

Shell model treatment of neutron-rich nuclei near ^{78}Ni

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- Recent experimental progress and forthcoming experiments:
new regions of neutron rich nuclei
- New magic numbers at extreme N/Z ratio
- astrophysical processes
- isomerism in nuclei around ^{78}Ni



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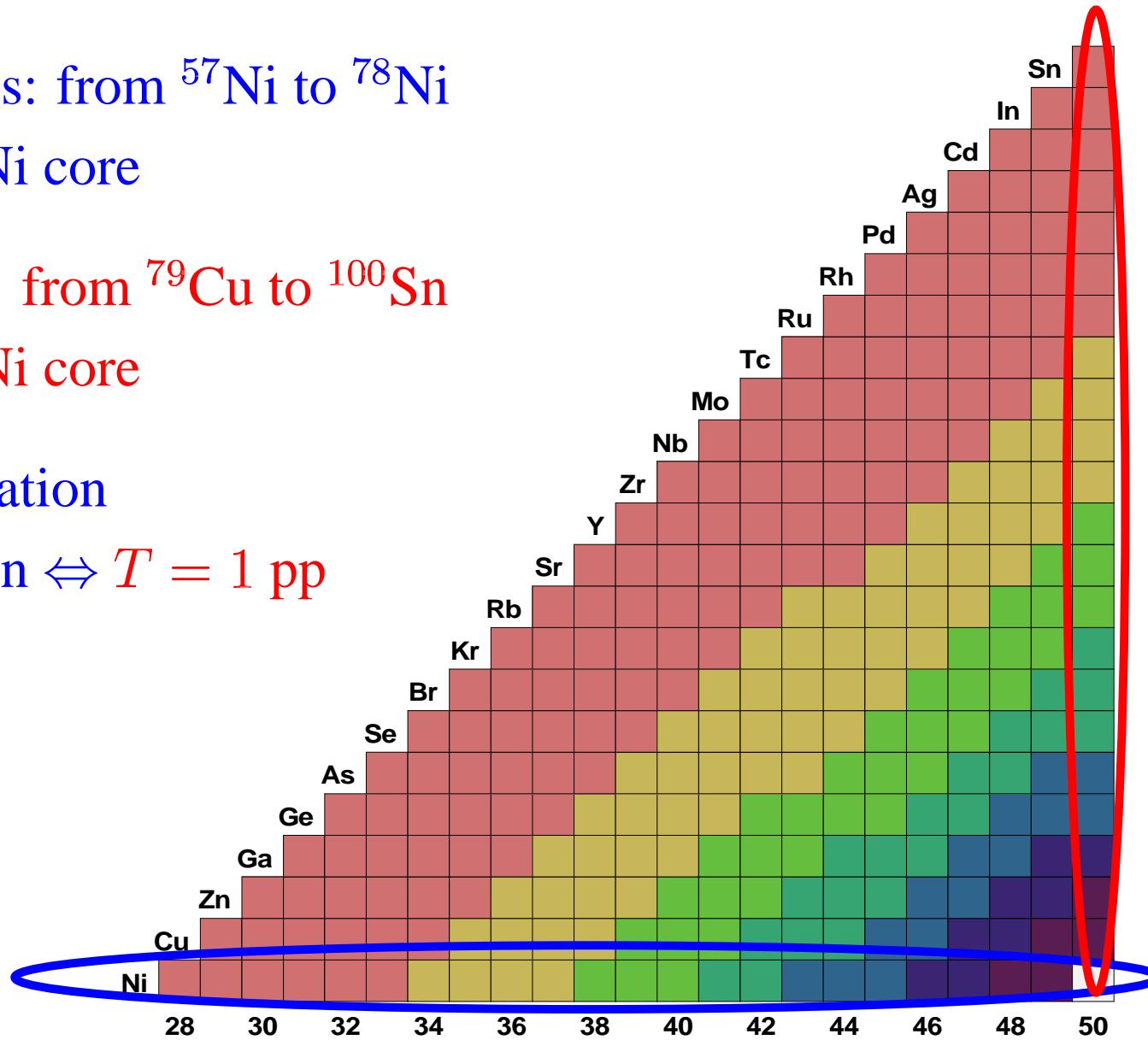
Unique $T = 1$ interaction ?

Neutrons: from ^{57}Ni to ^{78}Ni
with ^{56}Ni core

Protons: from ^{79}Cu to ^{100}Sn
with ^{78}Ni core

Interpolation

$T = 1 \text{ nn} \Leftrightarrow T = 1 \text{ pp}$



Determination of the effective SM interaction

$$E_{\alpha}^{\text{th}} = \sum_i \epsilon_i \cdot n_i + \sum_{ij,km} \langle ij|V|km \rangle_J \cdot D_{ij,km}^J$$

$$\chi^2\text{-minimization} \quad \chi^2 = \frac{1}{N} \sum_{\alpha,k} [E_{\alpha}^{\text{th}}(k) - E_{\alpha}^{\text{exp}}(k)]^2$$

Parameters:

4 s.p.e. ϵ_i : $p_{3/2}$, $p_{1/2}$, $f_{5/2}$ and $g_{9/2}$

65 T.B.M.E. : $\langle ij|V|km \rangle_J$

Initial interaction: G-matrix

Linear Combination Method: 20 most important linear combinations
of interaction parameters;

