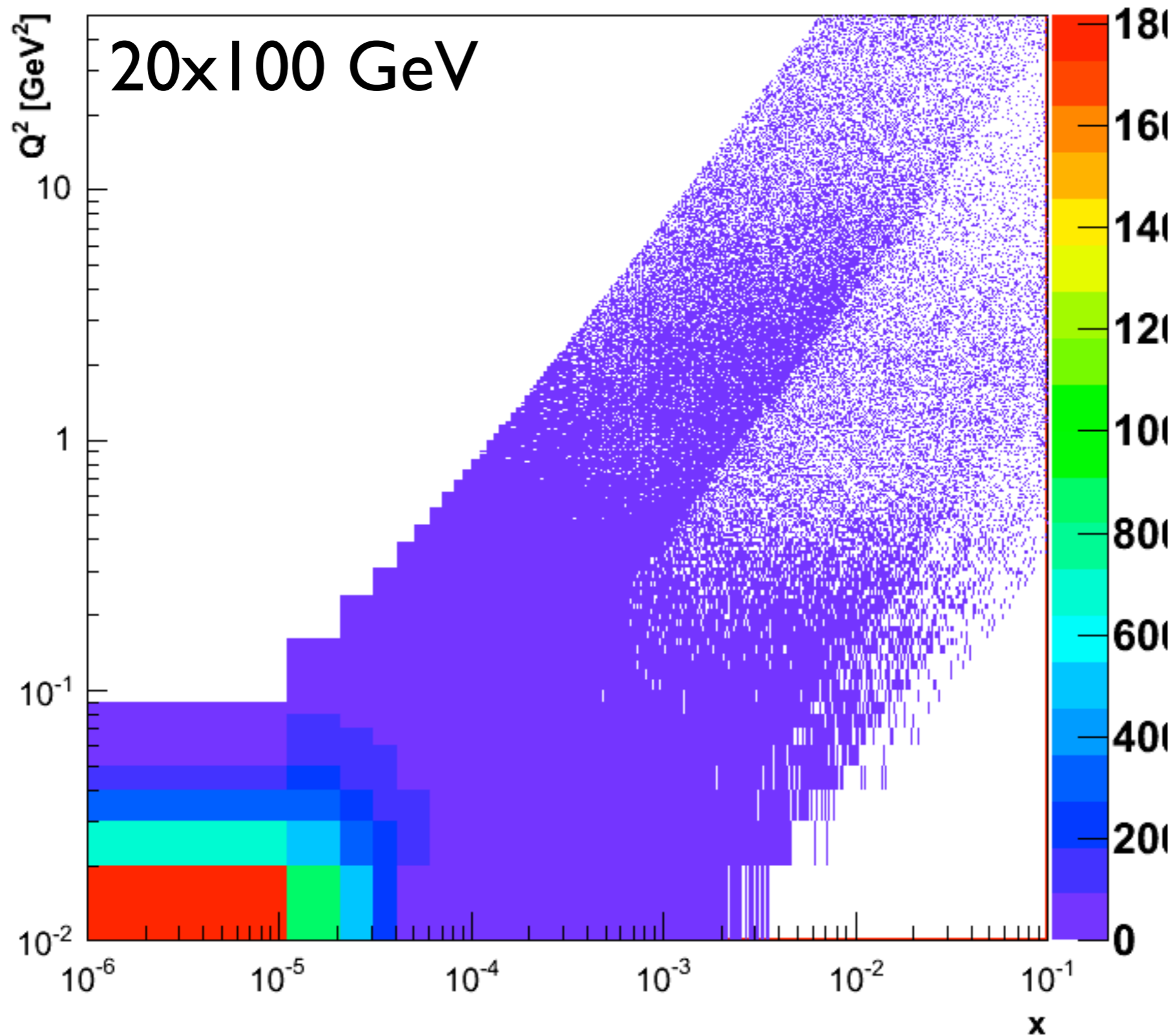
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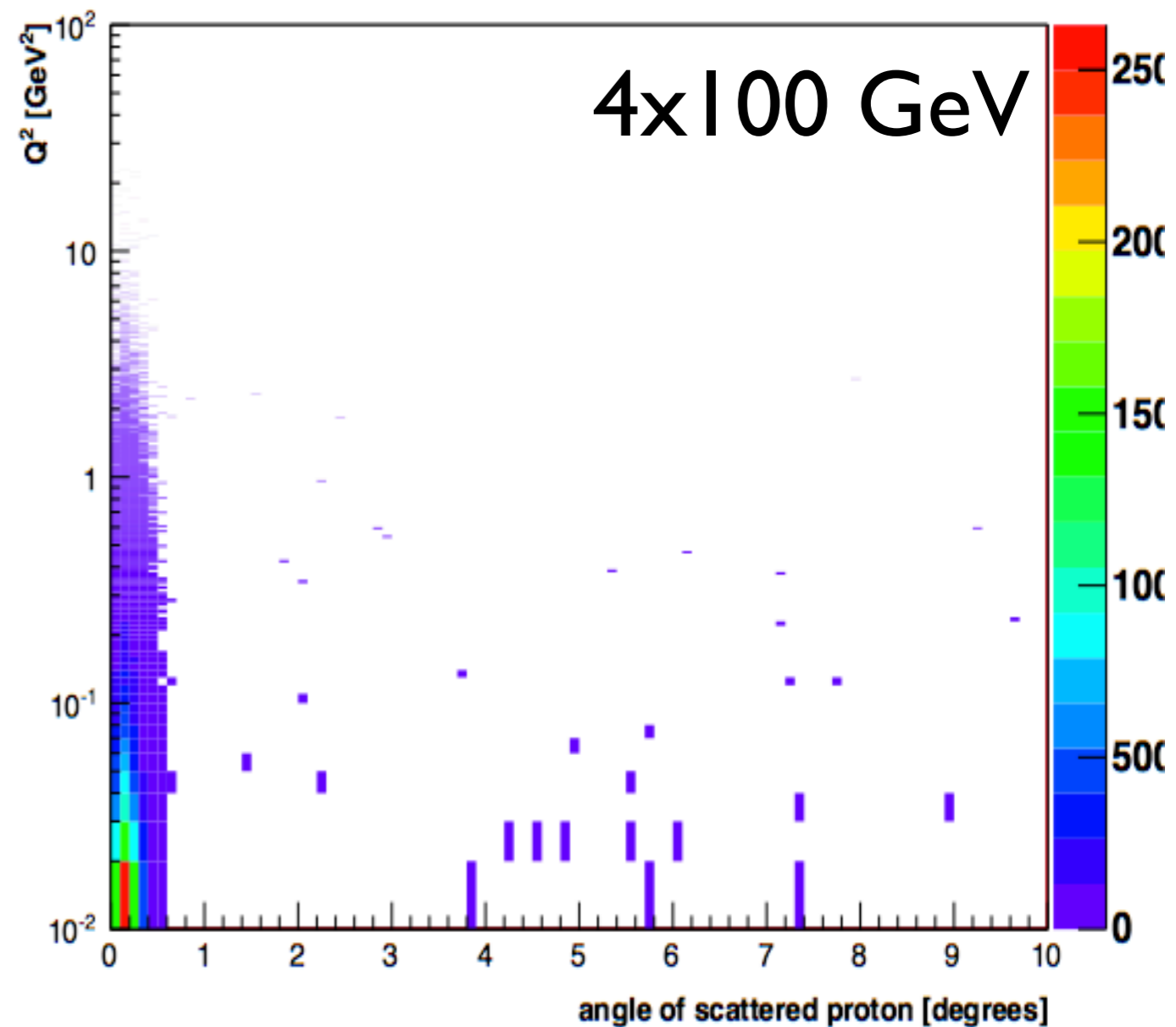
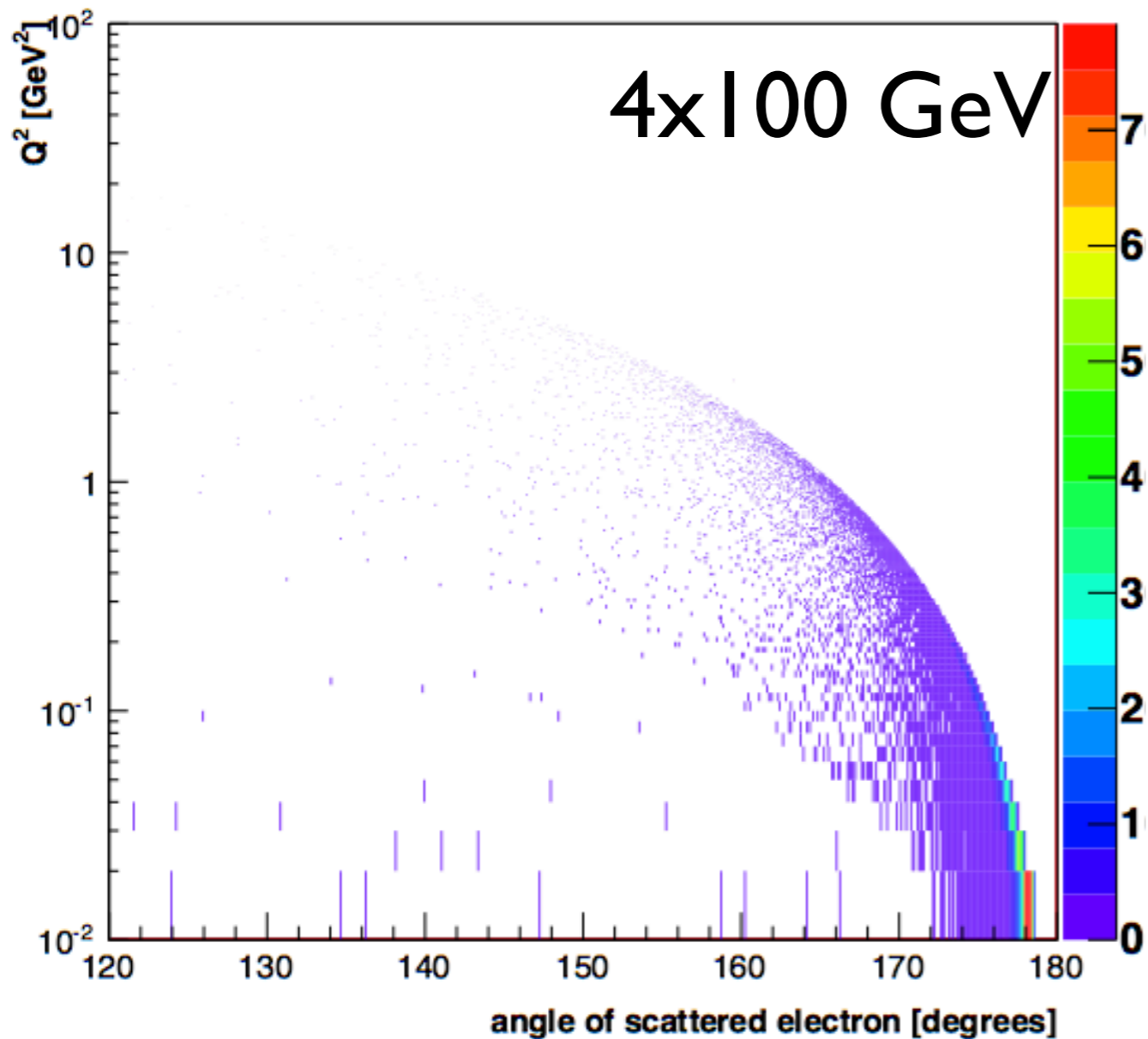
# $x$ - $Q^2$ acceptance vs energy



# electron and proton angles vs $Q^2$

electron

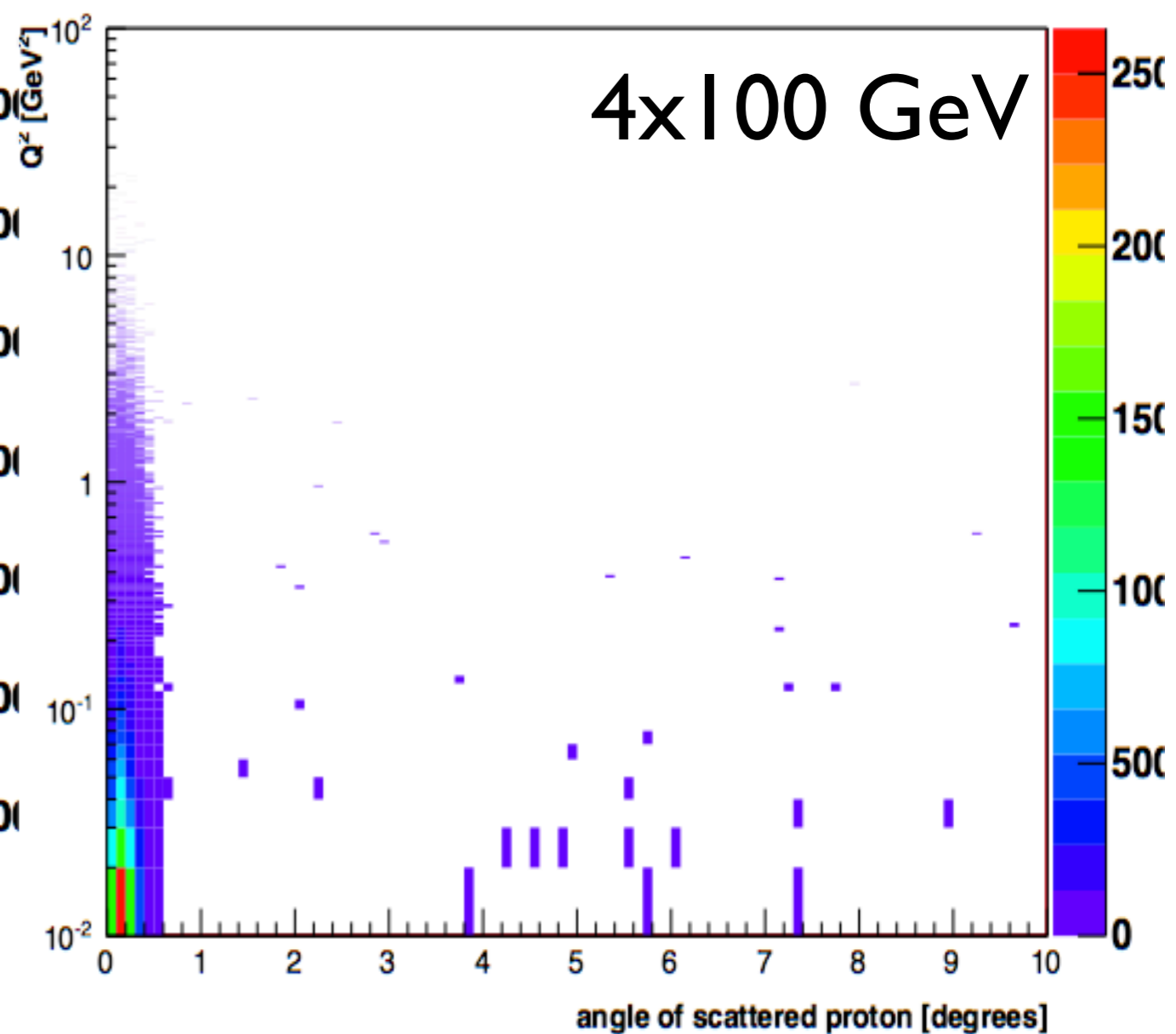
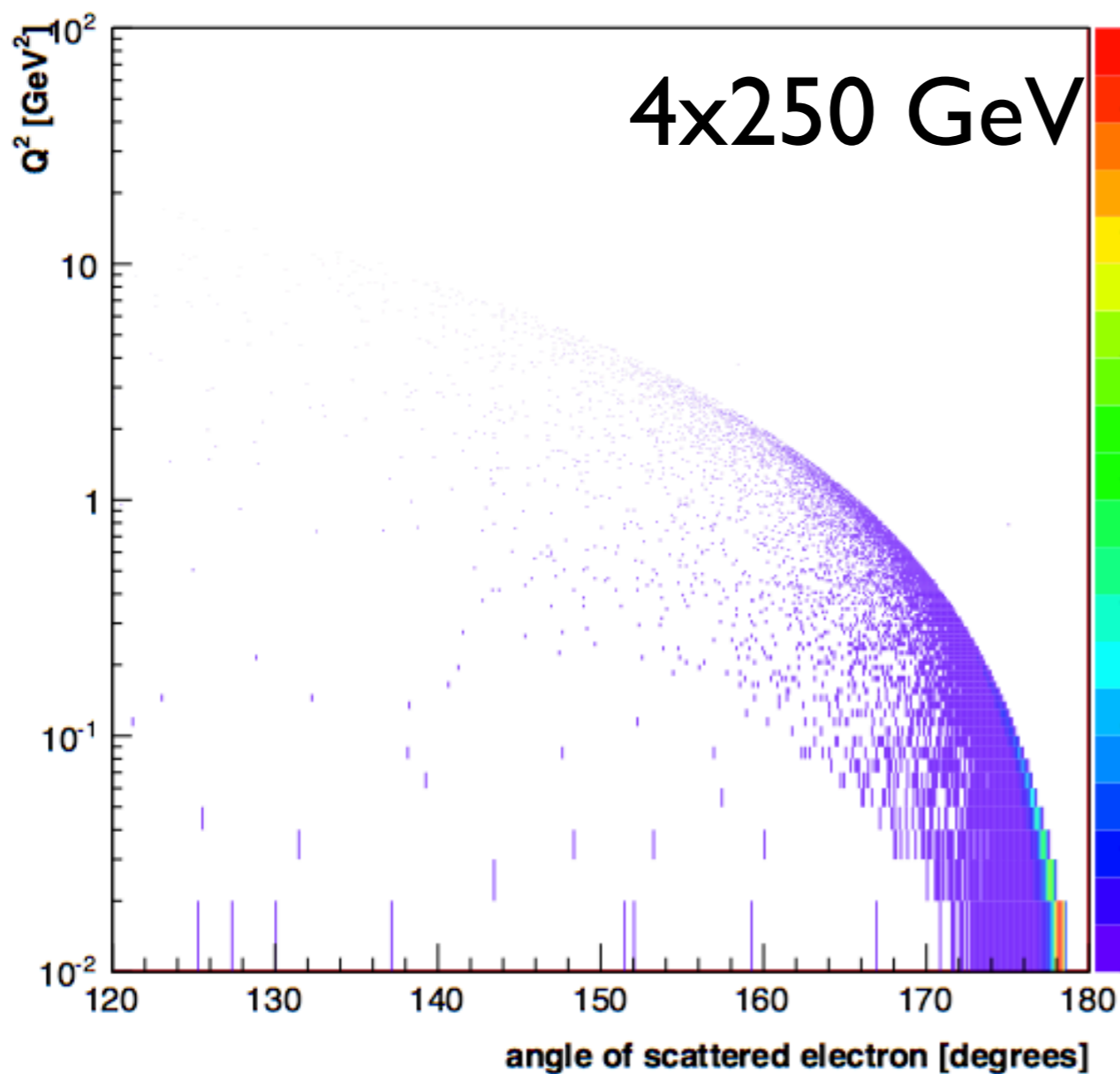
proton