Convergence of energies after 6 iterations

Results

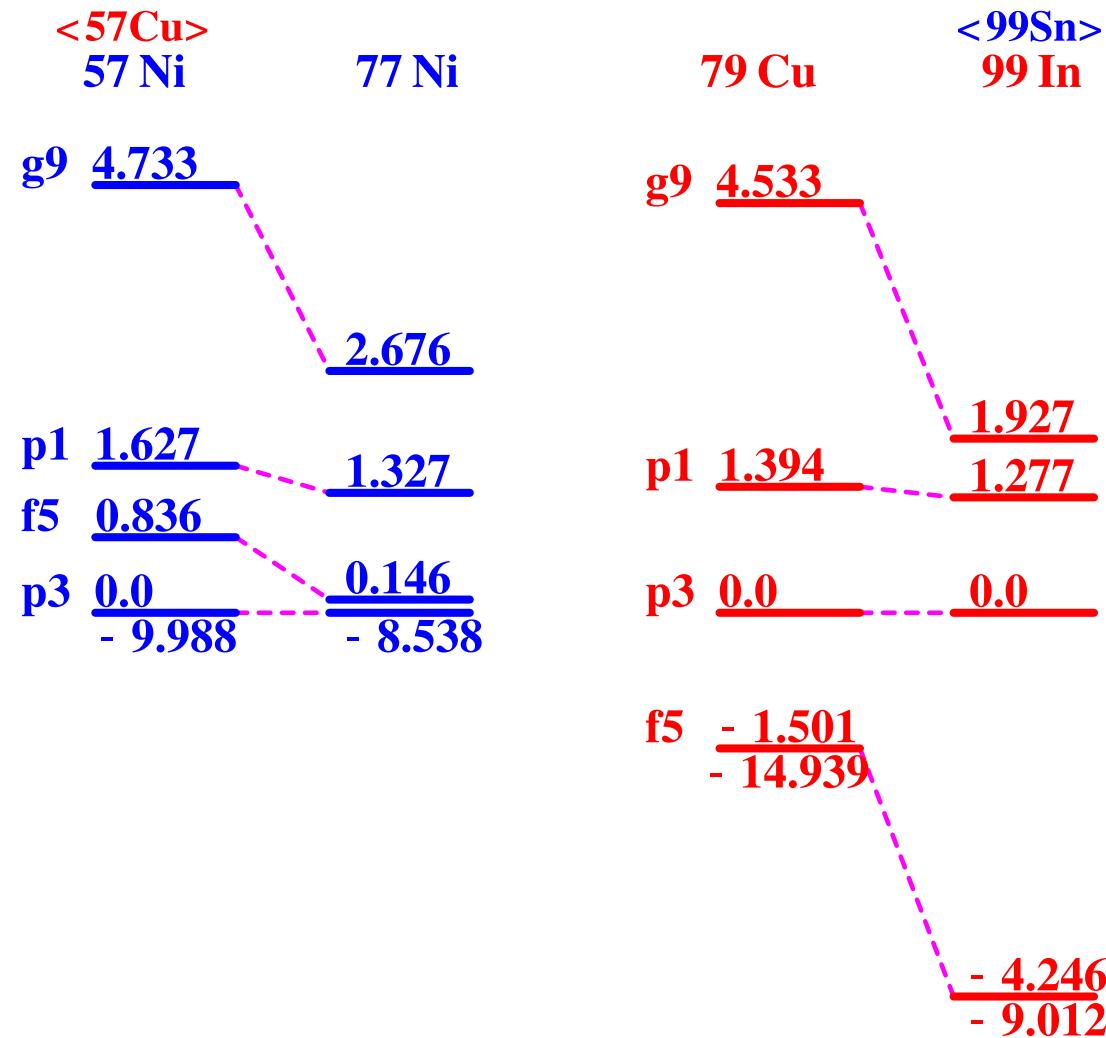
Neutrons: Z=28; ^{61}Ni – ^{78}Ni ; 106 states ; $\chi^2=0.241 \text{ MeV}$

$p_{3/2} = -9.988 \text{ MeV}$	$\langle g_{9/2}^2, J = 0 \rangle = -1.372 \text{ MeV}$
$p_{1/2} = -8.361 \text{ MeV}$	$\langle g_{9/2}^2, J = 2 \rangle = -0.999 \text{ MeV}$
$f_{5/2} = -9.153 \text{ MeV}$	$\langle g_{9/2}^2, J = 4 \rangle = -0.329 \text{ MeV}$
$g_{9/2} = -5.255 \text{ MeV}$	$\langle g_{9/2}^2, J = 6 \rangle = 0.189 \text{ MeV}$
	$\langle g_{9/2}^2, J = 8 \rangle = 0.325 \text{ MeV}$

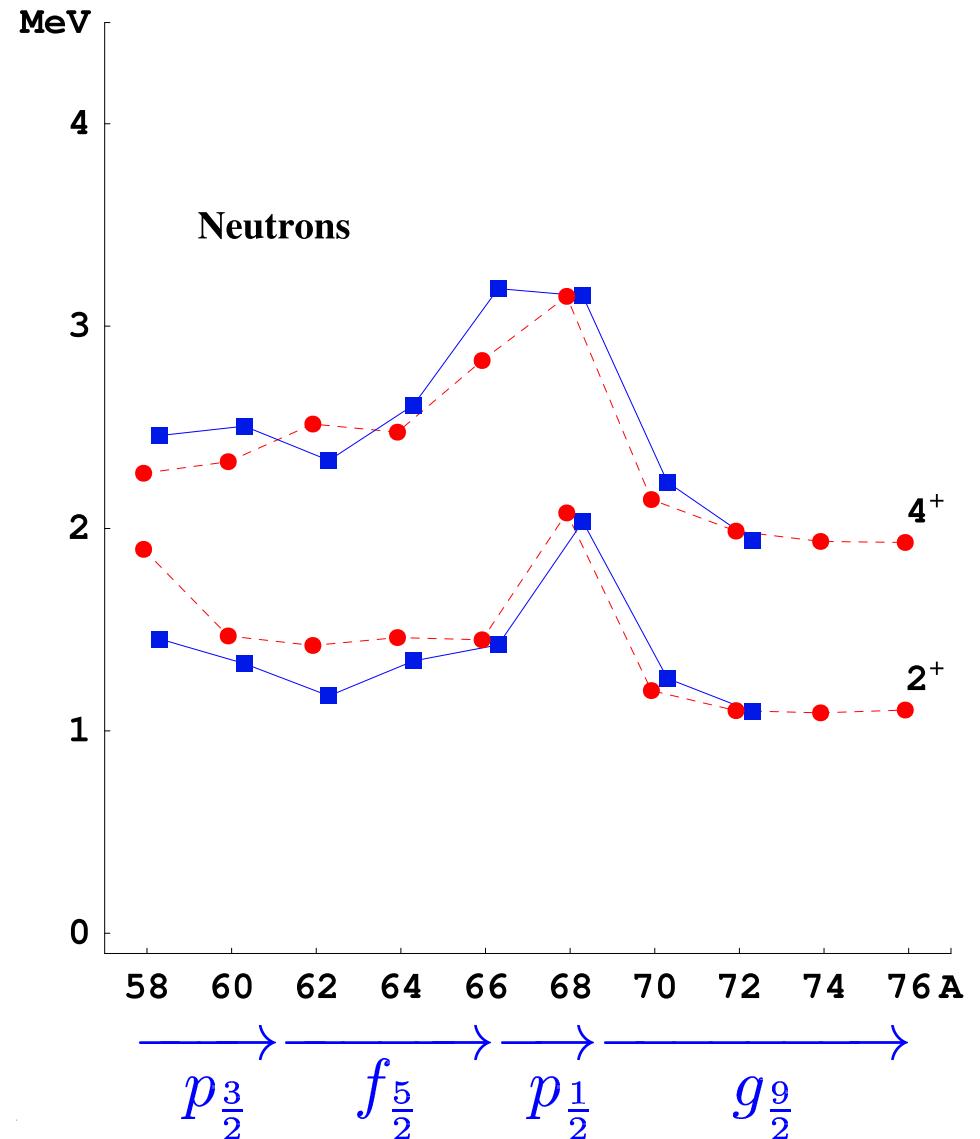
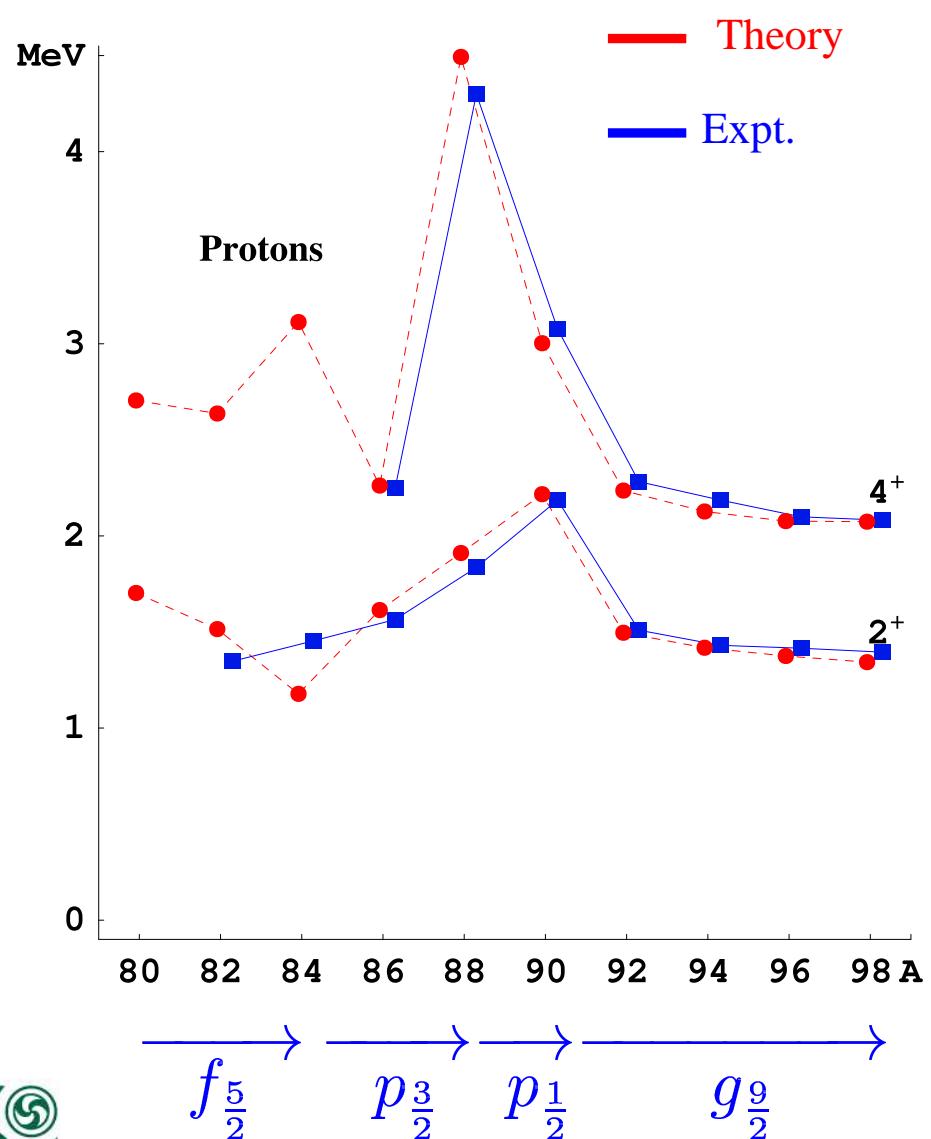
Protons: N=50; ^{79}Cu – ^{100}Sn ; 132 states; $\chi^2=0.124 \text{ MeV}$

$p_{3/2} = -13.437 \text{ MeV}$	$\langle g_{9/2}^2, J = 0 \rangle = -1.146 \text{ MeV}$
$p_{1/2} = -12.044 \text{ MeV}$	$\langle g_{9/2}^2, J = 2 \rangle = -0.419 \text{ MeV}$
$f_{5/2} = -14.938 \text{ MeV}$	$\langle g_{9/2}^2, J = 4 \rangle = 0.219 \text{ MeV}$
$g_{9/2} = -8.905 \text{ MeV}$	$\langle g_{9/2}^2, J = 6 \rangle = 0.442 \text{ MeV}$
	$\langle g_{9/2}^2, J = 8 \rangle = 0.629 \text{ MeV}$