# electron and proton angles vs $Q^2$

electron

proton

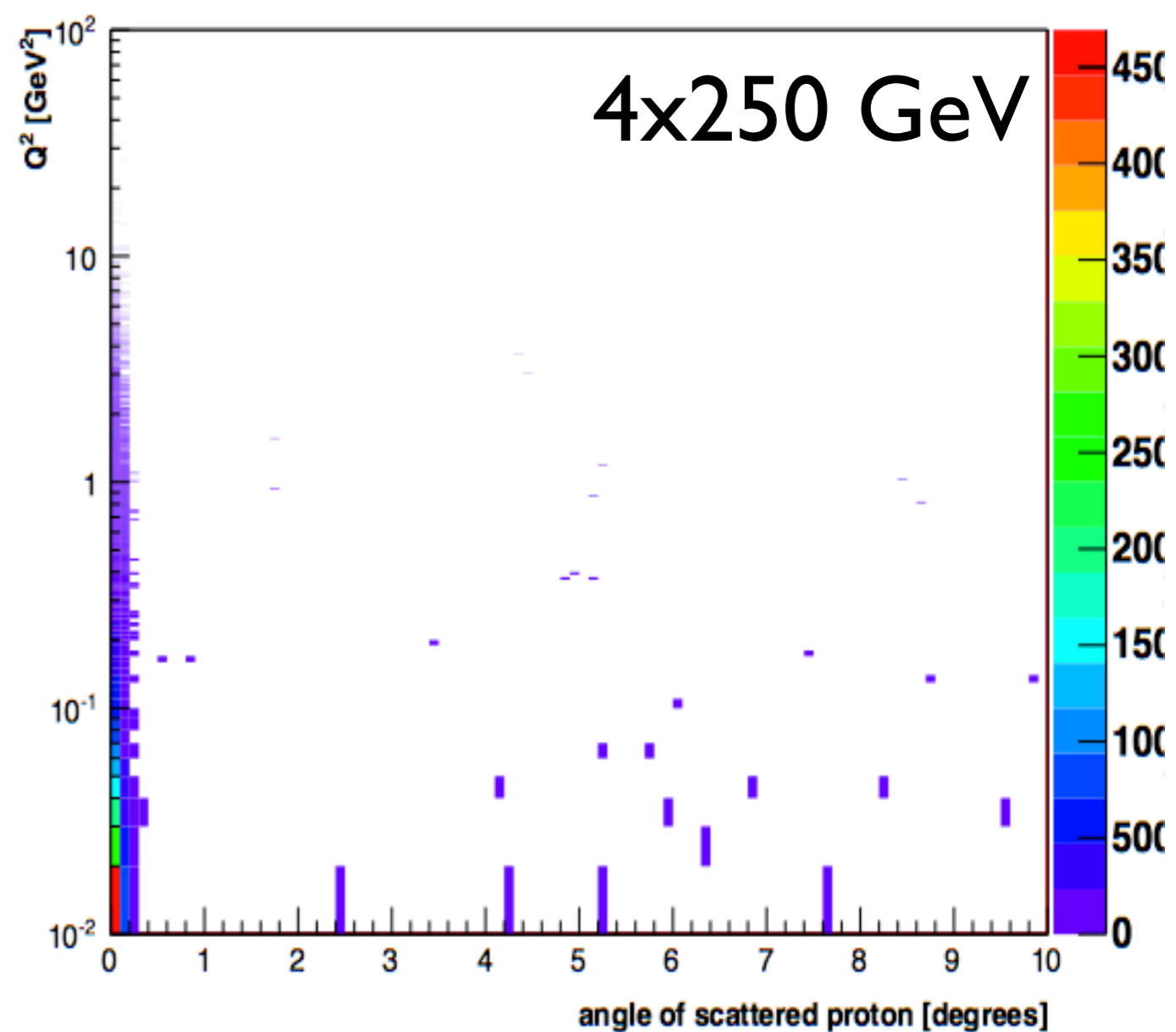
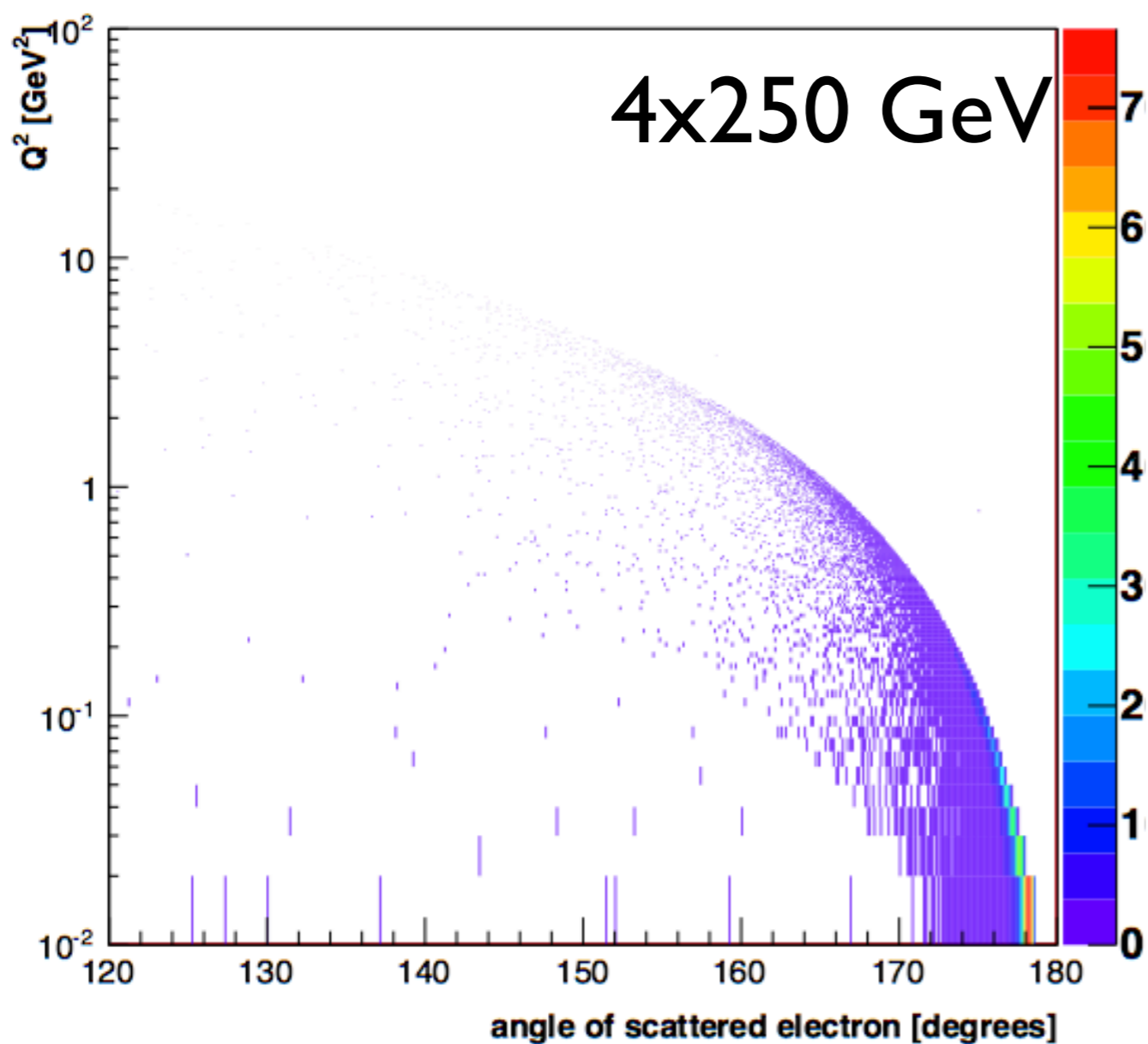




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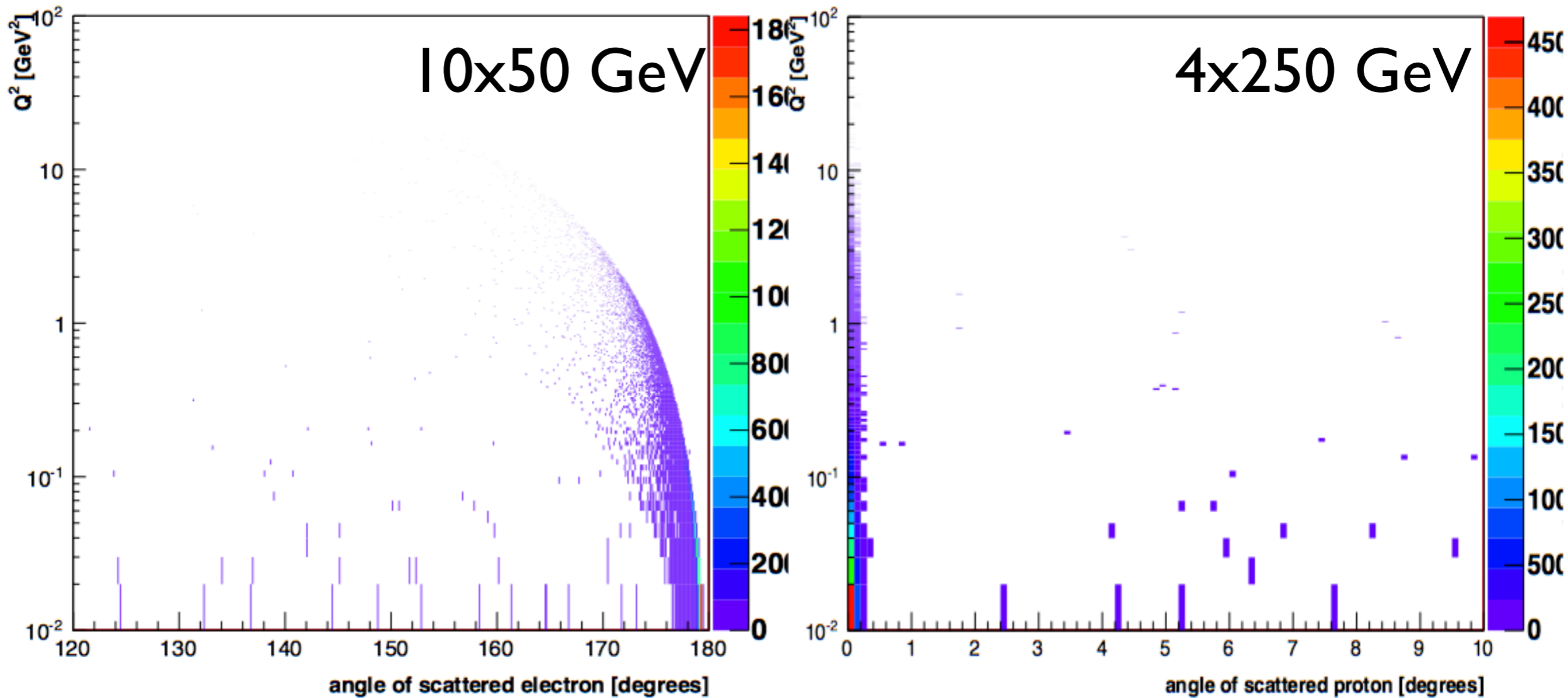
proton