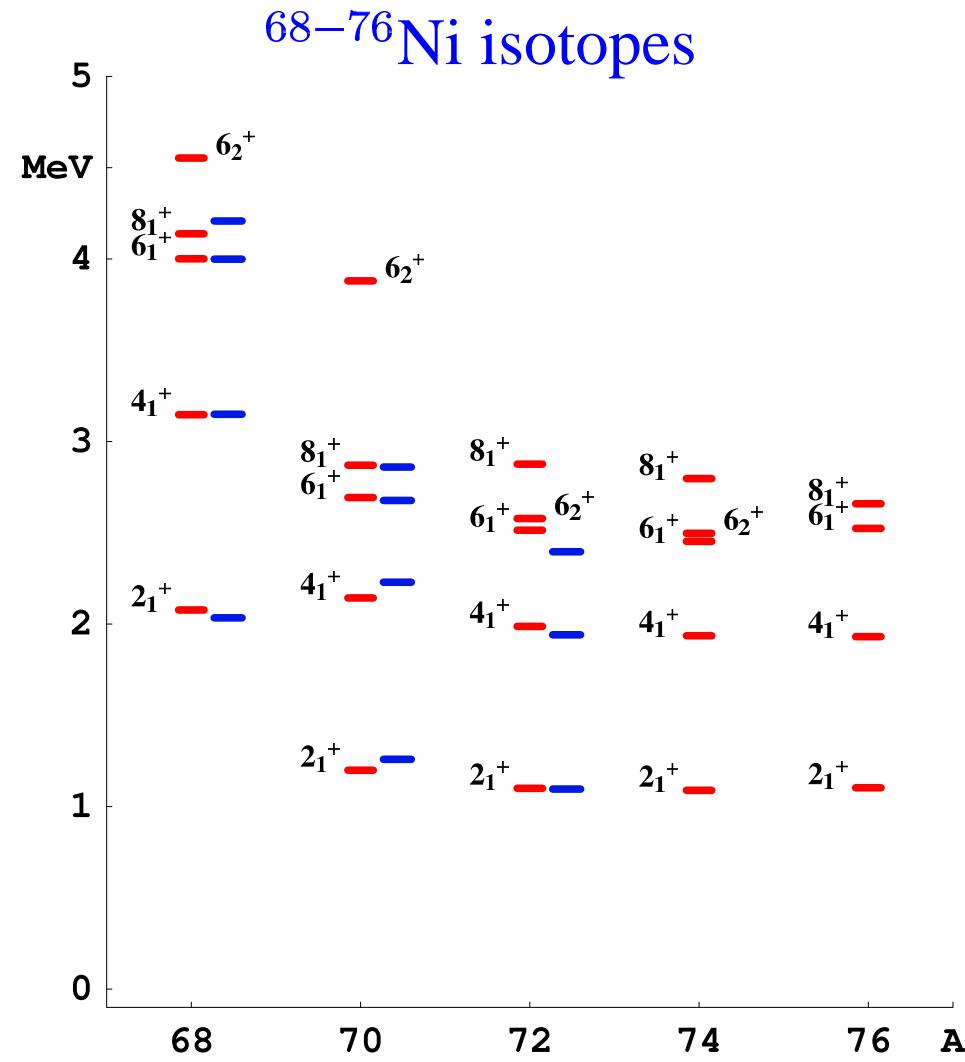
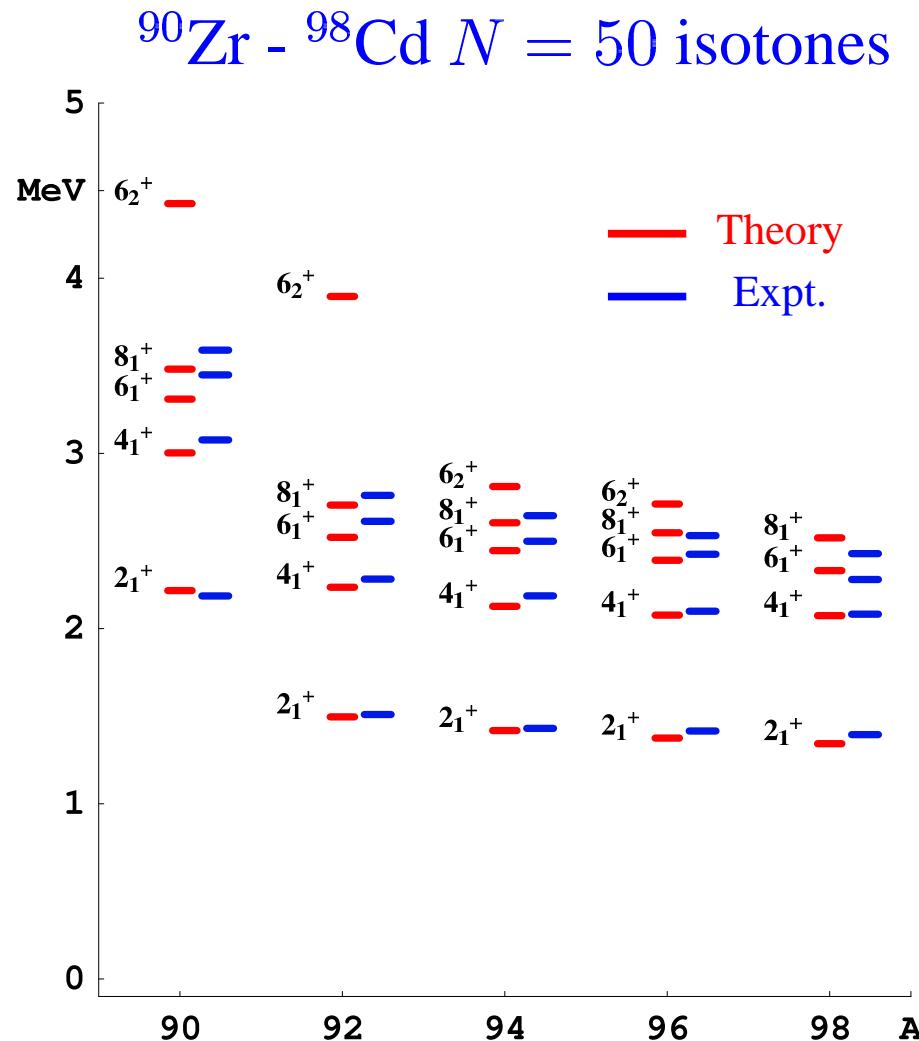
SPE's



2^+ and 4^+ states



Spectra of Valence Mirror Symmetry partners



Ni-isotopes: B(E2) values and lifetimes of 8^+ states

$B(E2; J_i^\pi \rightarrow J_f^\pi)$, [$e^2 \text{fm}^4$], $e_n=1.0$

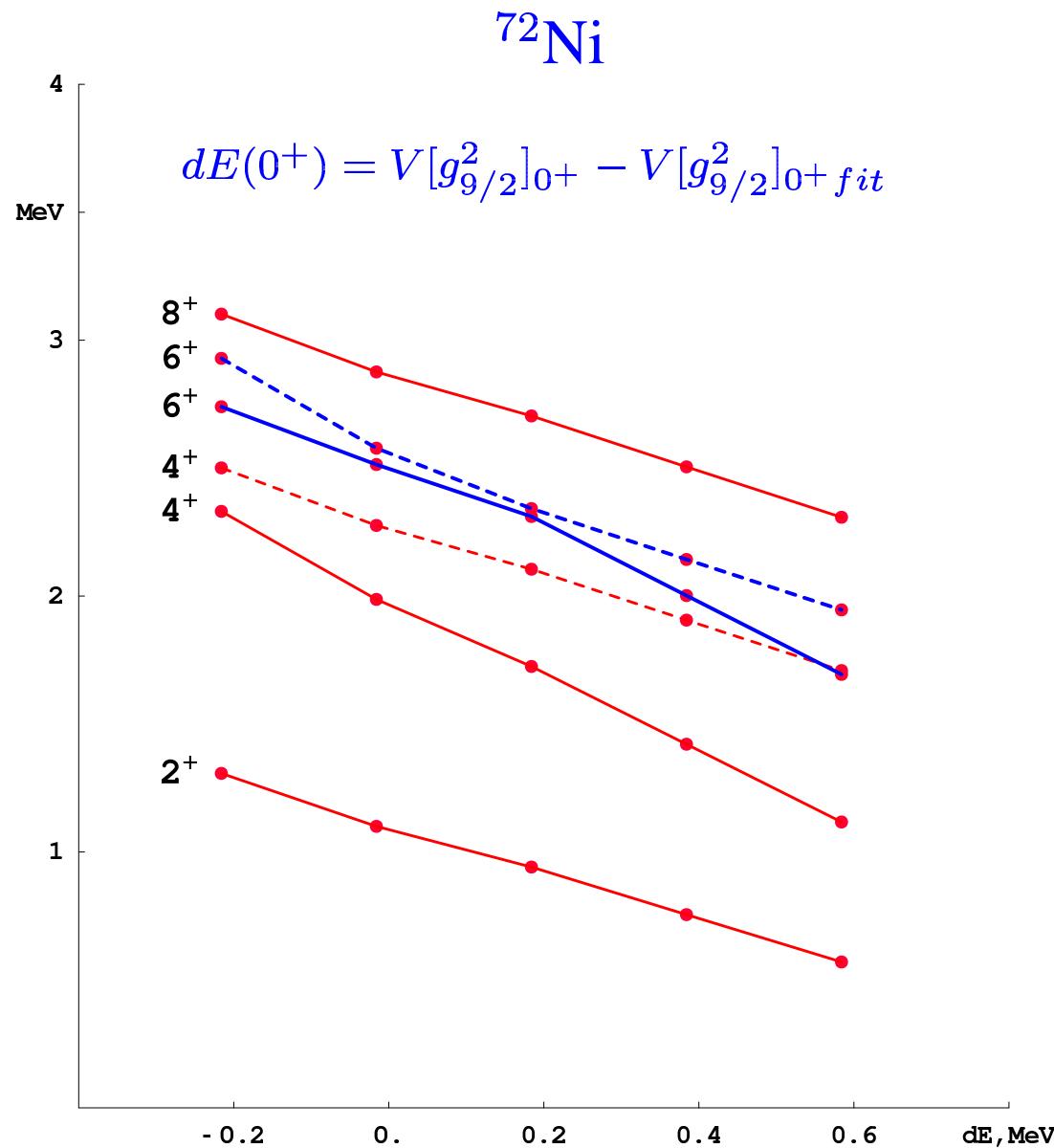
J_i^π	J_f^π	^{70}Ni	^{72}Ni	^{74}Ni	^{76}Ni
2_1^+	0_1^+	64	84	76	46
4_1^+	2_1^+	51	94	85	54
6_1^+	4_1^+	31	29	34	37
8_1^+	6_1^+	12	1.9	9.2	15
	6_2^+	3.3	52	47	-
$\tau(8_1^+)$	Th.	326.0 ns	6.1 ns	5.1 ns	$1.2 \mu\text{s}$
	Expt.	335(4) ns	<26 ns	<87 ns	