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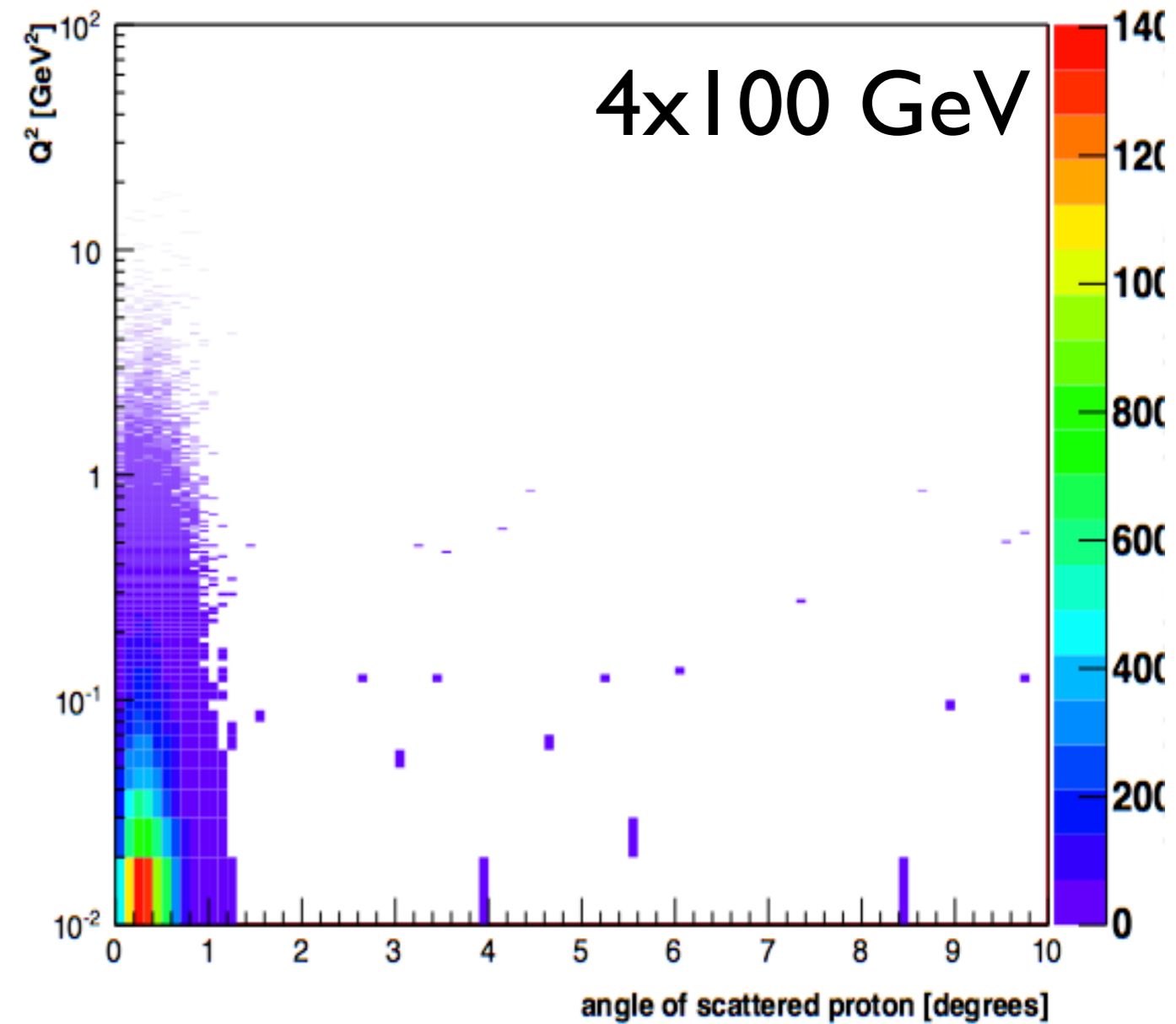
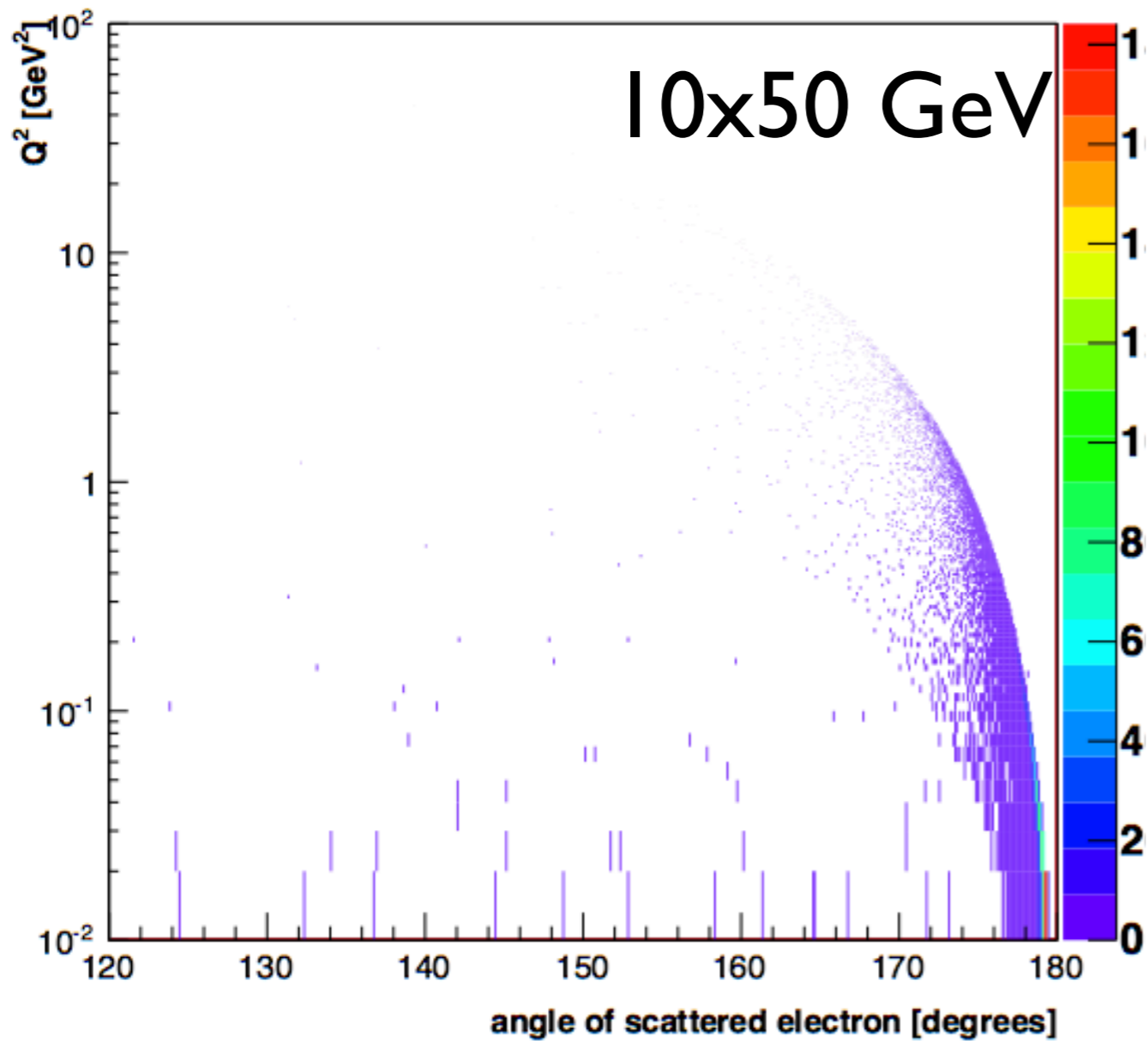
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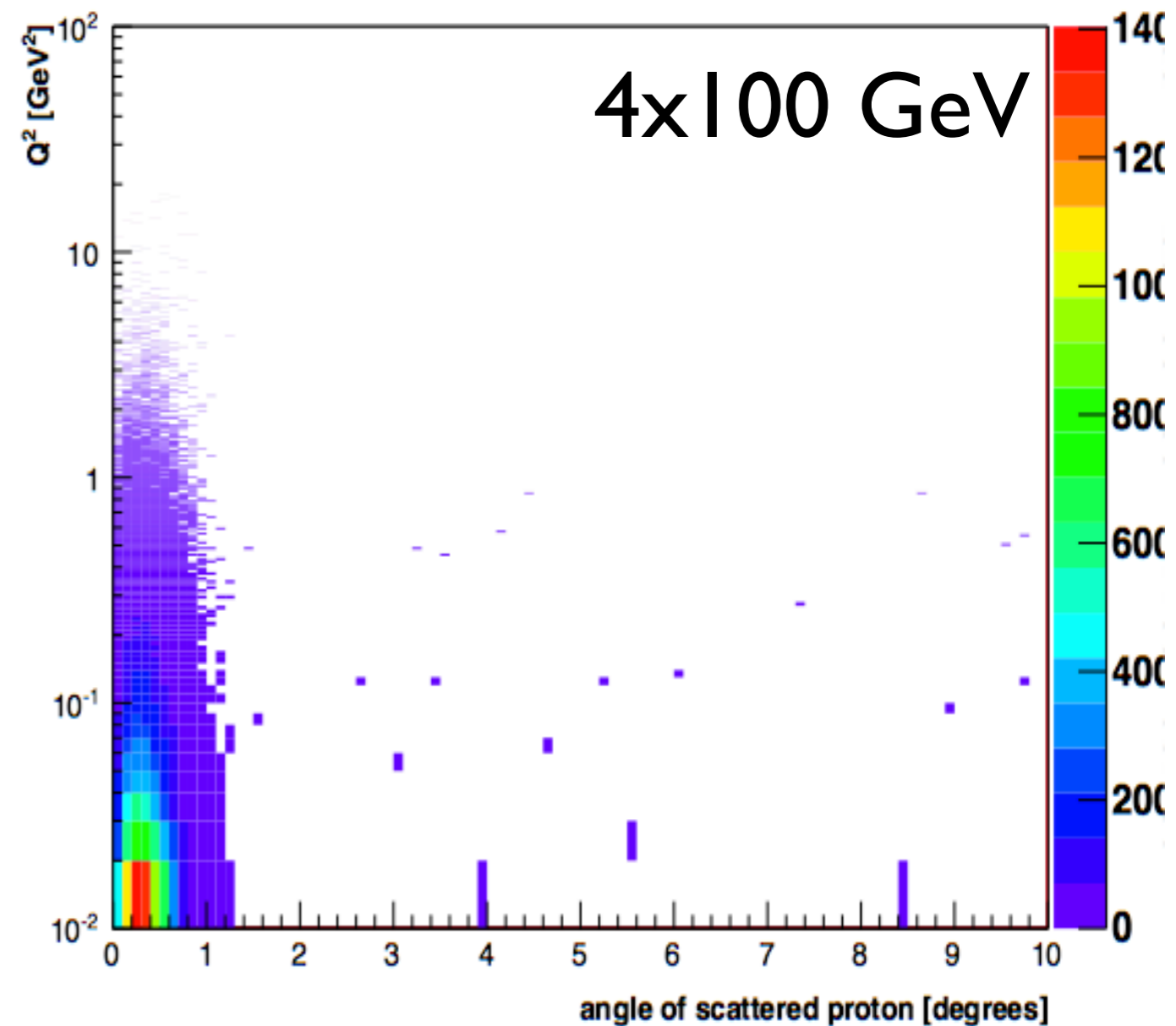
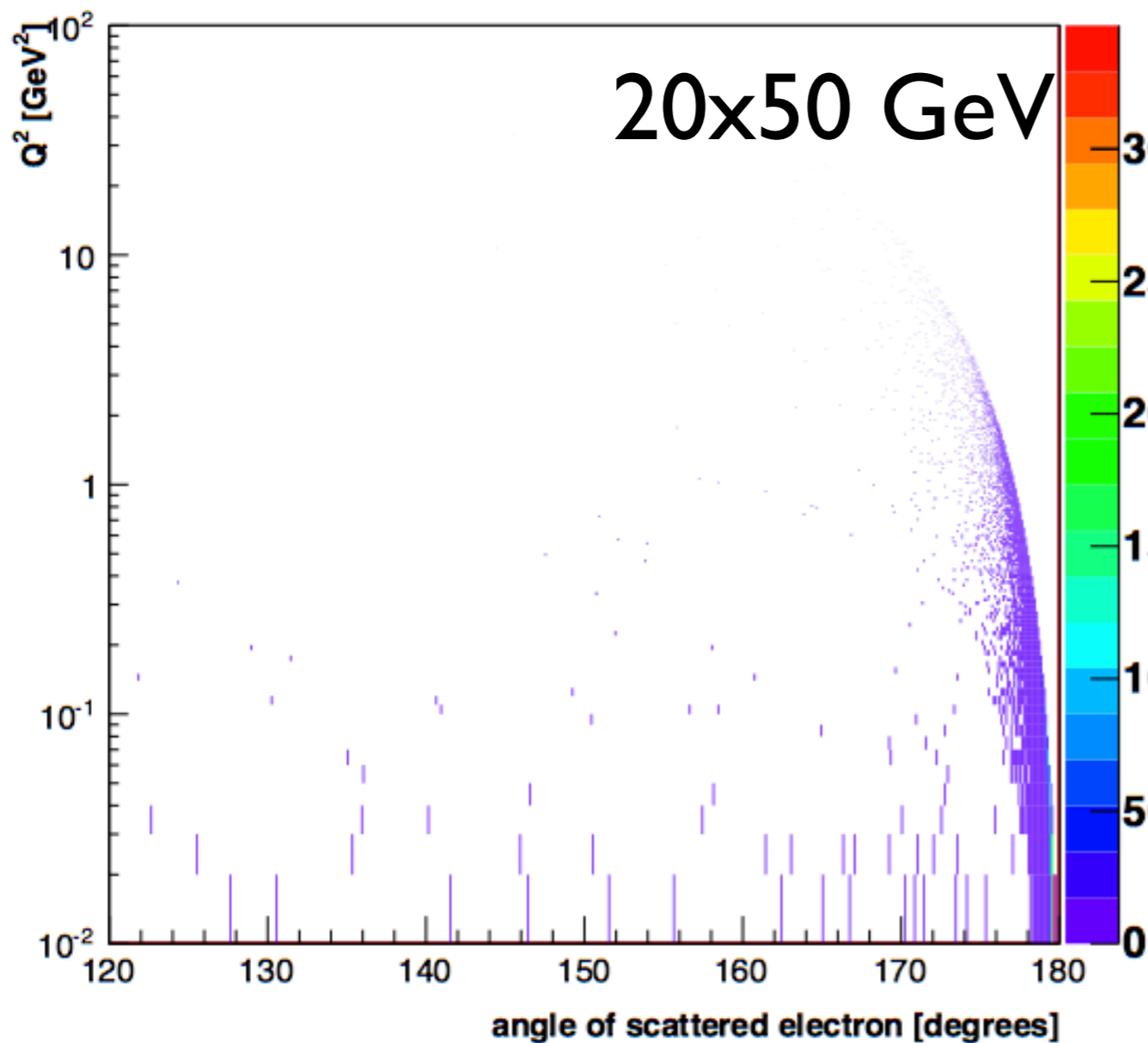
proton