Lifetimes of 8^+ isomers in $N = 50$ isotones

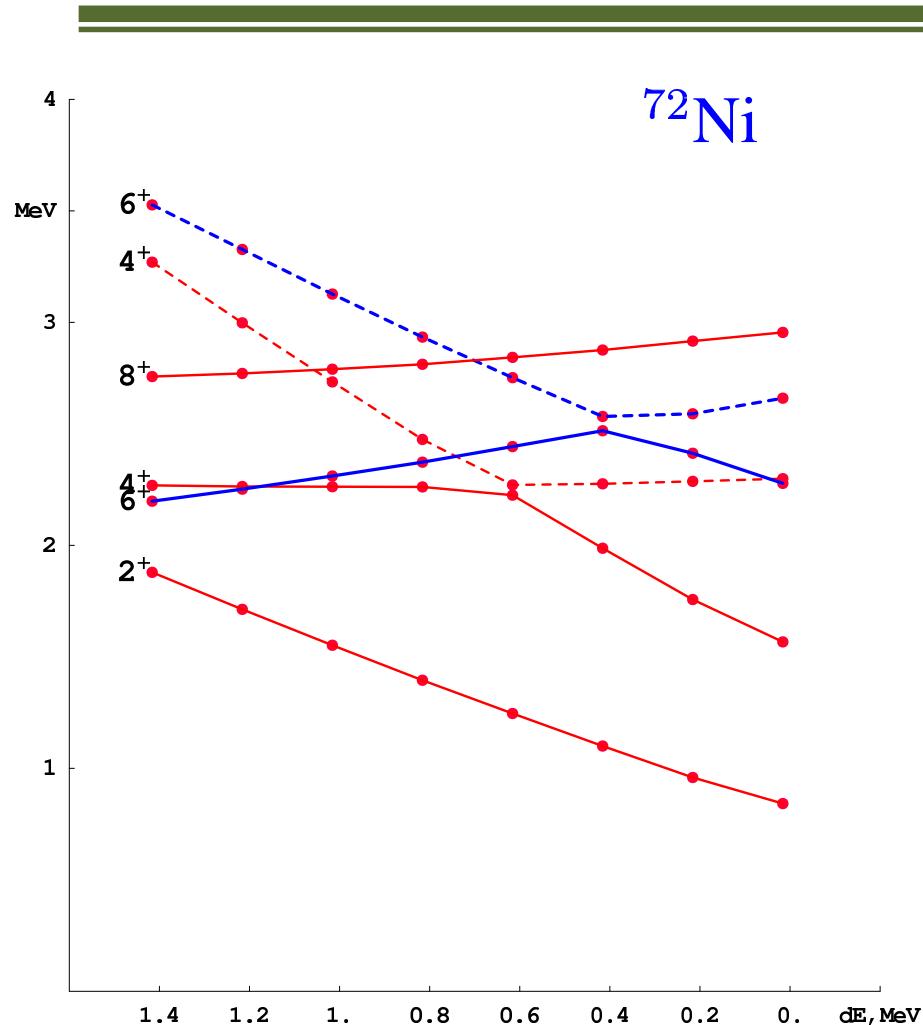
$$B(E2; J_i^\pi \rightarrow J_f^\pi), [e^2 \text{fm}^4], e_p=2.0$$

J_i^π	^{92}Mo		^{94}Ru		^{96}Pd		^{98}Cd	
	Th.	Expt.	Th.	Expt. ^a	Th.	Expt. ^a	Th.	Expt. ^b
2_1^+	235	207(12)	304	-	283	-	181	-
4_1^+	164	<605	9.2	-	40	-	214	-
6_1^+	110	81(2)	8.2	2.9(1)	20	20(3)	149	-
8_1^+	42	32.4(5)	2.7	0.09(1)	7.1	8.9(12)	60	35(11)
$\tau(8_1^+), [\mu\text{s}]$	0.213	0.274(4)	4.4	102(6)	4.0	3.2(4)	0.19	0.69(23)

Effect of $0^+ g_{9/2}^2$ tbme on excitation energies



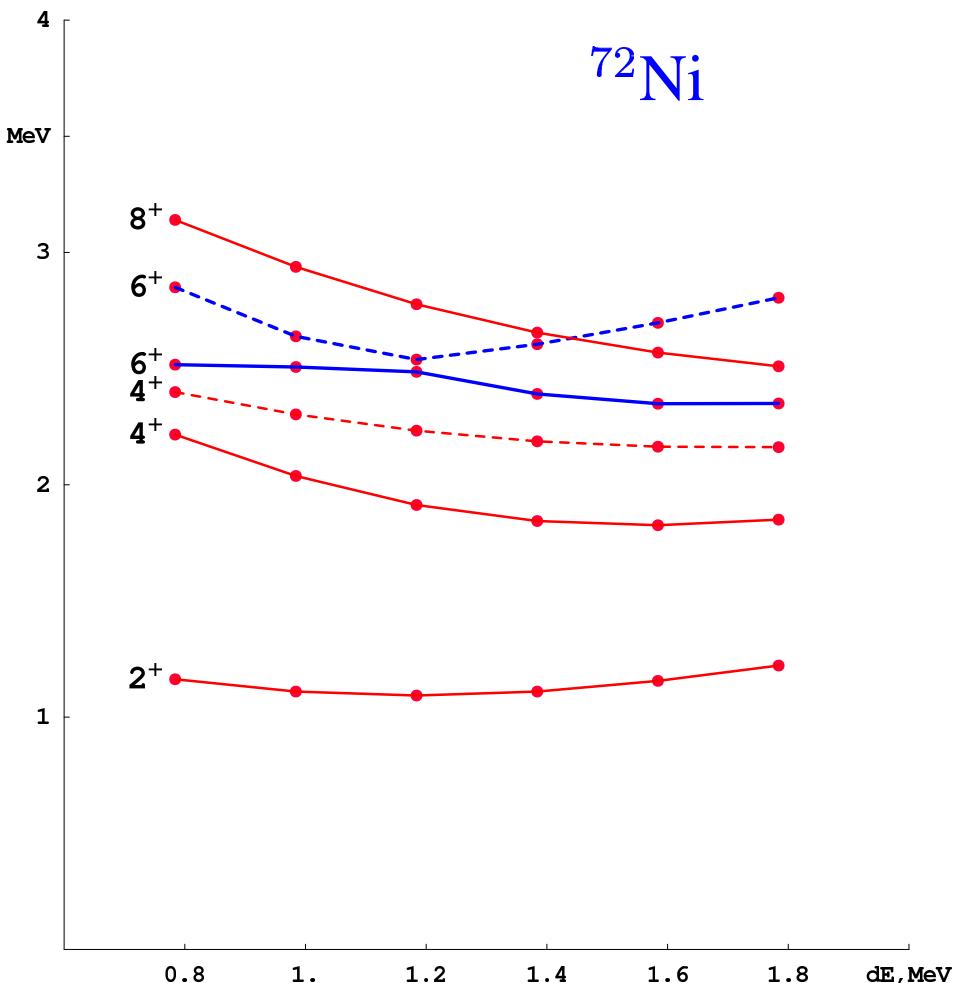
Effect of 2^+ and 4^+ $g_{9/2}^2$ tbme's on excitation energies