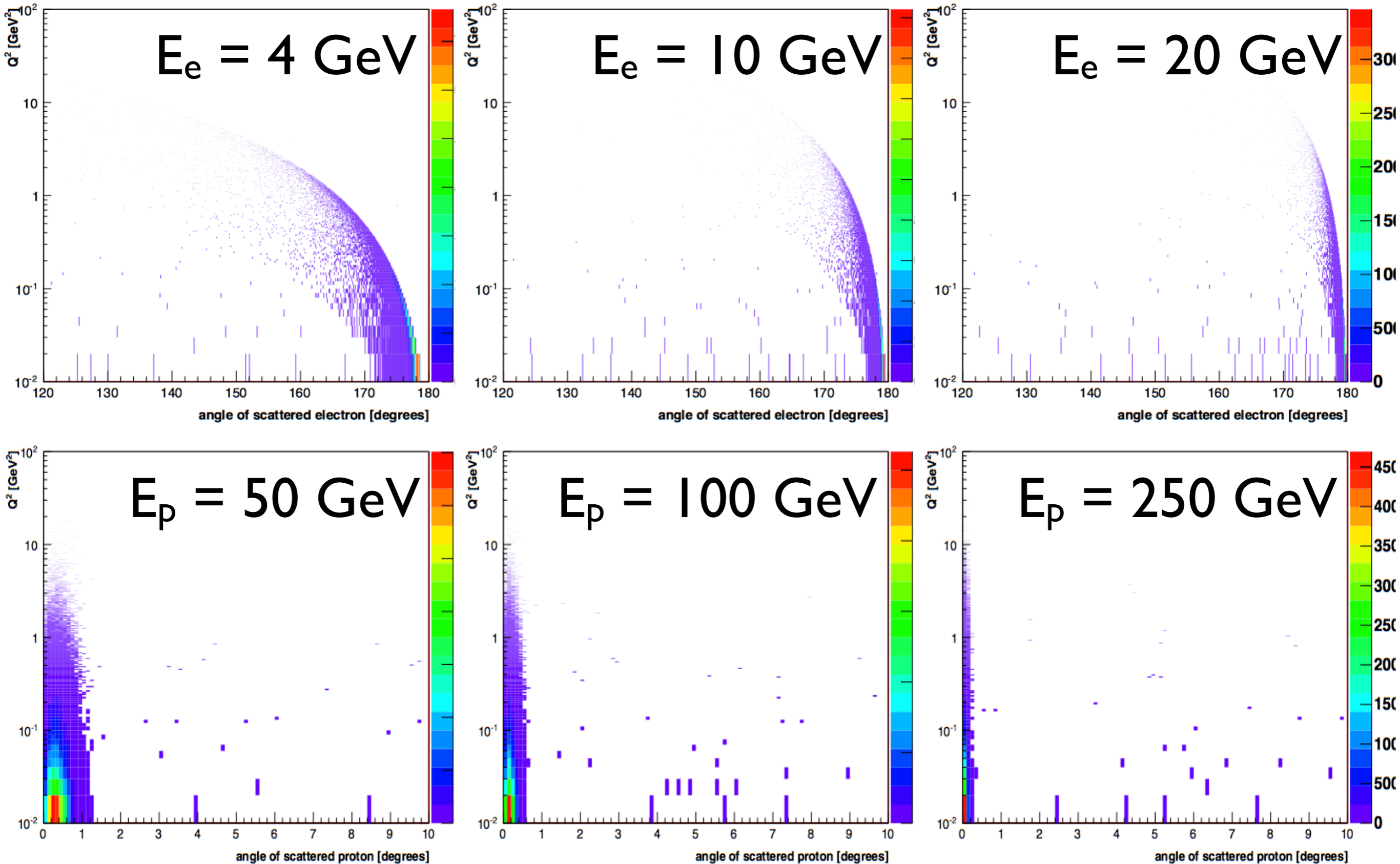
# electron and proton angles vs $Q^2$

electron

proton

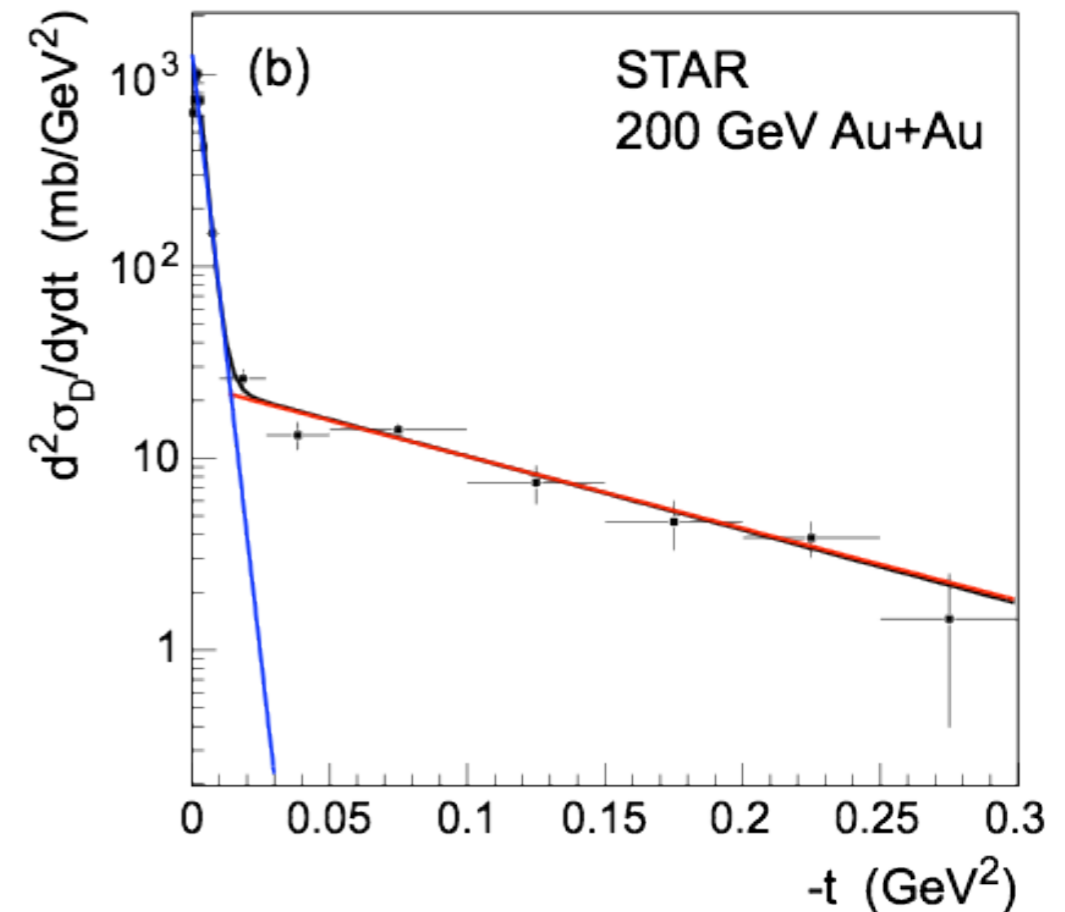
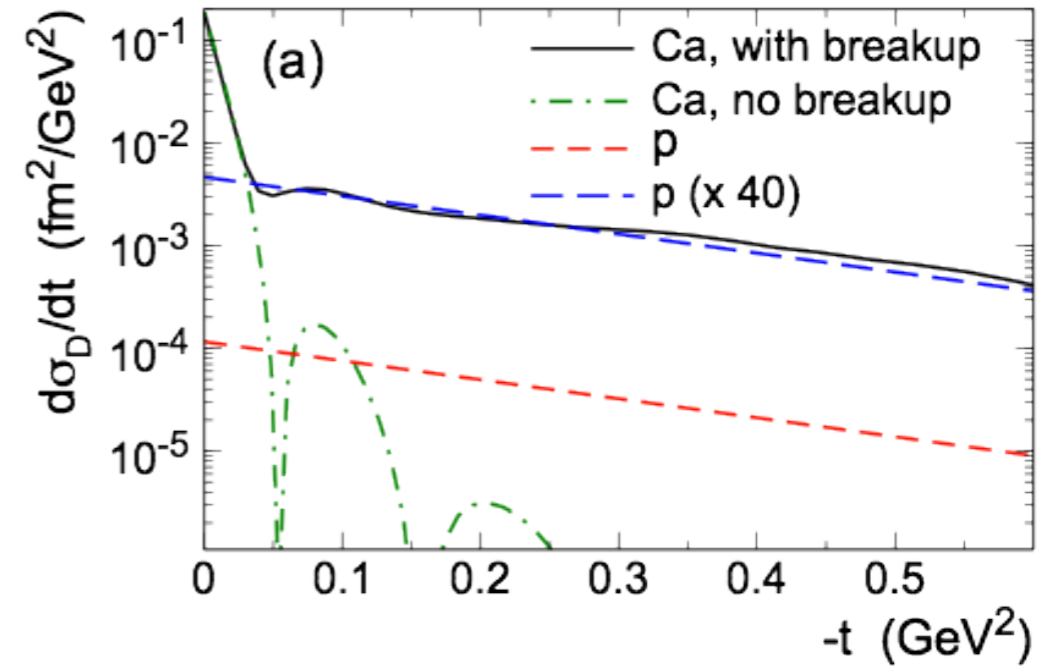


# electron and proton angles vs $Q^2$



# How to measure coherent diffraction in e+A ?

$$\frac{d\sigma}{dt} \Big|_{t=0} (\gamma^* A \rightarrow VA) \propto \alpha_s^2 [G_A(x, Q^2)]^2$$



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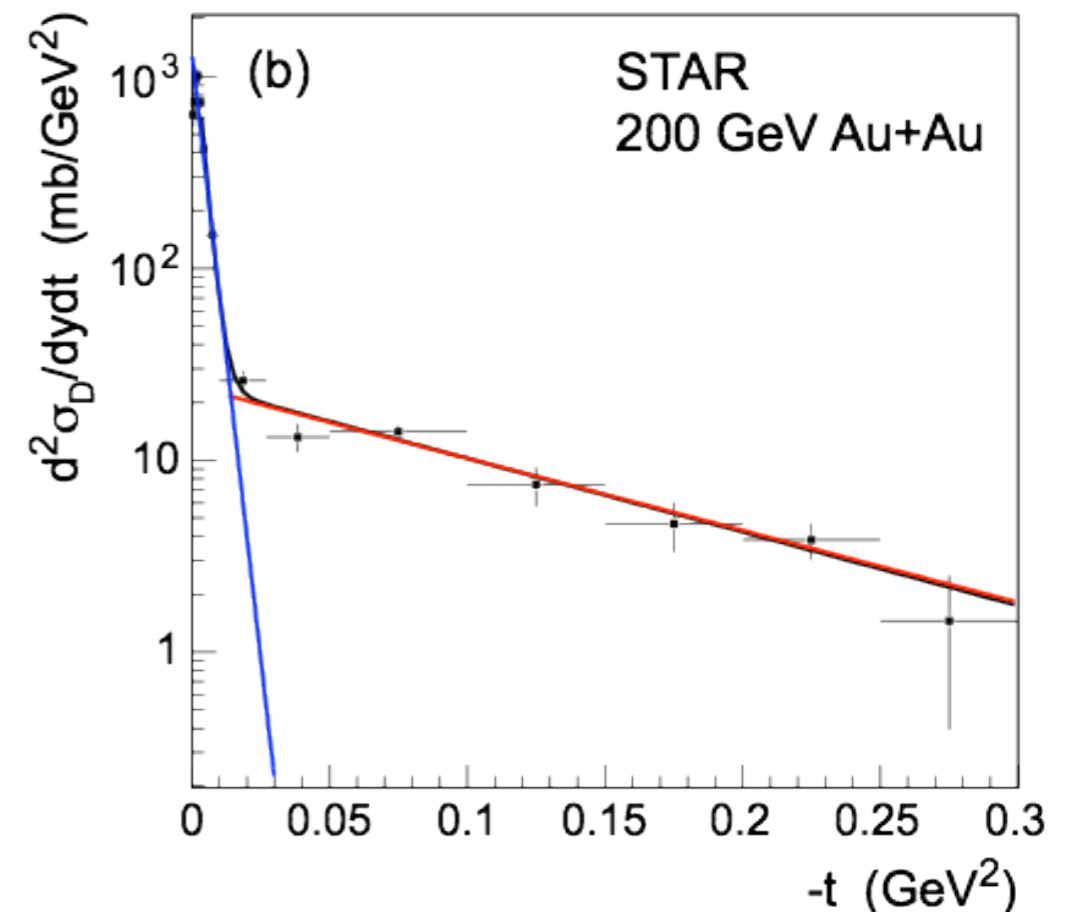
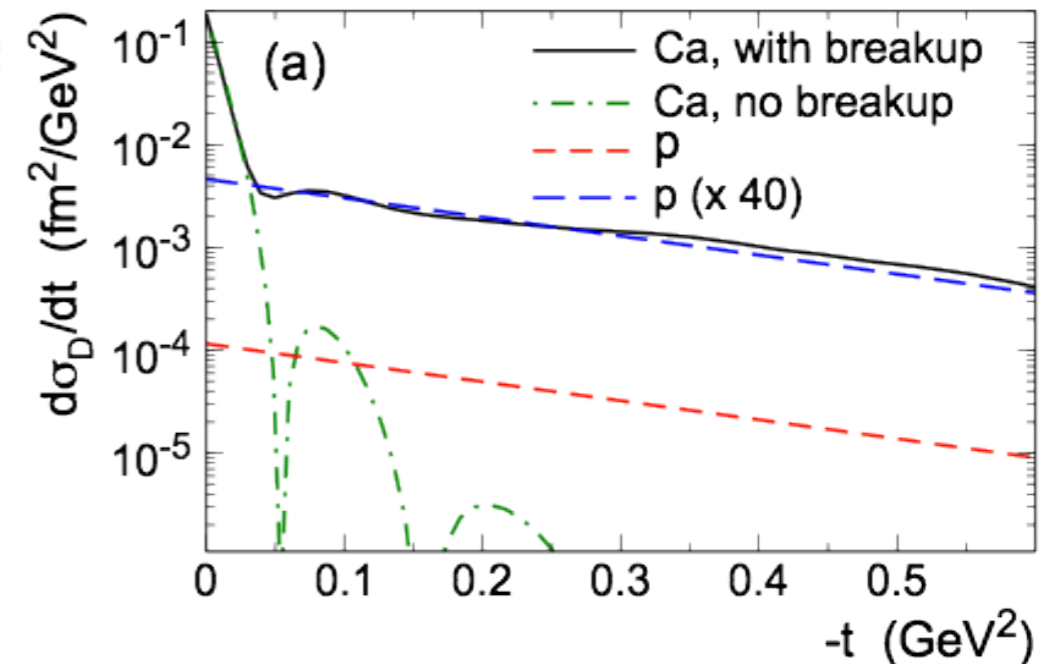
$$\frac{d\sigma}{dt} \Big|_{t=0} (\gamma^* A \rightarrow VA) \propto \alpha_s^2 [G_A(x, Q^2)]^2$$

- Coherent diffraction == low t
- Can measure the nucleus if it is separated from the beam in Si (Roman Pot) “beamline” detectors

$$\rightarrow p_T^{\min} \sim pA\theta_{\min}$$

- ▶ For beam energies = 100 GeV/n and  $\theta_{\min} = 0.08$  mrad:

- These are large momentum kicks,  $\gg$  the binding energy ( $\sim 8$  MeV)



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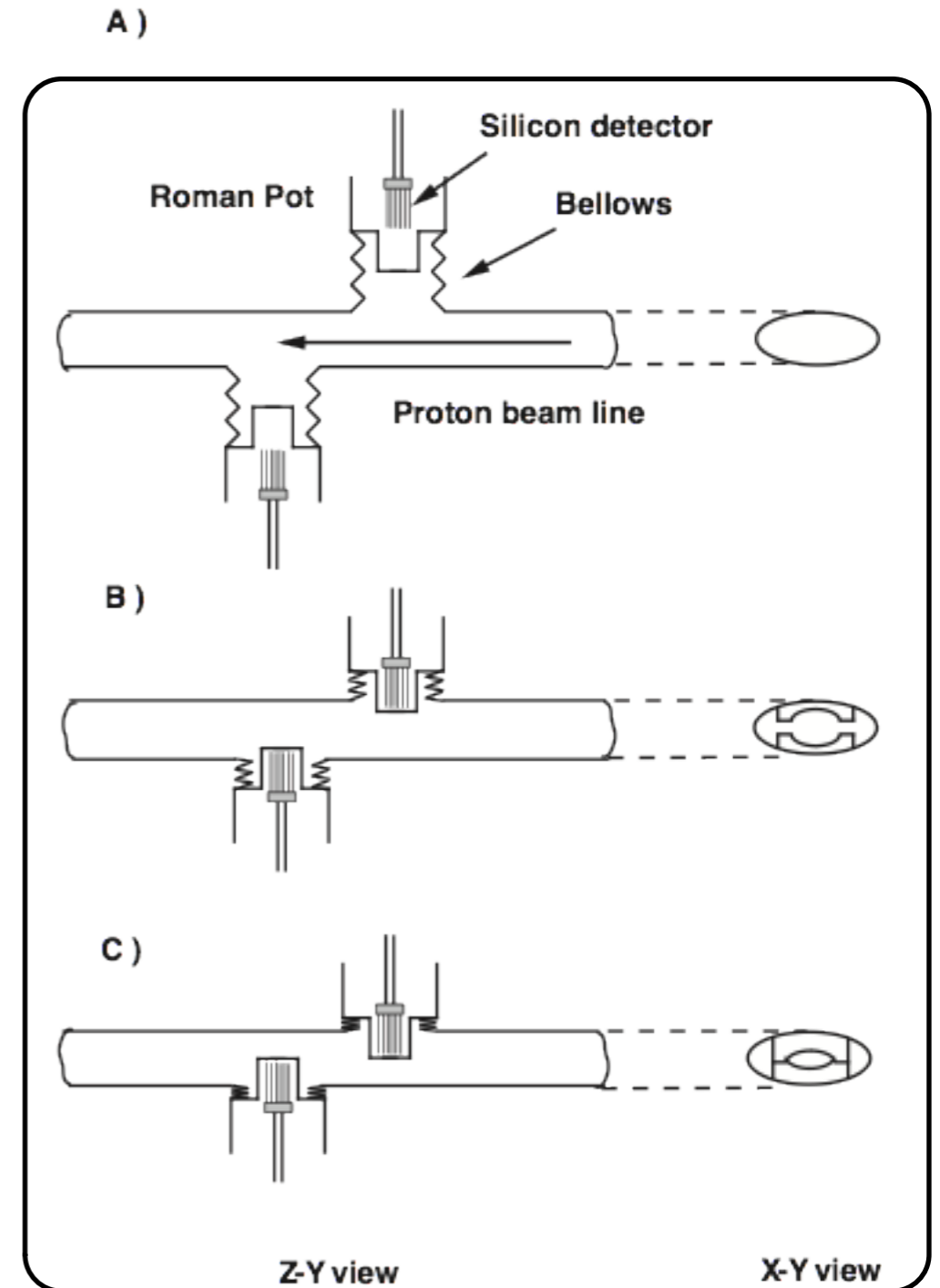
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species (A)	$p_T^{\min}$ (GeV/c)
d (2)	0.02
Si (28)	0.22
Cu (63)	0.51
In (115)	0.92
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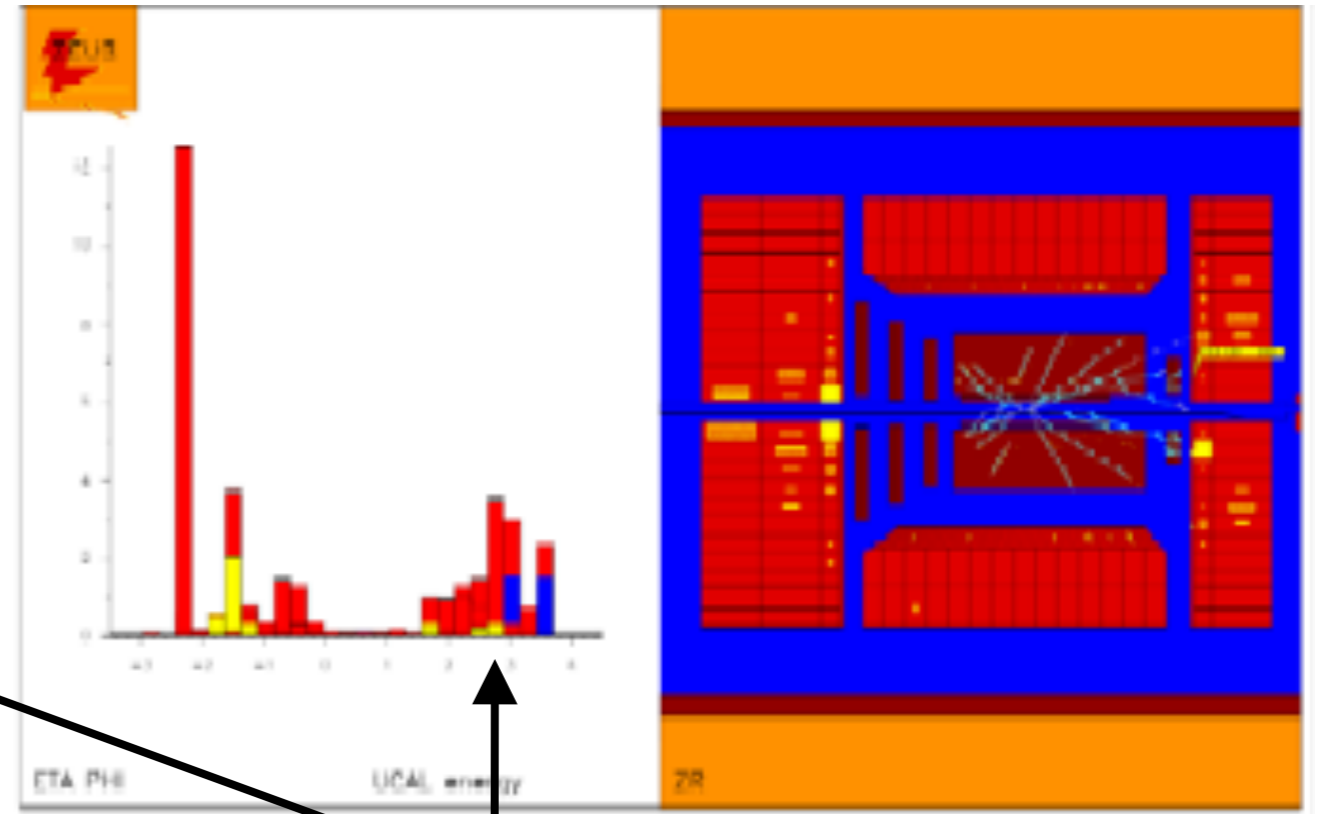
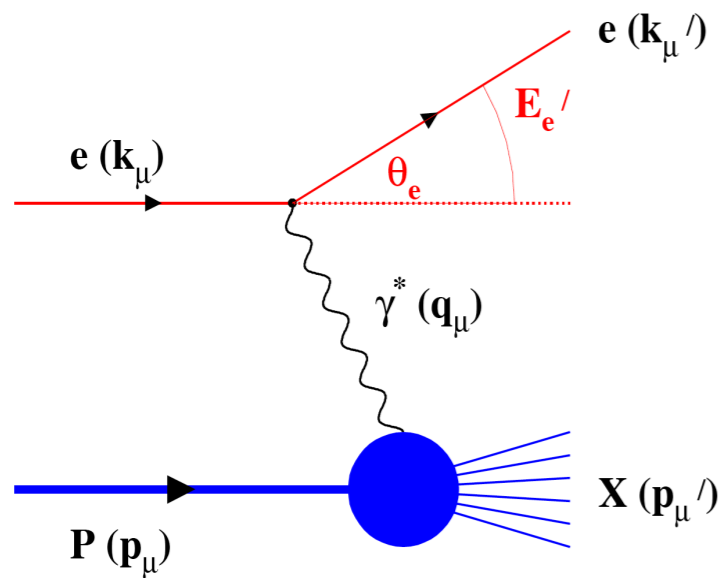
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For large A, nucleus cannot be separated from beam  
without breaking up