$$dE(2^+) = V[g_{9/2}^2]_{2+} - V[g_{9/2}^2]_{0+} \text{fit}$$

$$dE_p(2^+) = 0.7 \text{ MeV}$$

$$dE_n(2^+) = 0.4 \text{ MeV}$$



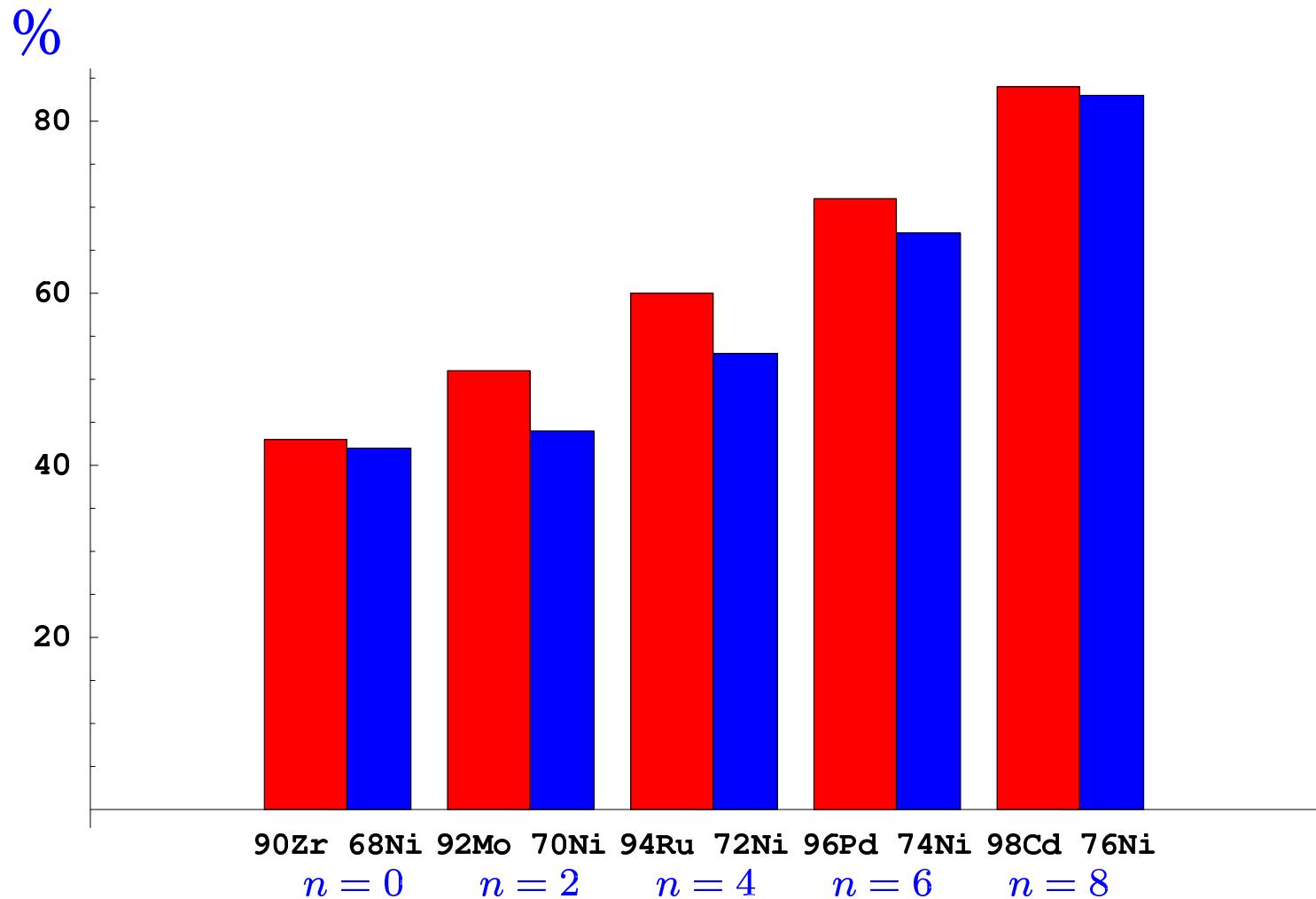
$$dE(4^+) = V[g_{9/2}^2]_{4+} - V[g_{9/2}^2]_{0+} \text{fit}$$