# Diffraction Physics in $e+A$

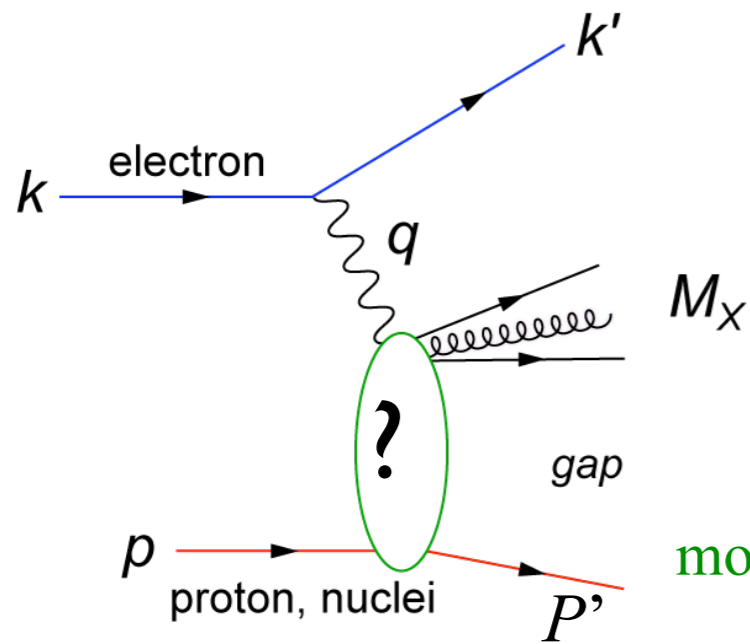
‘Standard DIS event’



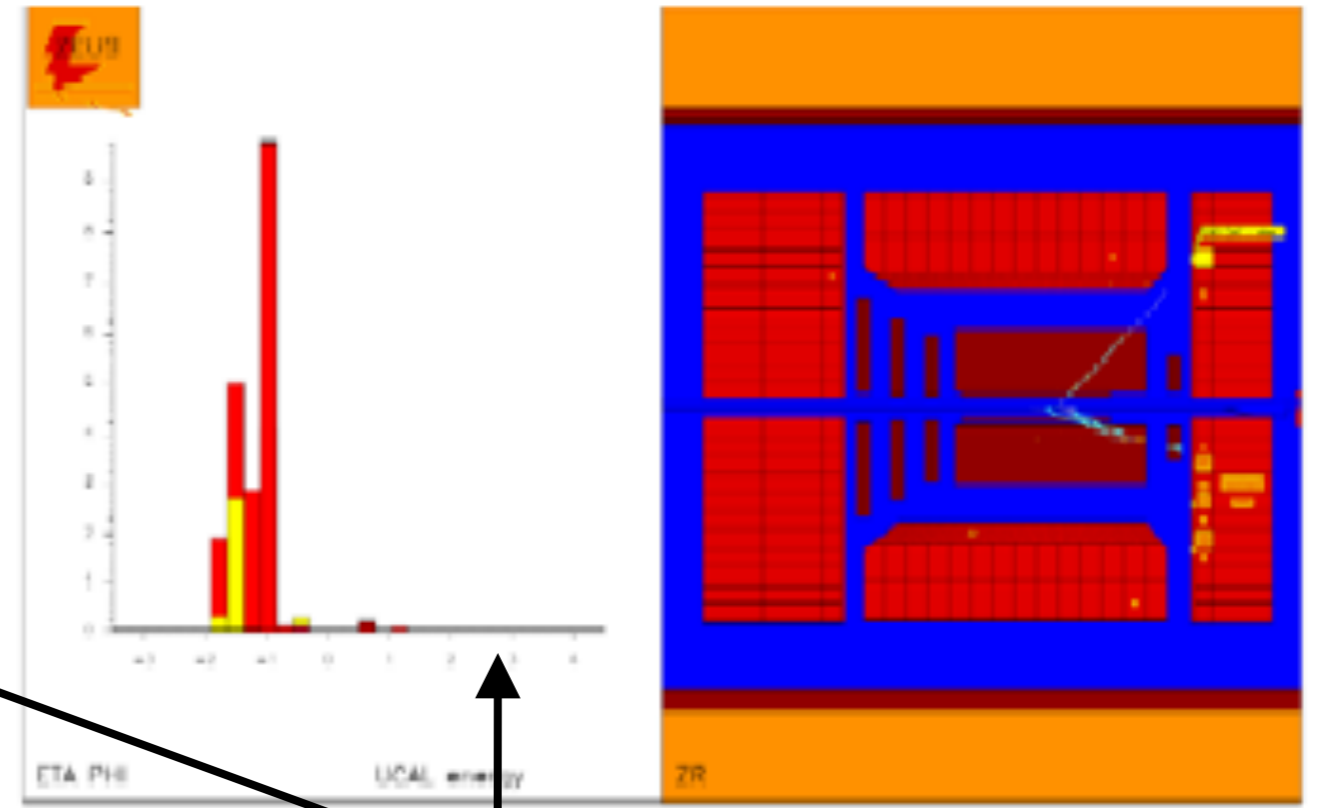
Activity in proton direction

# Diffractive Physics in $e+A$

## Diffractive event



momentum transfer:  
 $t = (P - P')^2$

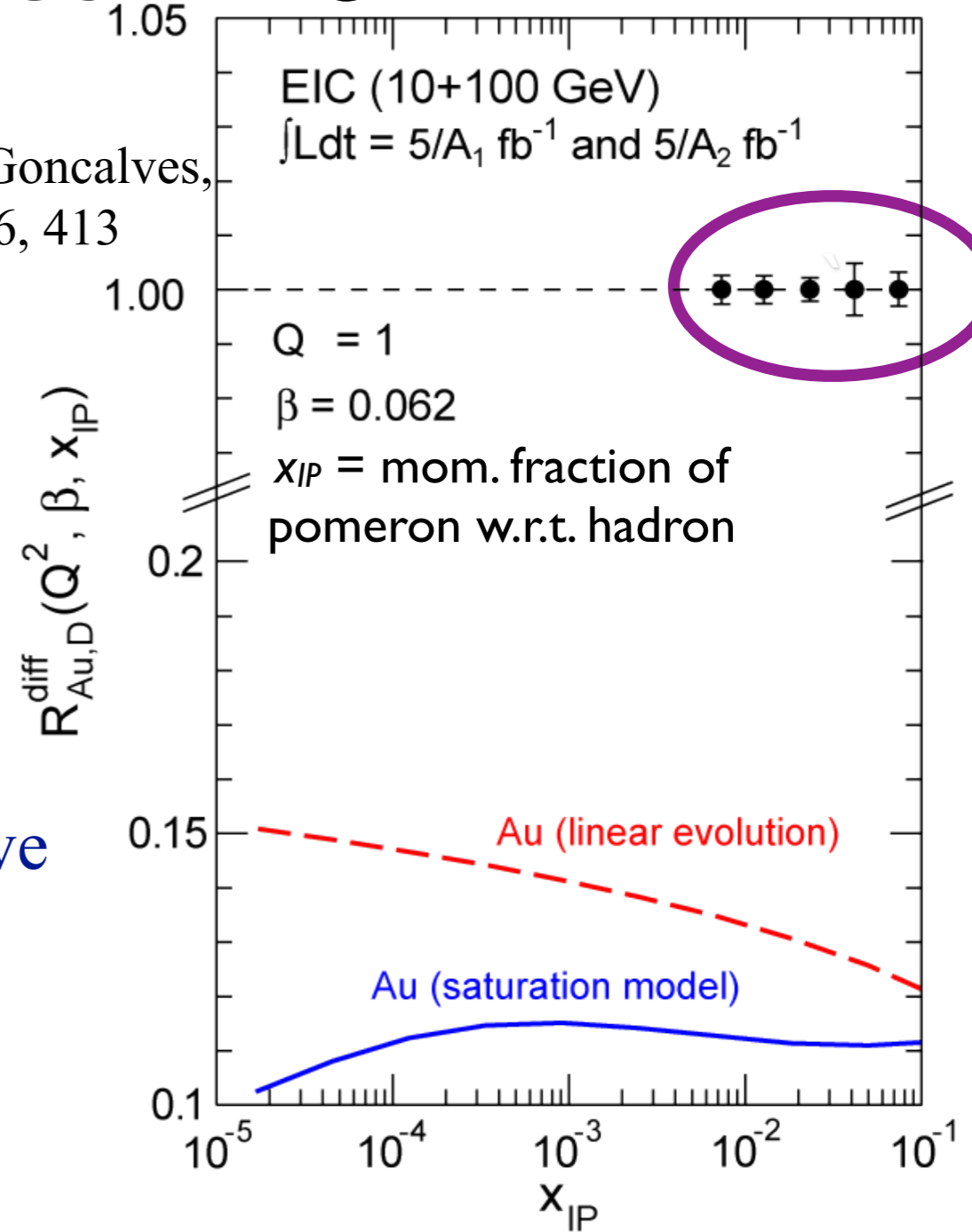
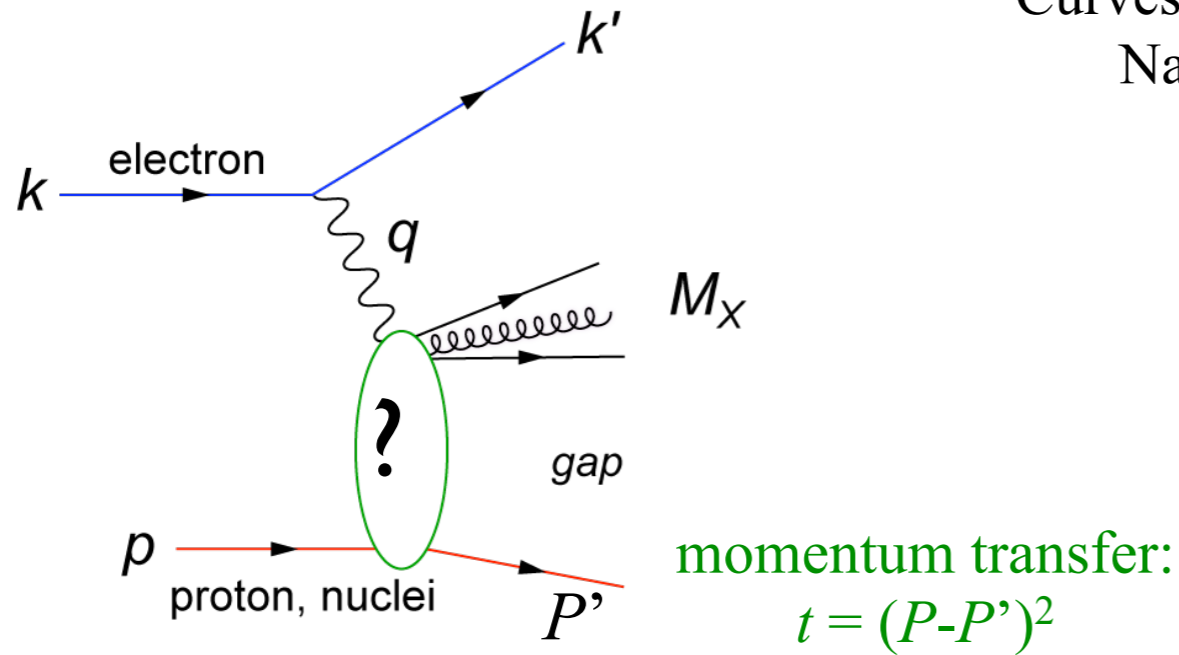


Activity in proton direction

- HERA/ep: 15% of all events are hard diffractive
- Diffractive cross-section  $\sigma_{\text{diff}}/\sigma_{\text{tot}}$  in  $e+A$  ?
- ➔ Predictions: ~25-40%?
- Look inside the “Pomeron”
- ➔ Diffractive structure functions
- ➔ Exclusive Diffractive vector meson production:  $d\sigma/dt \sim [xG(x, Q^2)]^2$  !!

# Diffraction Physics in $e+A$

## Diffraction event



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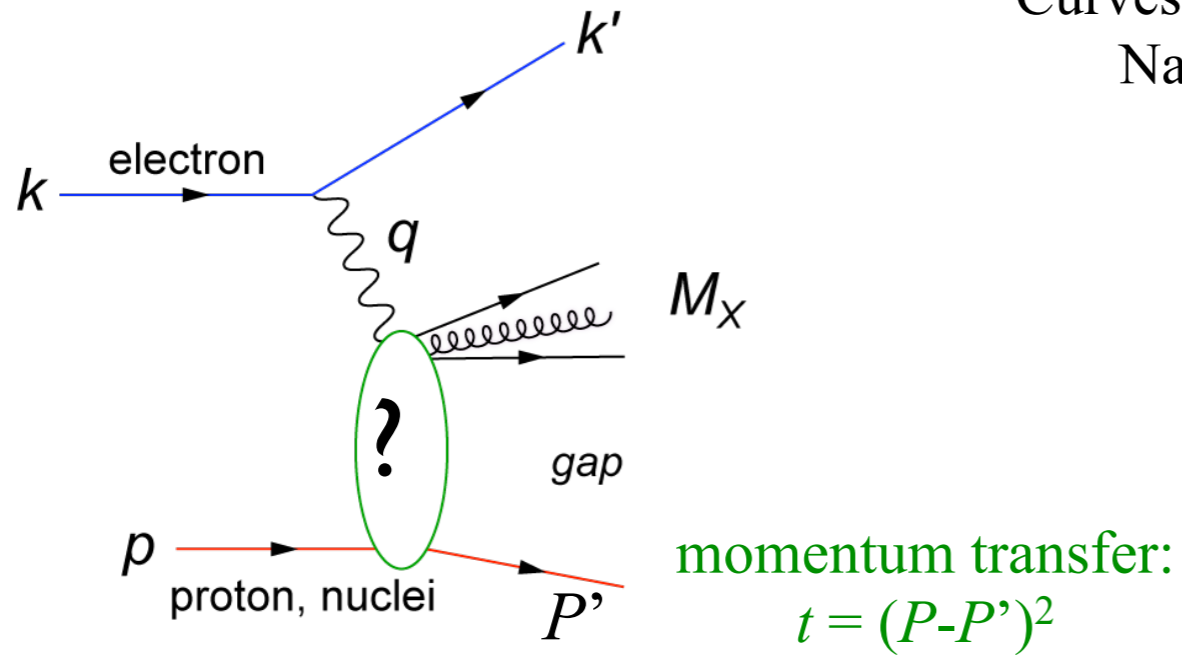
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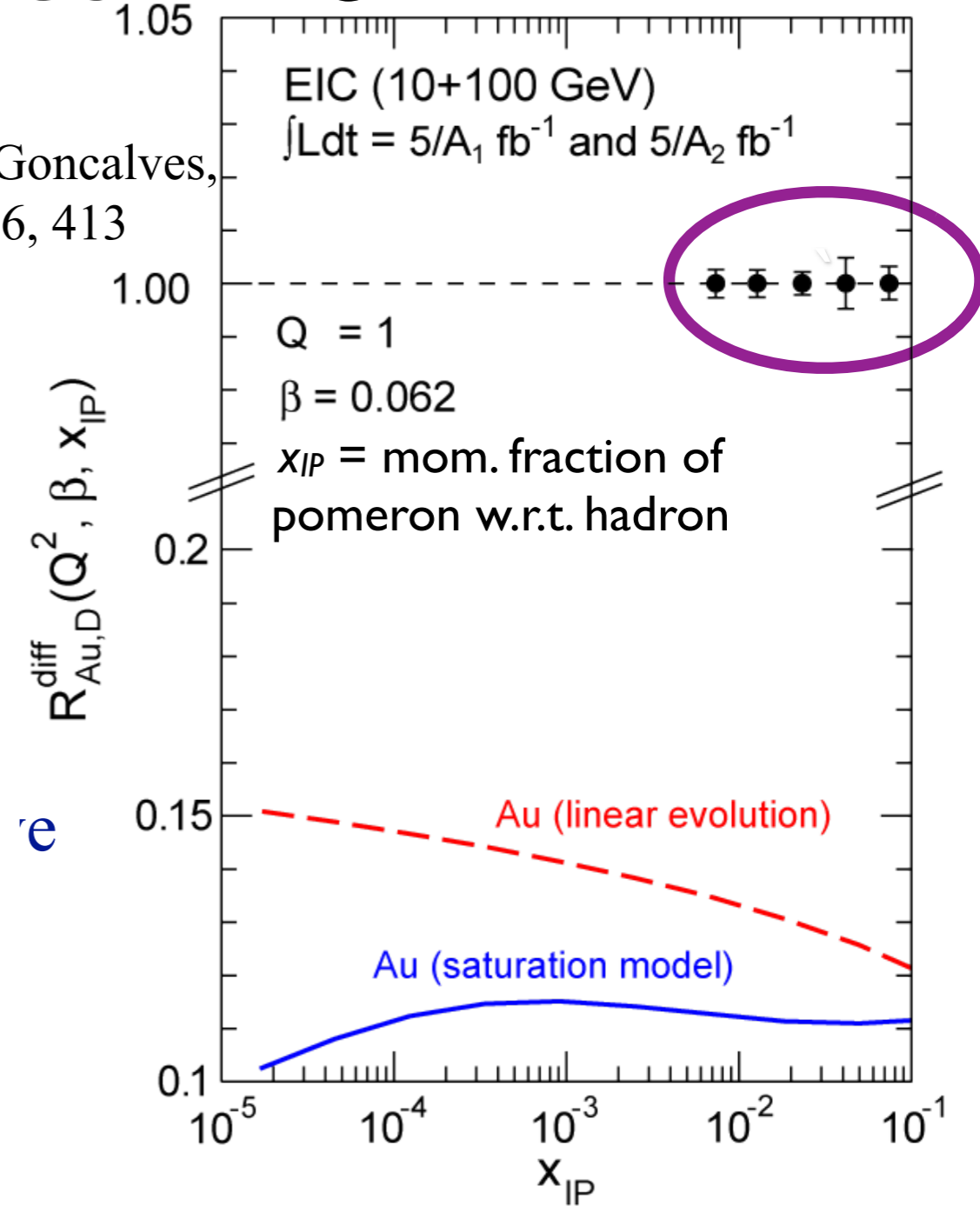
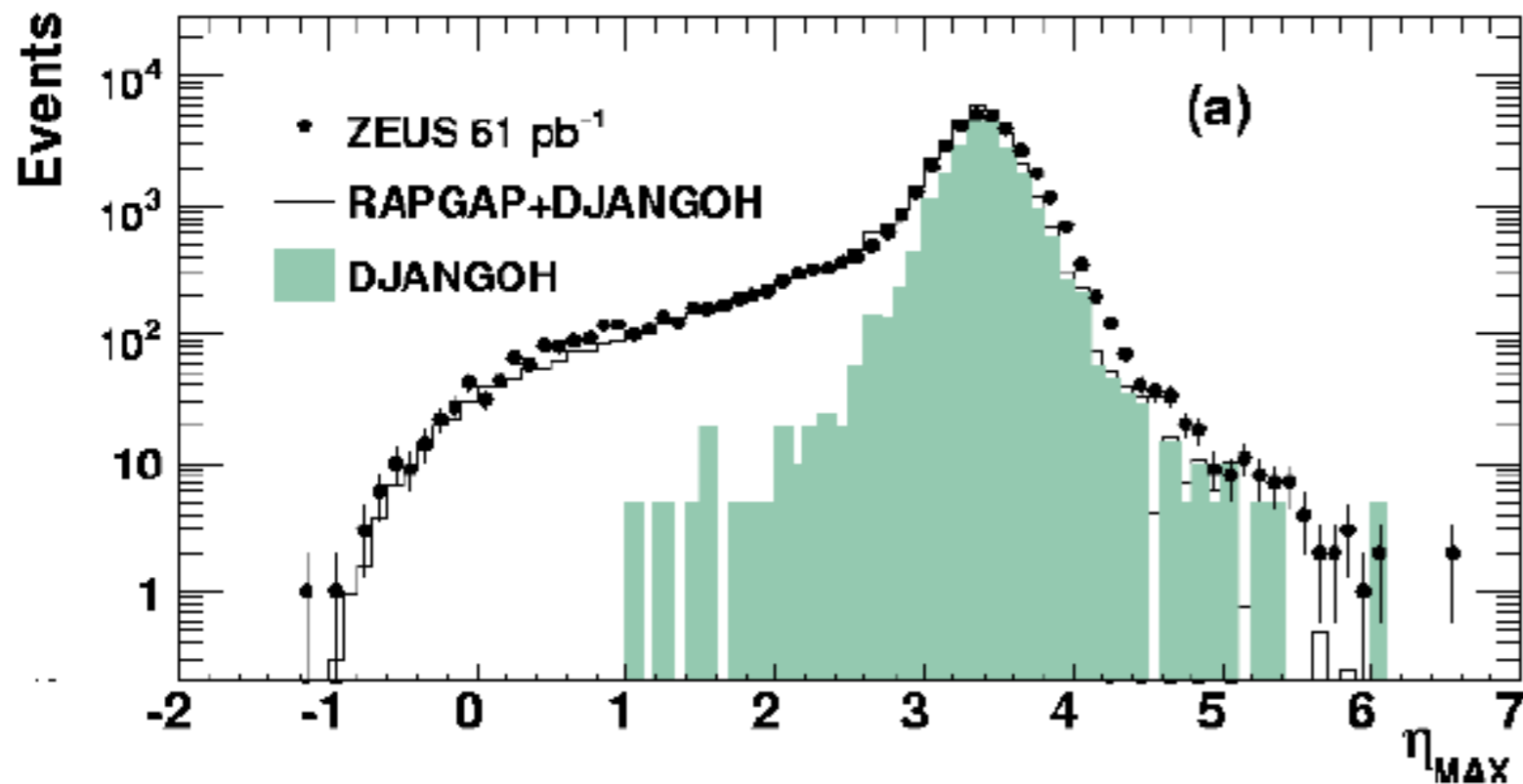
- Distinguish between linear evolution and saturation models

# Diffractive Physics in e+A

## Diffractive event



**ZEUS**



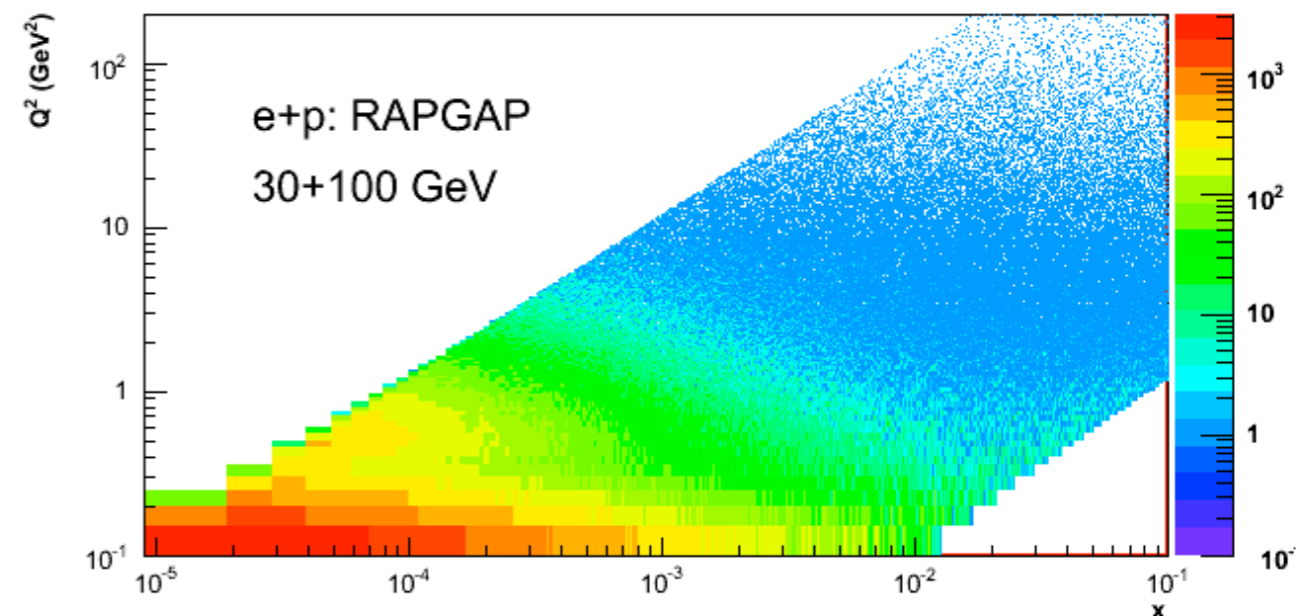
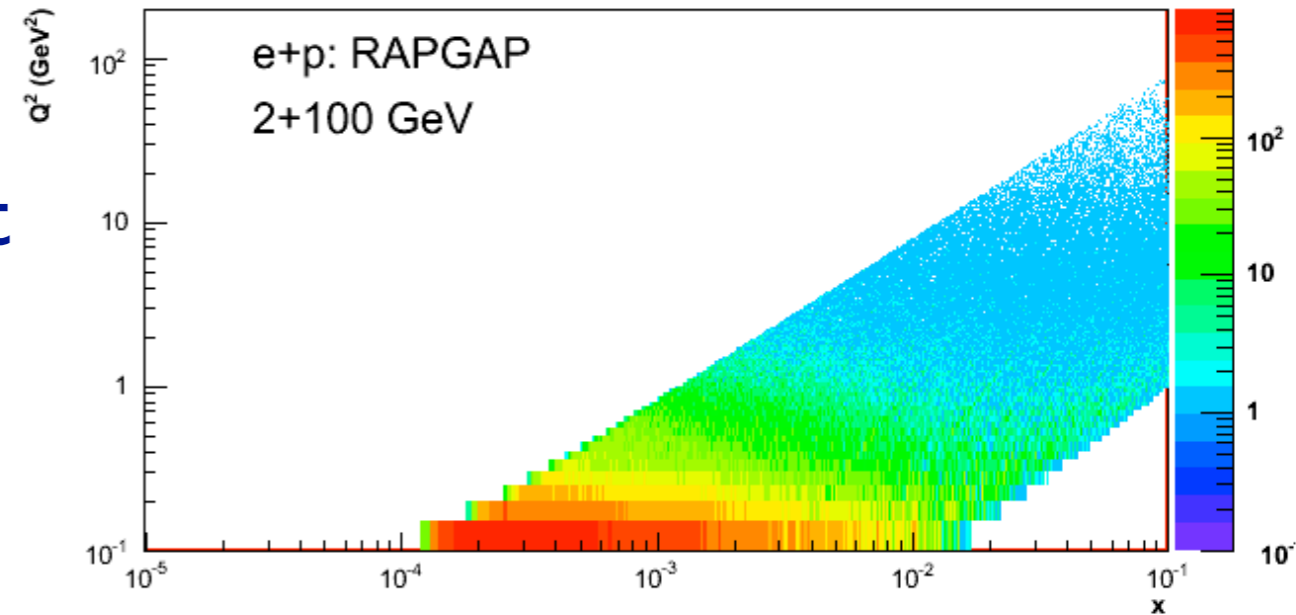
$d/dt \sim [xG(x, Q^2)]^2 !!$

ation models

# Diffraction Physics at an EIC

- Significant coverage in  $x$ - $Q^2$ 
  - ➔ increases by ~ order of magnitude over EIC energies
- Plotted the distribution of the Most Forward Particle in the event for DIS and Diffractive events
  - ➔ significant gap between two classes of events
- Reproduce the “ZEUS” plot?
- Important - plot the efficiency vs purity
  - ➔ Can place a cut in rapidity for ~90% efficiency and ~90% purity !!