$$dE_p(4^+) = 1.5 \text{ MeV}$$

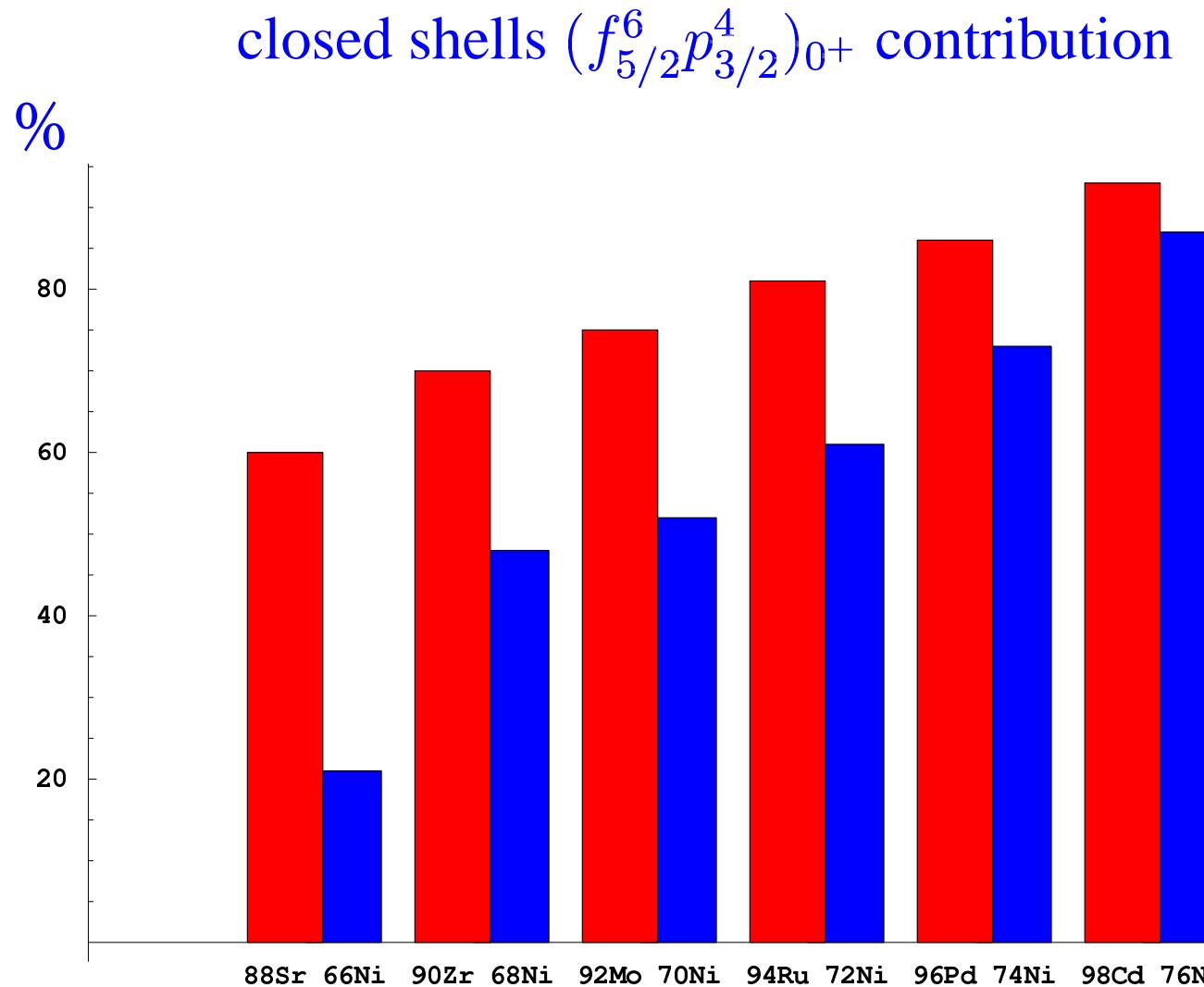
$$dE_n(4^+) = 1.1 \text{ MeV}$$

$g_{9/2}$ content

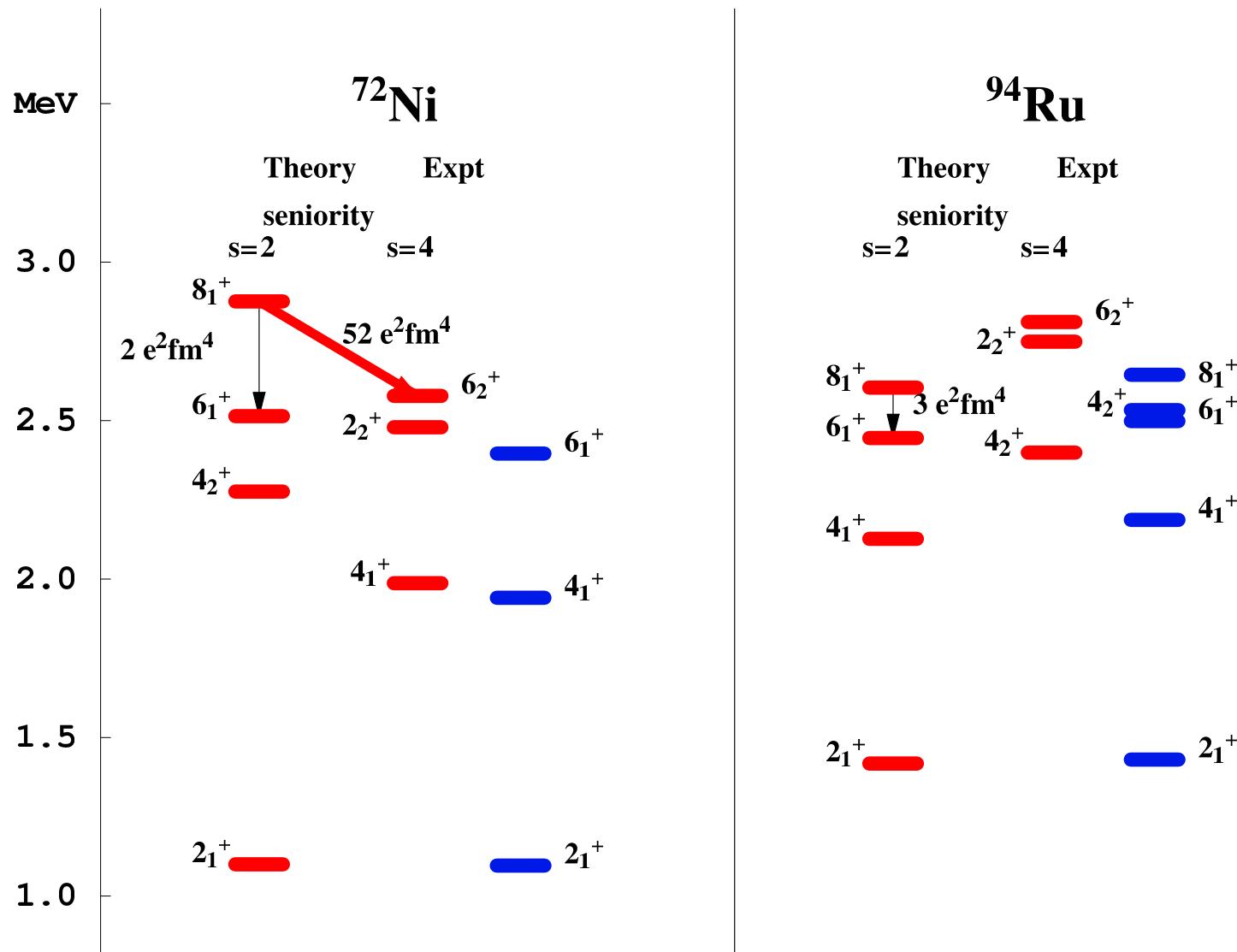
Ground state $0^+(g_{9/2})^n$ component



Contribution of the $(f_{5/2}^6 p_{3/2}^4)_{0+}$ component



Mechanism of Isomerism Disappearance in Ni isotopes



Comparison of $(g_{9/2}^2)_J$ tbmes