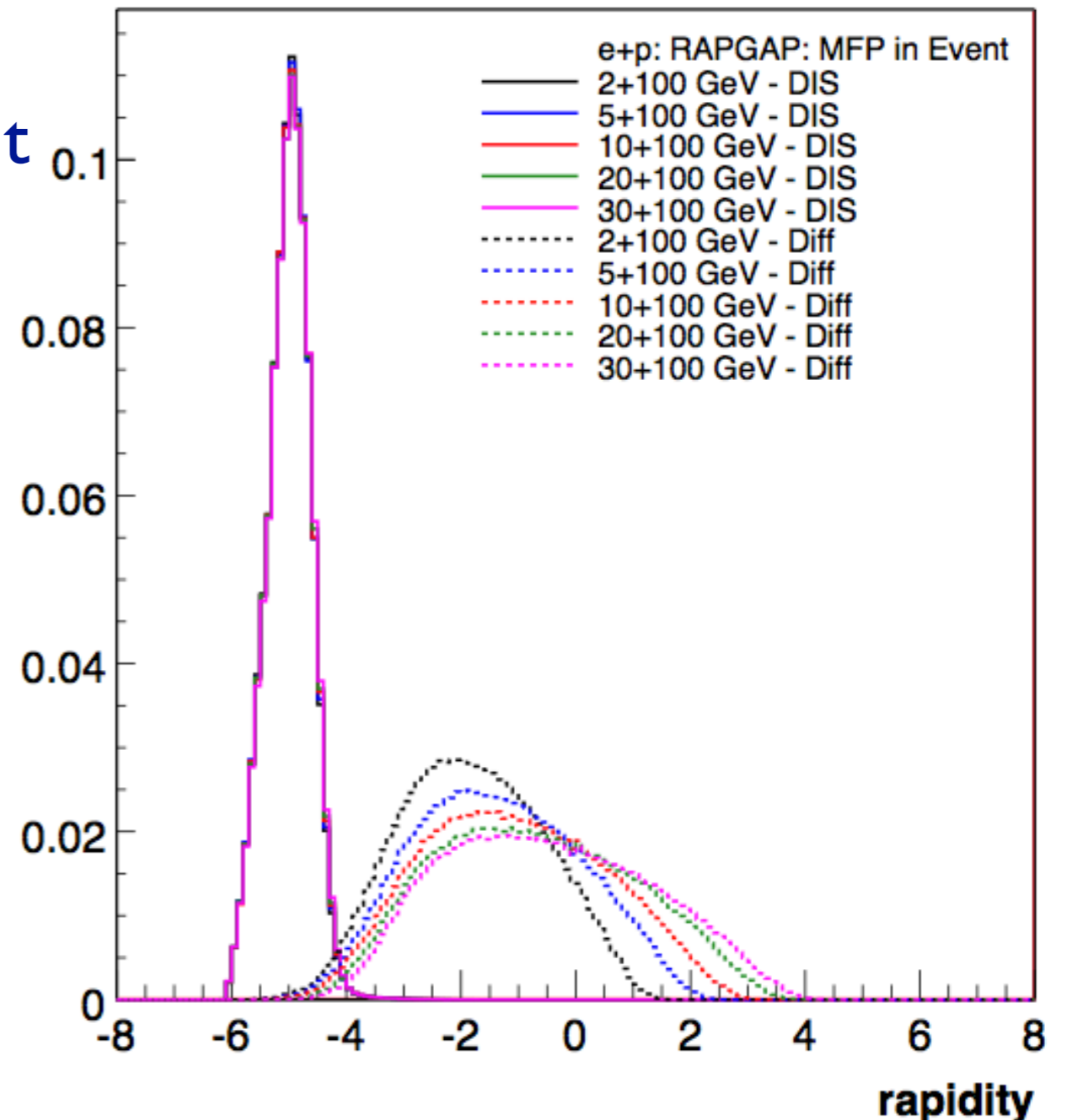
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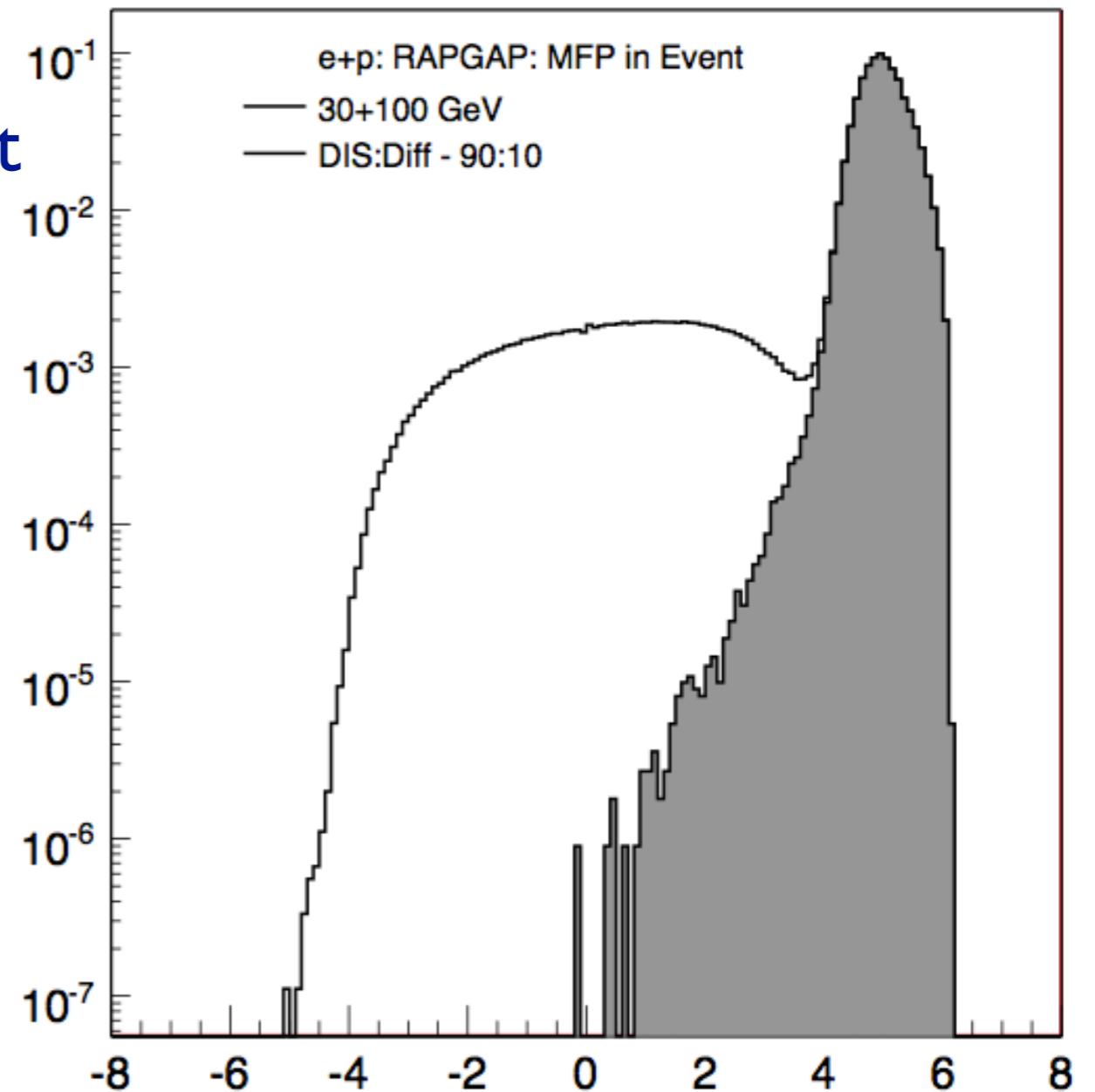




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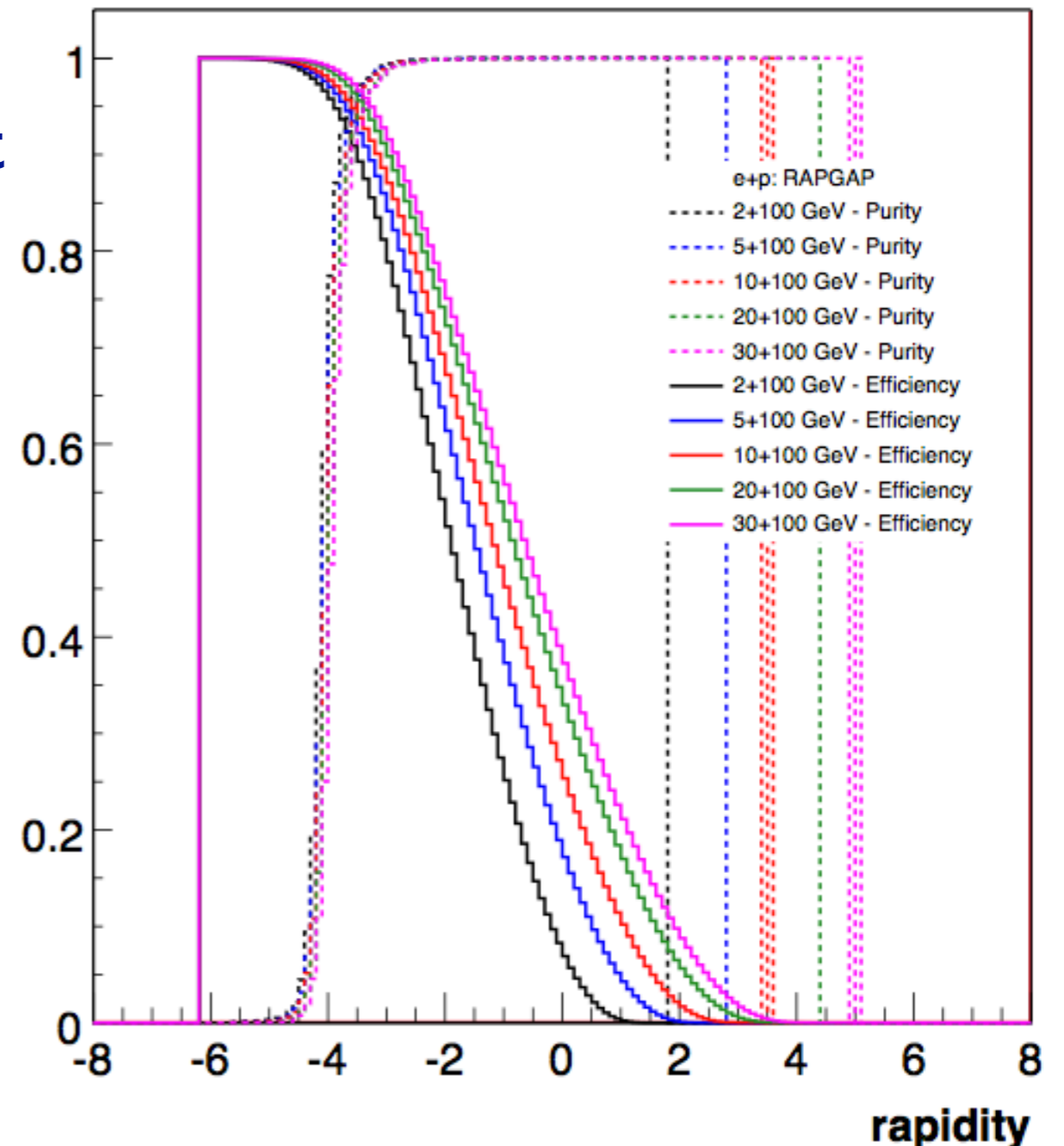
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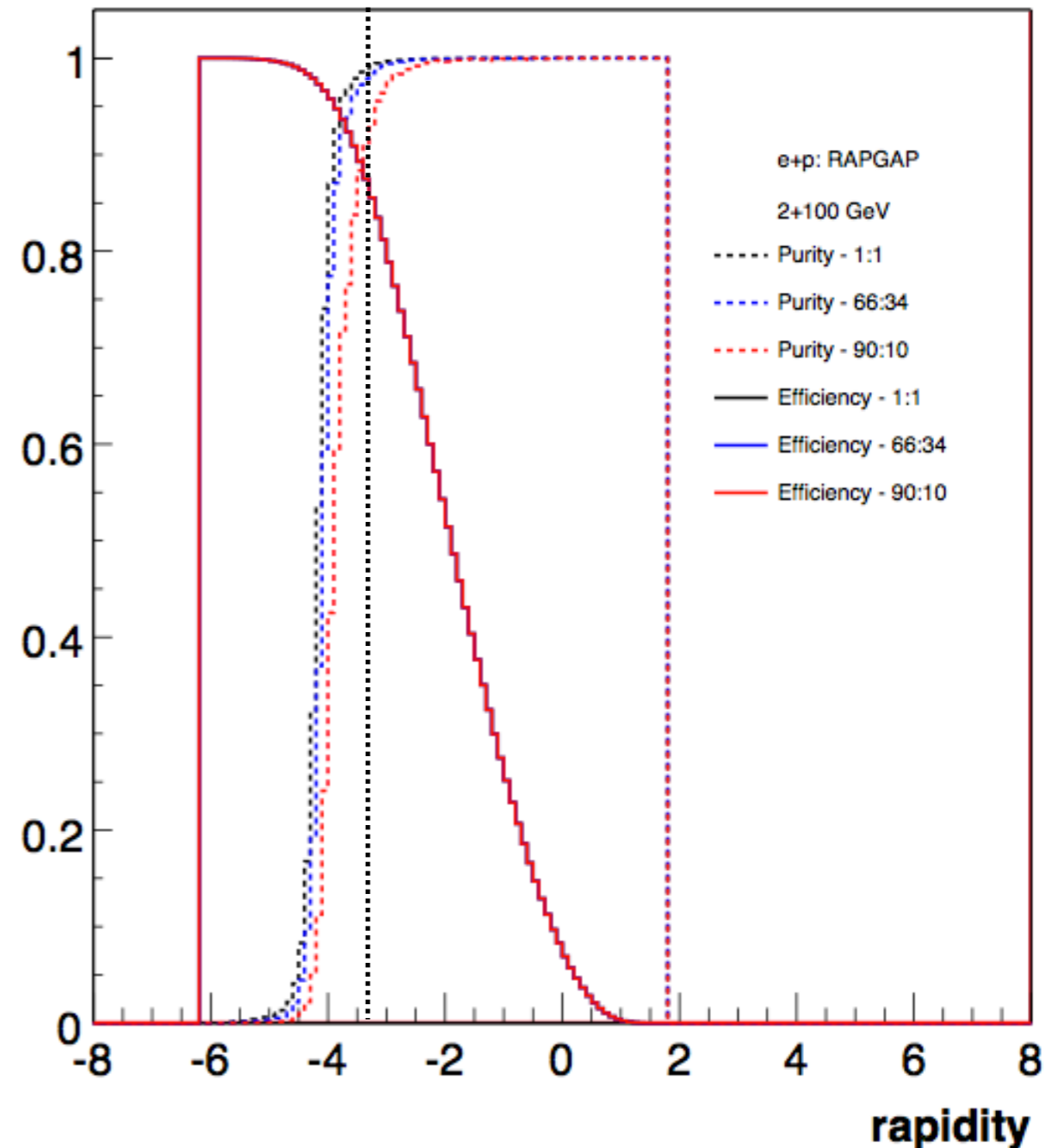
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**Effic:** frac of Diff events out of all Diff events  
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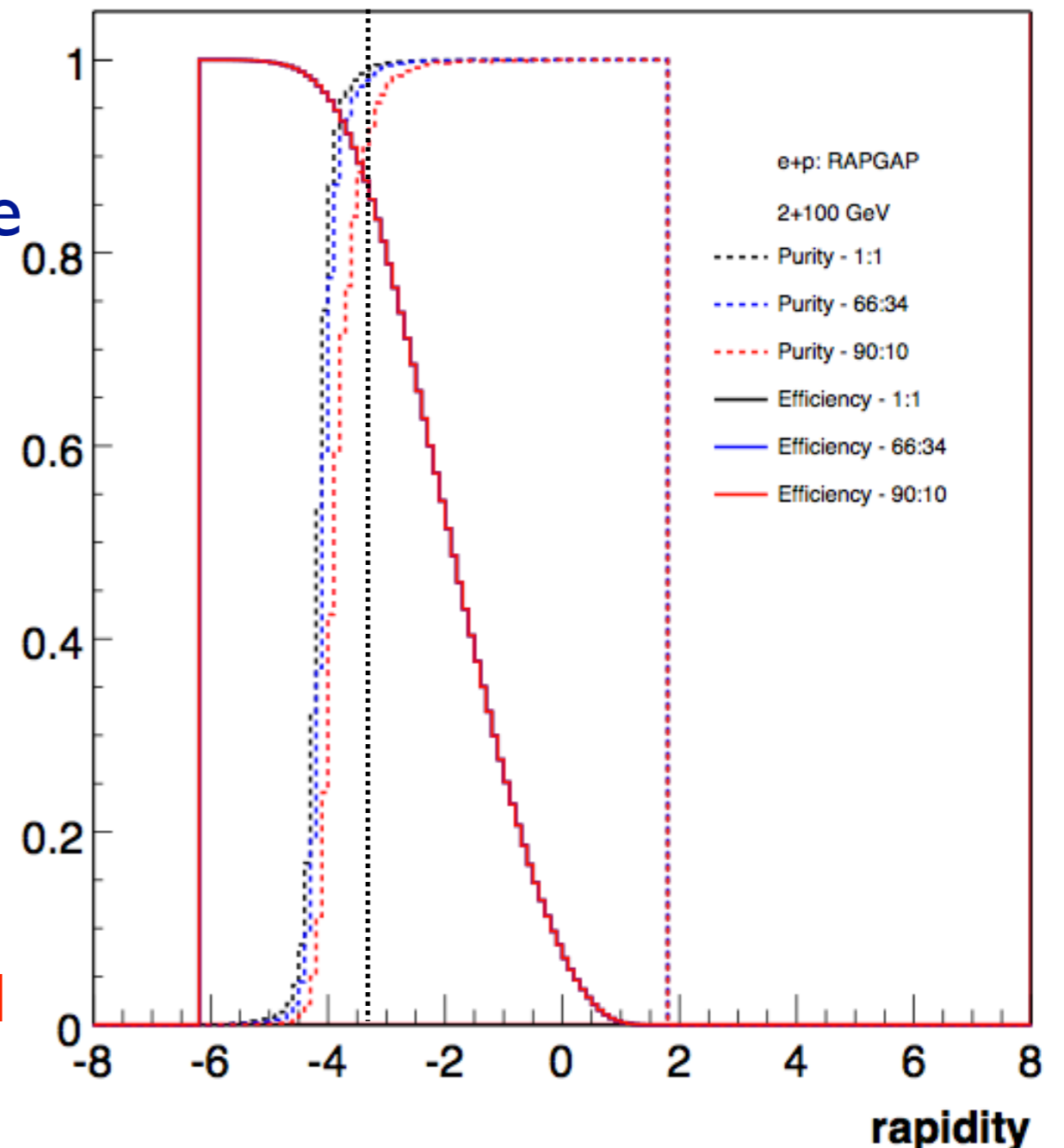
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# Diffraction Physics at an EIC - Acceptance

- ZEUS had a gap in detector coverage (acceptance) of  $\sim 3$  units.
- Studied this effect in the **MFP** distribution for EIC energies:
- Keeping the 90% Purity level has the following effect:
  - **1 unit cut in rapidity**
    - ➔ Efficiency falls by factor of 2, rapidity moves 2 units to right
  - **2 unit cut in rapidity**
    - ➔ Efficiency falls by a factor of 4, rapidity cut moves farther to right !!
- **When designing a detector, it is essential to be as hermetic as possible !!!**

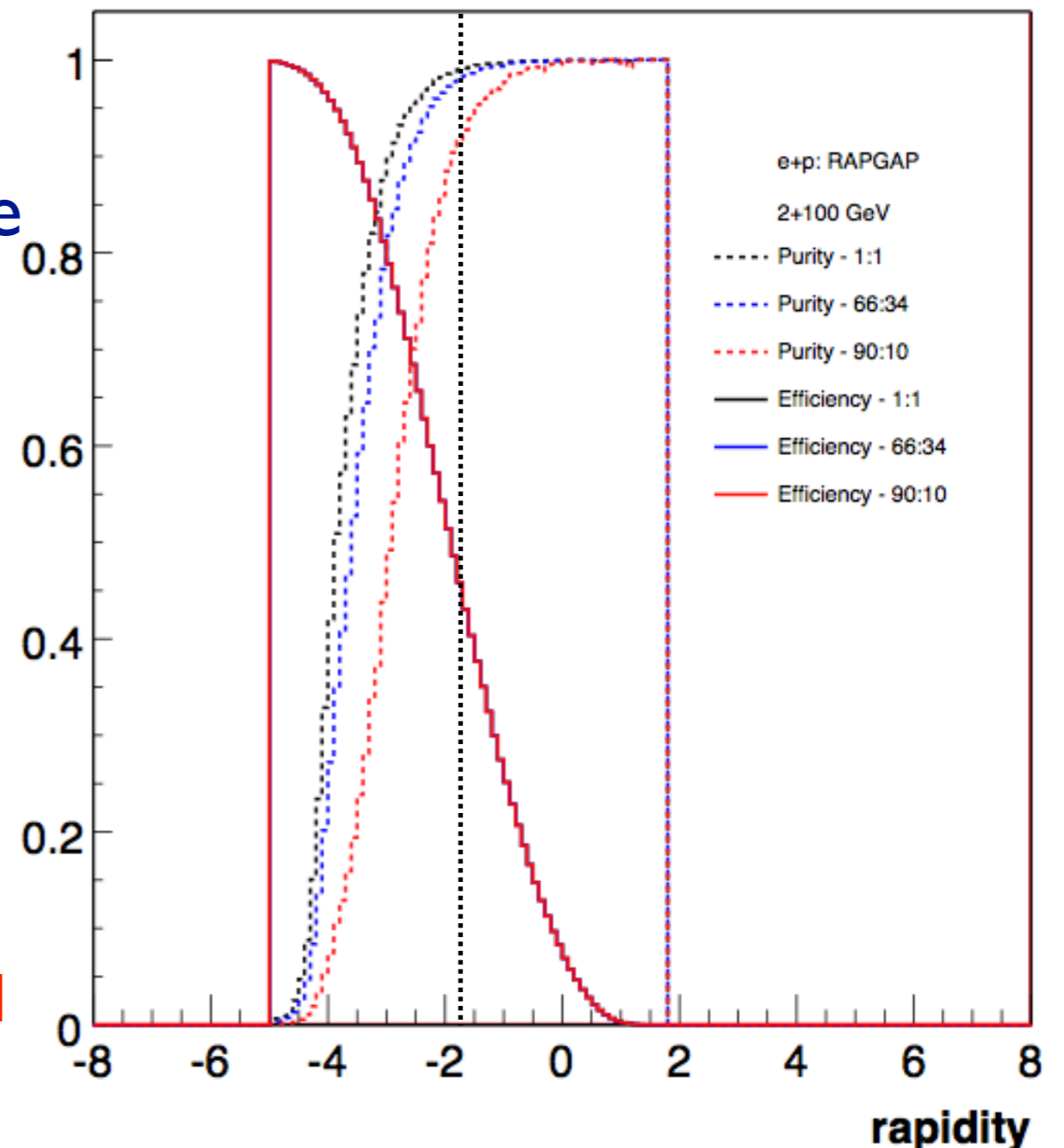
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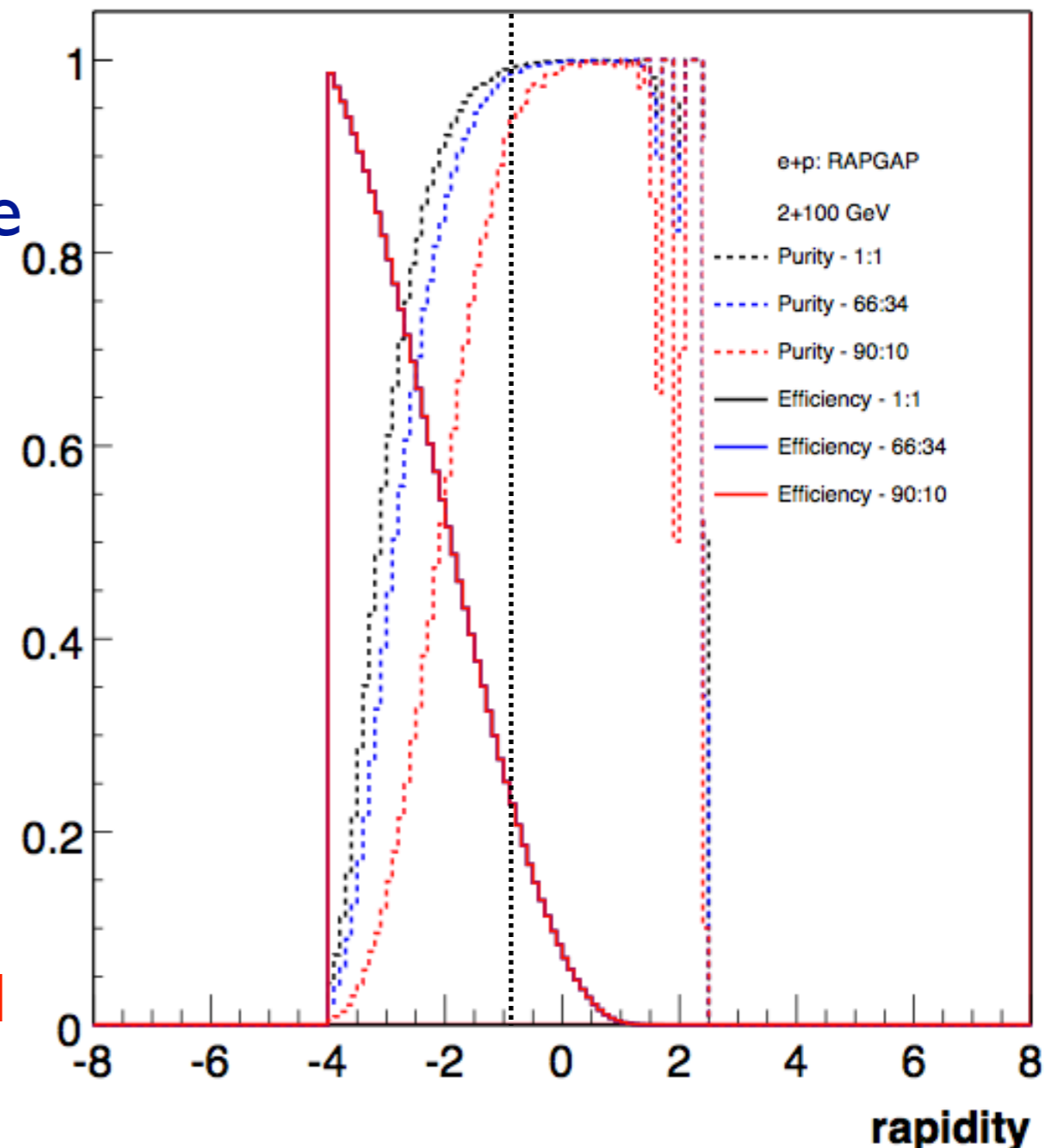
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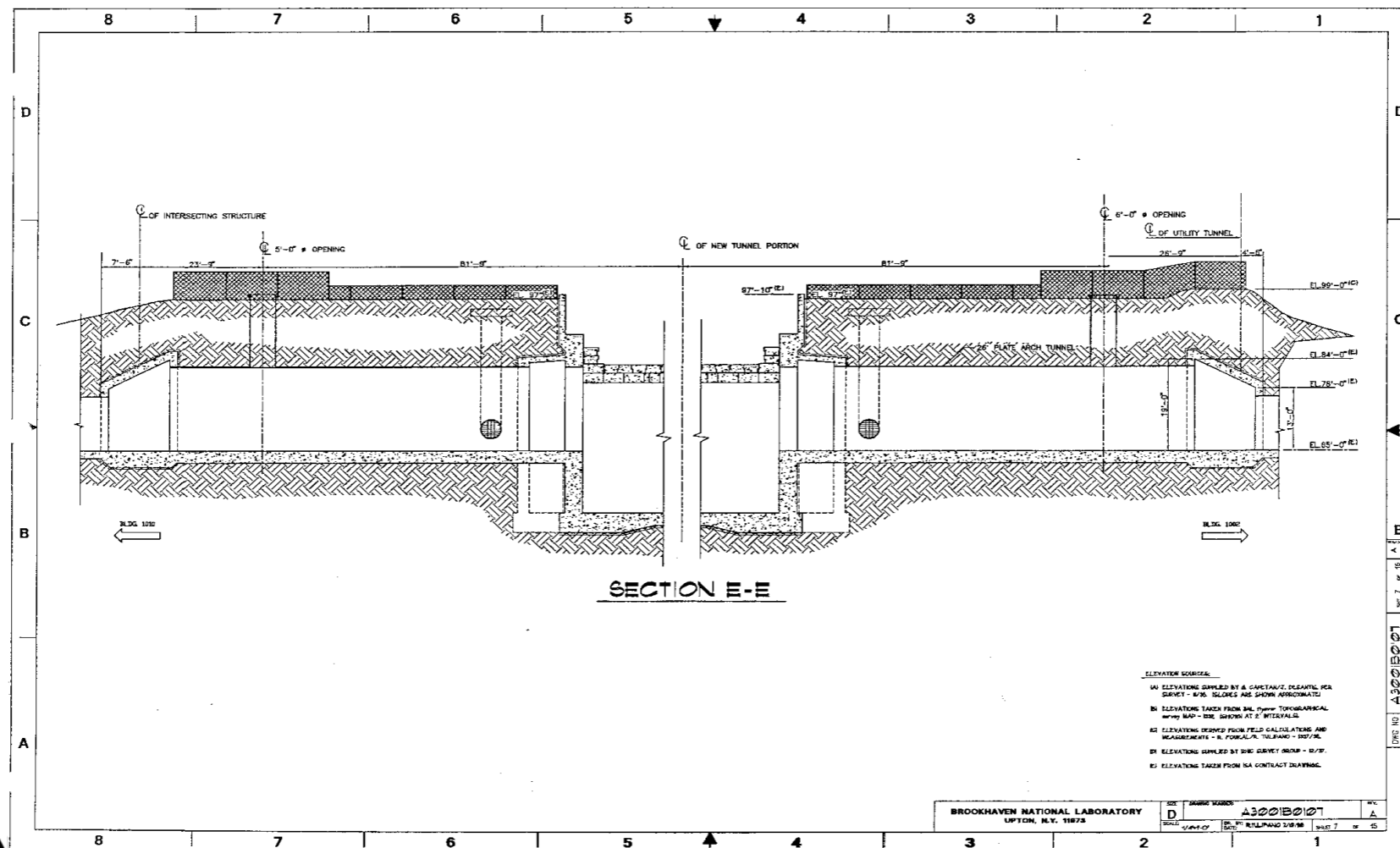
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# Why 2 o'clock and not 12 o'clock?

- Start at 12 o'clock originally:
  - ➔ Detector cost savings
    - ▶ fully staged detector from MeRHIC to eRHIC
      - vertical stage much bigger
      - need to buy magnets only once
      - can stage detector components (i.e. hadronic calorimeter)
      - no moving of detector



# Summary and Outlook

- First steps made on detector design
- Optimisations needed
  - ➔ Do we need 4 T for solenoid and 3 Tm for dipole?
  - ➔ What radiation length can be tolerated for low energy electron?
  - ➔ Optimise the distance from solenoid to dipole
  - ➔ What is the impact of the beam lines through the detector on the physics?
  - ➔ Need to optimise acceptance at low scattering angle
    - ▶ Need acceptance down to 1 degree
- Need to add Roman Pots into detector configuration
- Need to include luminosity monitor and lepton polarimeter in IR design



# Photon Flux

---

Dipole models provide  $\sigma_{L,T} (\gamma^* p \rightarrow p' V)$

For generator we need to consider  $\sigma (e p \rightarrow \varepsilon' p' V)$

Need Photon Flux  $\Gamma_T, \Gamma_L$

$$\sigma^{e p \rightarrow \varepsilon' p' V} = \Gamma_L \sigma_L^{\gamma^* p \rightarrow p' V} + \Gamma_T \sigma_T^{\gamma^* p \rightarrow p' V}$$

The full formula is rather complex

What is used is a simplification (not always justified):

For  $Q^2/(4E^2) = 0$  and  $Q^2/v^2 = 0$ ,  $m_e = 0$

Pick 2 independent variables best for MC:  $x, Q^2$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{\alpha}{2\pi} \frac{1}{xQ^2} \left( \left[ 1 + (1-y)^2 - 2(1-y) \frac{Q_{min}^2}{Q^2} \right] \sigma_T + 2(1-y)\sigma_L \right)$$

where  $Q_{min}^2 = \frac{m_e^2 y^2}{1-y}$

Jacobian!

# Full Shebang ...

---

Dipole model calculations + flux give:

$$\frac{d^6 \sigma}{dx dQ^2 dt db dz dr}$$

- ▶ 6-dim Probability Distribution Function (PDF)
- ▶ all variables independent
- ▶ Given (input): beam energies  $\mathbf{p}_e, \mathbf{p}_p$

# Final State Particles

---

Given:  $\mathbf{p}_e, \mathbf{p}_p, s, t, x, Q^2, y$

Need:  $\mathbf{p}_{e'}, \mathbf{p}_{p'}, \mathbf{p}_{\gamma^*}, \mathbf{p}_{VM}$

Hannes Jung (DESY) gave me analytic solutions for all. After many checks:  $\mathbf{p}_{e'}, \mathbf{p}_{\gamma^*}$  formulas are correct!

$\mathbf{p}_{p'}$  is not correct (possible source of problems in RAPGAP?)

## New Ansatz:

- $t = (\mathbf{p} - \mathbf{p}')^2, m_{VM}^2 = (\mathbf{p}_{\gamma^*} + \mathbf{p}_p - \mathbf{p}_{p'})^2, |\mathbf{p}_{p'}| = m_p$
- allows to derive  $\mathbf{p}_p$  numerically (root finder)
- use Hanne's analytic formula as first guess
  - ▶ fails at times since first guess is off by several GeV
- $\mathbf{p}_{VM}$  through  $\mathbf{p}_e + \mathbf{p}_p = \mathbf{p}_{e'} + \mathbf{p}_{p'} + \mathbf{p}_{VM}$
- solution obtained this way is fully consistent
  - ▶  $\mathbf{p}_{e'}, \mathbf{p}_{p'}, \mathbf{p}_{\gamma^*}, \mathbf{p}_{VM} \Rightarrow s, t, x, Q^2, y$

# Kinematic Boundaries

---

Tricky since some formulas neglect masses others not  
(something to still work on)

$$s = \frac{Q^2}{xy} + m_p^2 + m_e^2 \quad \text{not just } Q^2 = sxy$$

Currently implemented (but not sufficient):

$$0 < x < 1$$

$$0 < y < 1$$

$$\frac{m_e^2 y^2}{1-y} < Q^2 < s - m_e^2 - m_p^2$$

$$x_{IP} = \frac{m_V^2 + Q^2}{ys}$$

$$t < -\frac{x_{IP}^2 m_p^2}{1-x_{IP}}$$